Simulations in Matlab

Simulink, differential equations in Simulink

Simulink

- Simulink is a graphical interface to Matlab
- Its results are time courses of variables depending on one variable, typically time
- Simulink contains built in differential equation solvers, so the discretization of differential equations is not necessary

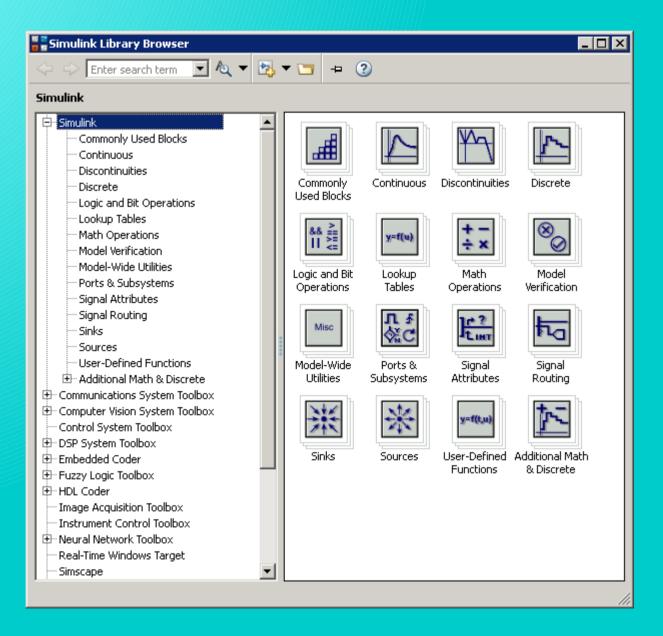
Running Simulink

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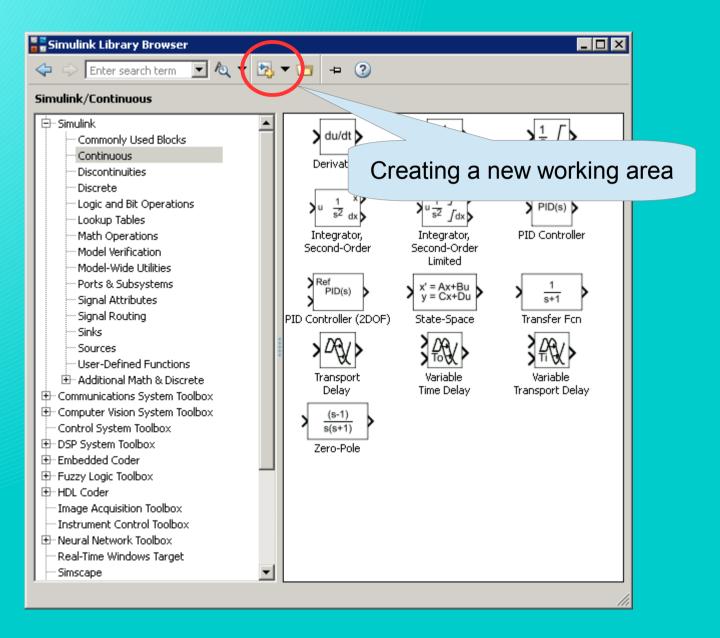
Programming in Simulink

- It is in a graphical form and it is based on placing and connecting blocks
- Blocks represent functions, connections represent variables
- Some blocks have only the output and are designates to generate variable values
- Some blocks have only the input and are designated to process the results – showing, saving, and others

