

Výpočet délky lana řetězovky:

$$s_{OB} = \int_0^B ds = \int_0^{x_B} \sqrt{1 + y'^2} dx = \int_0^{x_B} \sqrt{1 + \frac{p^2 x^2}{T_0^2}} dx$$

$$= \frac{1}{2} \left[x_B \sqrt{1 + \frac{p^2 x_B^2}{T_0^2}} + \frac{T_0}{p} \ln \left(\frac{p x_B}{T_0} + \sqrt{1 + \frac{p^2 x_B^2}{T_0^2}} \right) \right]$$

Délka s_{OA} se vypočítá analogicky a celková délka je pak jejich součtem

$$s = s_{OA} + s_{OB}$$

$$\int_0^{x_B} \left(1 + \frac{p^2 x^2}{T_0^2} \right)^{\frac{1}{2}} dx = \frac{p}{T_0} \int_0^{x_B} \left(\frac{T_0^2}{p^2} + x^2 \right)^{\frac{1}{2}} dx = \left[\frac{p}{T_0} \cdot \frac{1}{2} \left(x \sqrt{x^2 + \frac{T_0^2}{p^2}} + \frac{T_0^2}{p^2} \operatorname{arcsinh} \frac{x \cdot p}{T_0} \right) \right]_0^{x_B} =$$

$$\left(\int (x^2 + a^2)^{\frac{1}{2}} dx = \frac{1}{2} \left(x \sqrt{x^2 + a^2} + a^2 \operatorname{arcsinh} \frac{x}{a} \right) \right)$$

$$= \left[\frac{1}{2} \left(x \sqrt{\frac{p^2}{T_0^2} x^2 + 1} + \frac{T_0}{p} \operatorname{arcsinh} \frac{x \cdot p}{T_0} \right) \right]_0^{x_B} = \left[\frac{1}{2} \left(x \sqrt{1 + \frac{p^2}{T_0^2} x^2} + \frac{T_0}{p} \ln \left(\frac{x \cdot p}{T_0} + \sqrt{1 + \frac{p^2}{T_0^2} x^2} \right) \right) \right]_0^{x_B} =$$

$$\left(\operatorname{arcsinh}(x) = \ln(x + \sqrt{x^2 + 1}) \right)$$

$$= \frac{1}{2} \left[x_B \sqrt{1 + \frac{p^2}{T_0^2} x_B^2} + \frac{T_0}{p} \ln \left(\frac{x_B \cdot p}{T_0} + \sqrt{1 + \frac{p^2}{T_0^2} x_B^2} \right) \right] - \emptyset$$