Block library



Block library

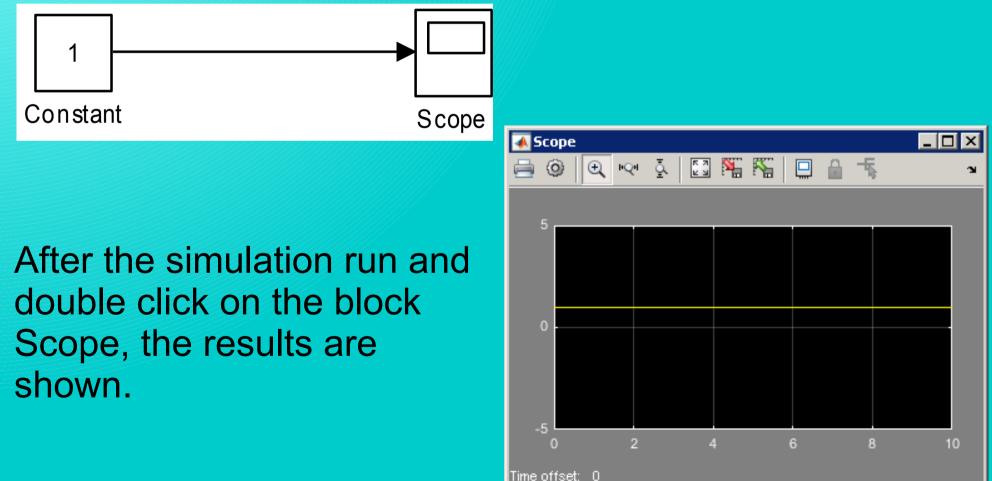


Working area for building a model

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Model/scheme in Simulink

Simple scheme is possible to build with the use of the block Constant (from Simulink/Sources) and the block Scope (from Simulink/Sinks)



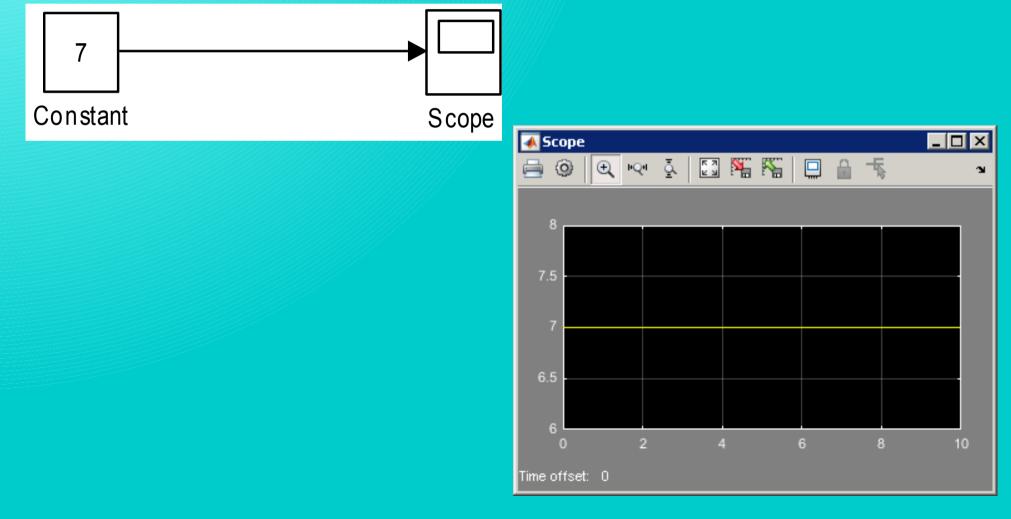
Block parameter settings

The parameters of majority of the blocks are possible to set in the dialog window that appears after double click on the chosen block.

🔁 Source	e Block Parameters: Constant 🛛 🗙	
Constar	nt	
Output the constant specified by the 'Constant value' parameter. If 'Constant value' is a vector and 'Interpret vector parameters as 1-D' is on, treat the constant value as a 1-D array. Otherwise, output a matrix with the same dimensions as the constant value.		
Main Signal Attributes		
Constant value:		
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0	OK <u>C</u> ancel <u>H</u> elp <u>Apply</u>	

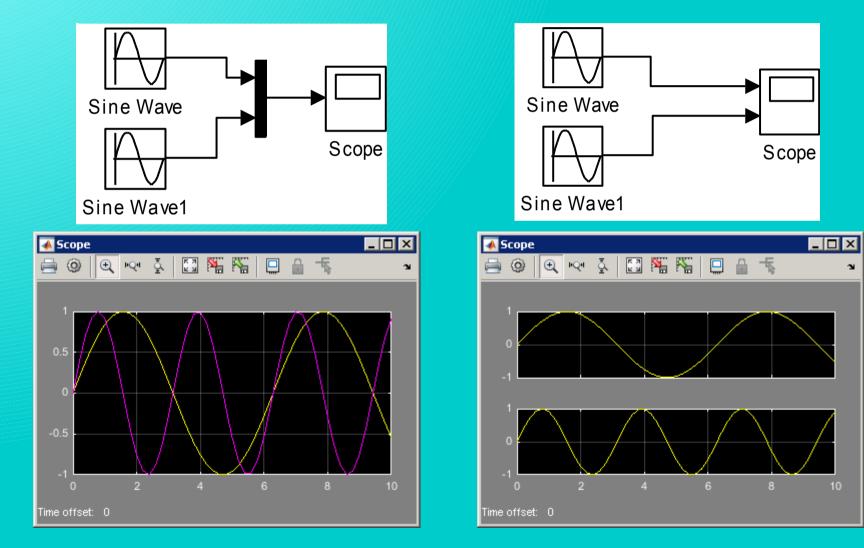
Model/scheme in Simulink

After the change of predefined value in the block Constant, the result is changed (it is necessarz to run the simulation again)



Showing more courses in one block Scope

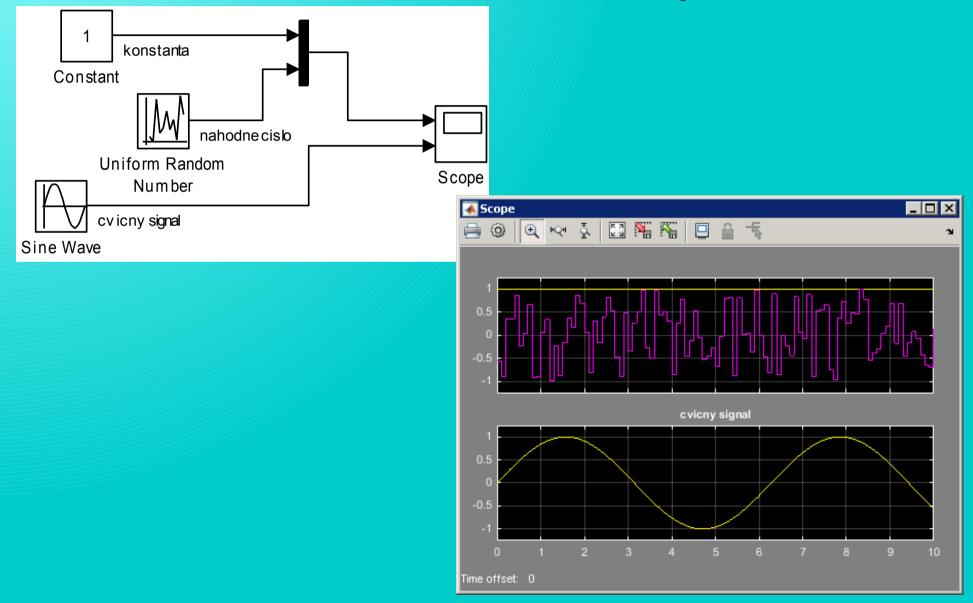
By the use of a bock Mux (from Simulink/Signal Routing) or by setting of more inputs to the block Scope



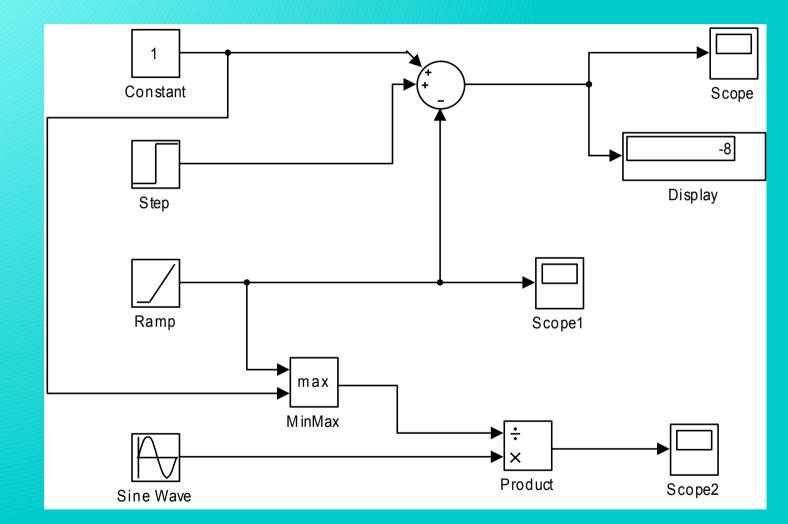
Showing more courses in one block Scope

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Showing more courses in one block Scope



Demonstration scheme



Scheme contains blocks from libraries Simulink/Sources, Simulink/Sinks a Simulink/Math Operations

Demonstration scheme

Block parameter settings in the demonstration scheme:

🚹 Function Block Parameters: Sum	
Sum Add or subtract inputs. Specify one a) string containing + or - for each ir (e.g. ++ - ++) b) scalar, >= 1, specifies the number When there is only one input port, ac	Function Block Parameters: Product Product Multiply or divide inputs. Choose element-wi specify one of the following: a) * or / for each input port. For example, *
dimensions or one specified dimension Main Signal Attributes Icon shape: round List of signs:	uii u2/us u4. b) scalar specifies the number of input ports If there is only one input port and the Multipli Element-wise(.*), a single * or / collapses the specified operation. However, if the Multiplica Matrix(*), a single * causes the block to output the material single / causes the block to output the mate
++ - Sample time (-1 for inherited): -1	Main Signal Attributes Number of inputs: /* /* Multiplication: Element-wise(.*) Sample time (-1 for inherited): -1
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Simulation time and simulation step

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	Higher priority value indicates higher task priority			
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Simulation time an simulation step

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There is one rule – avoiding block Derivation if it is possible.

The first step is separation of the highest derivation.

 $2(\dot{y})+3 y=0,5 u$

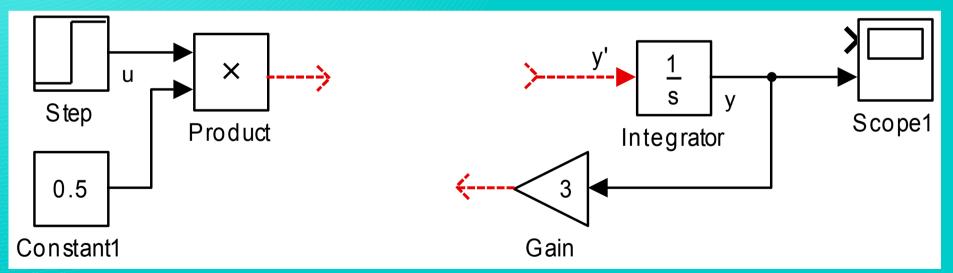
 $\underbrace{y}_{\neq} = \frac{0,5 \, u - 3 \, y}{2}$

Then it is suitable to put all necessary variables into the scheme. $\dot{y} = \frac{0.5u-3y}{2}$



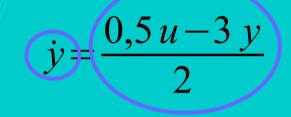
The next step is to multiply the variables by constants.

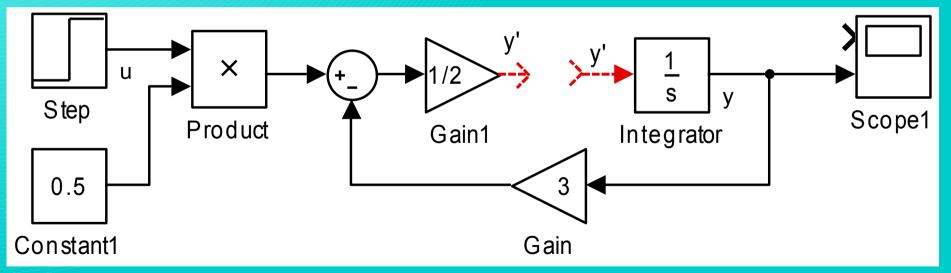
 $\dot{y} = \frac{0.5 u - 3 y}{2}$



When multiplying by a constant, it is possible to use either the block Gain or the blocks Product and Constant.

Then the conversion of the fraction can be finished.

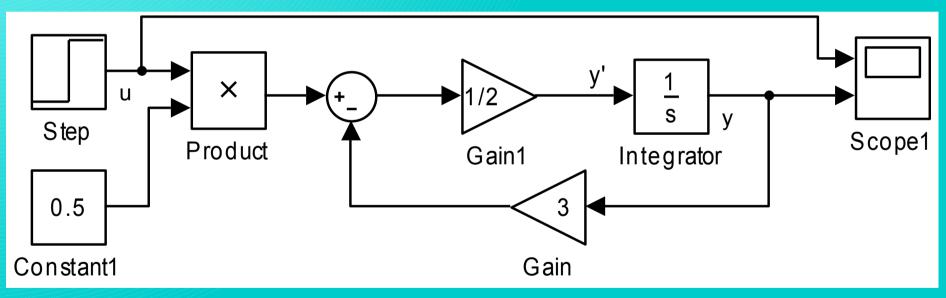


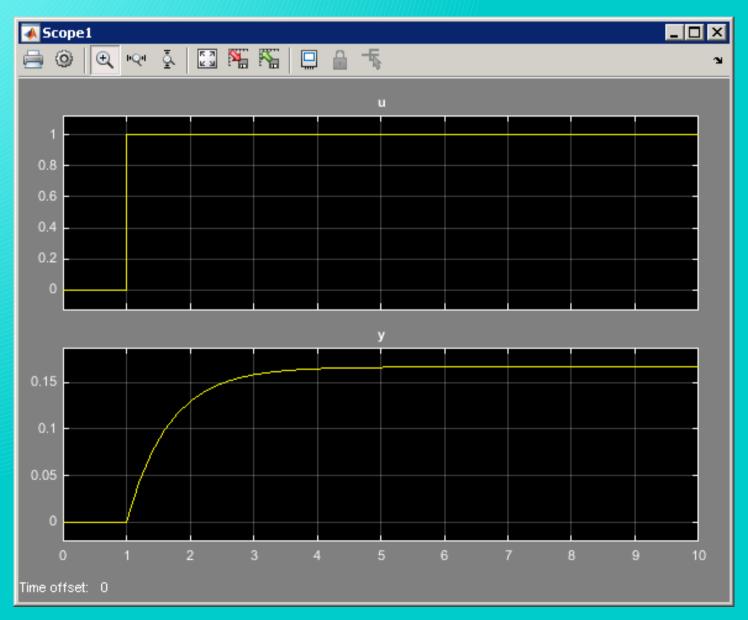


Both, the left side and the right side of the equation are finished now. As the values of both sides must be equal, both sides can be connected.

 $\frac{0,5 \, u - 3 \, y}{2}$

The final Simulink model is get by connecting left and right side of the scheme.Then the simulation can be run.



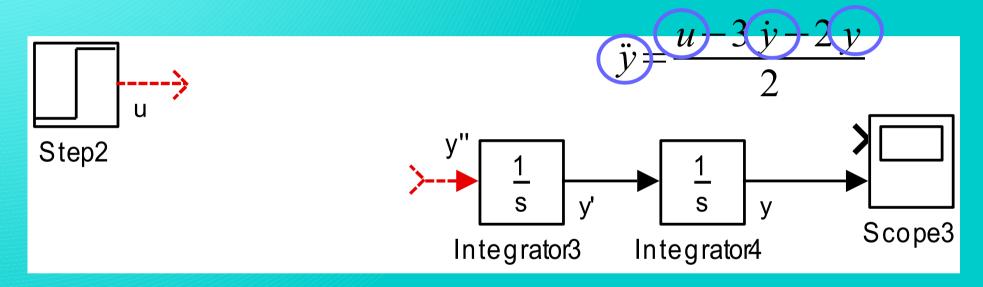


Similar procedure can be used also for differential equations of higher orders.

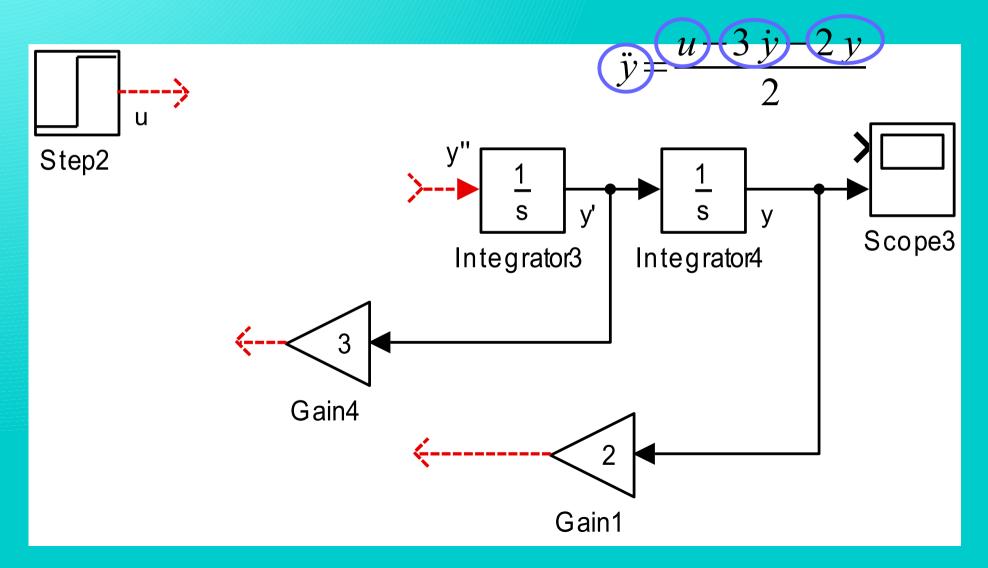
$$2\ddot{y}+3\dot{y}+2y=u$$

$$\underbrace{\ddot{y}}_{2} = \frac{u - 3 \dot{y} - 2 y}{2}$$

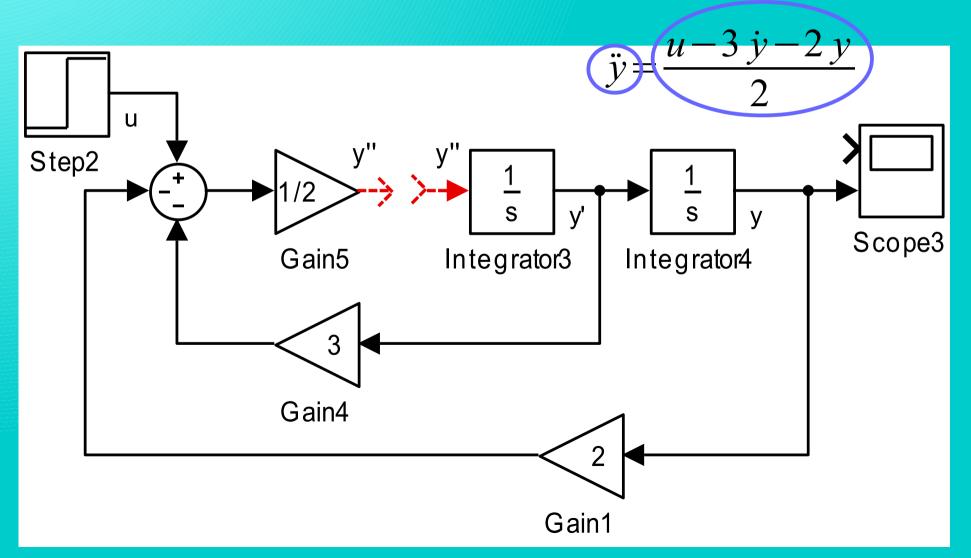
Preparing the variables into the model:



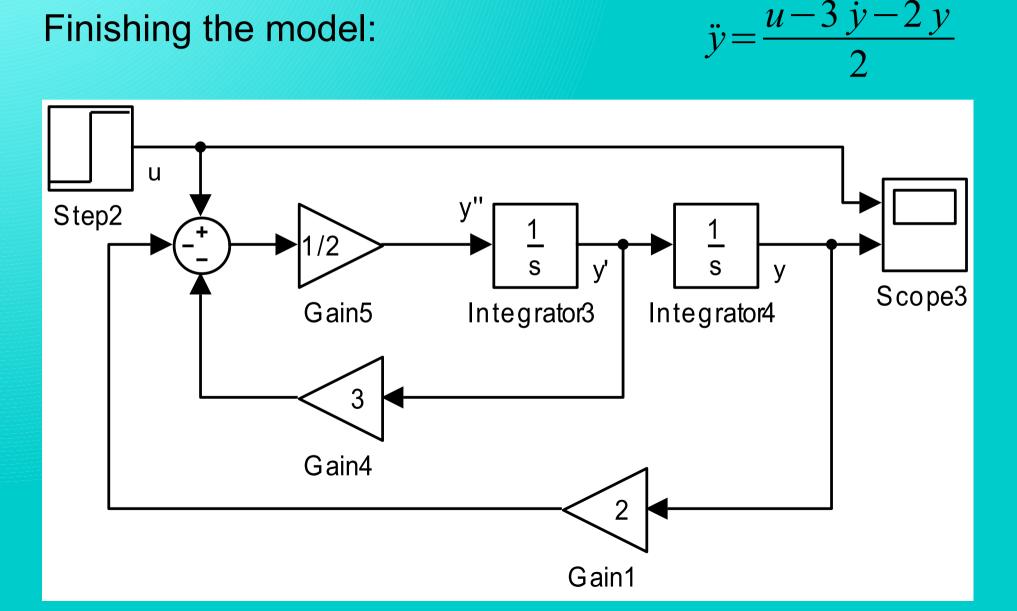
Multiplying variables by constants:

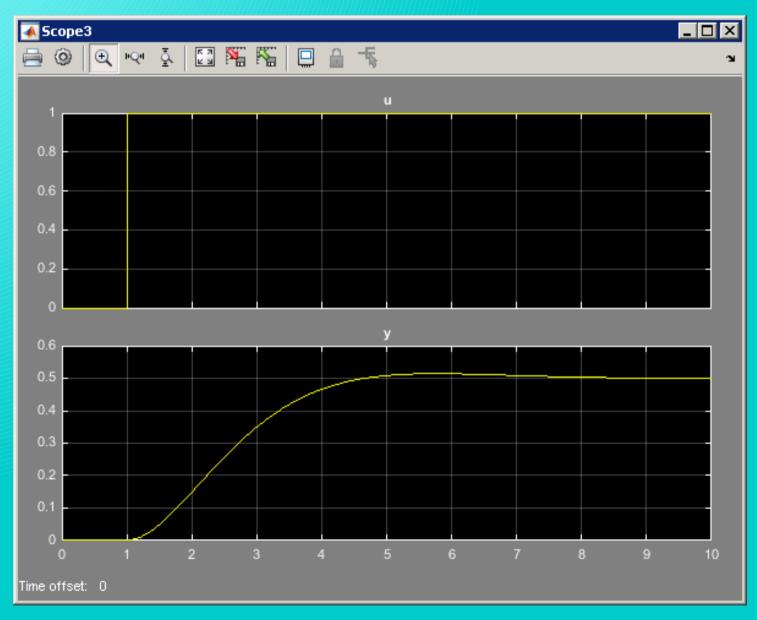


Finishing the fraction:



Finishing the model:





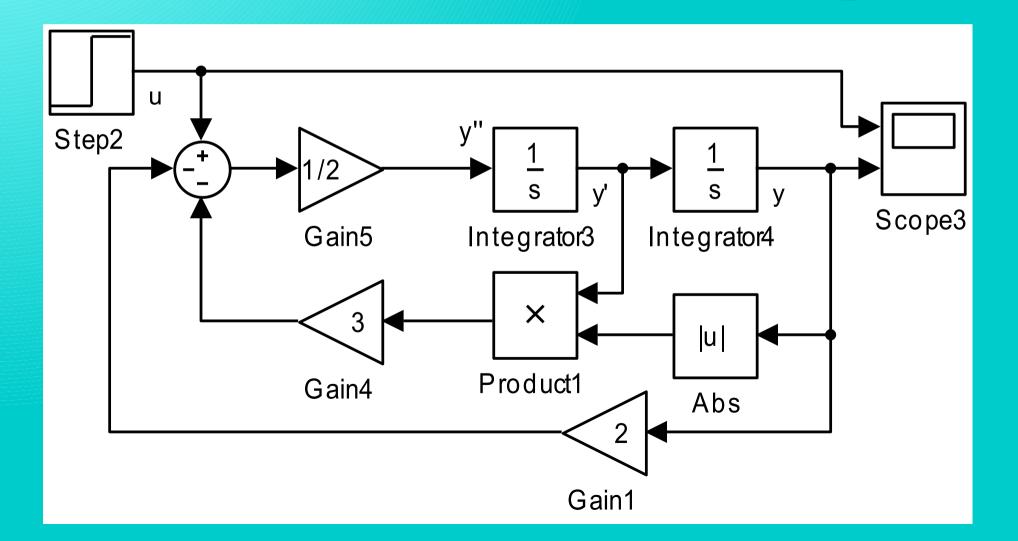
Similar procedure can be used also when the differential equation is non-linear

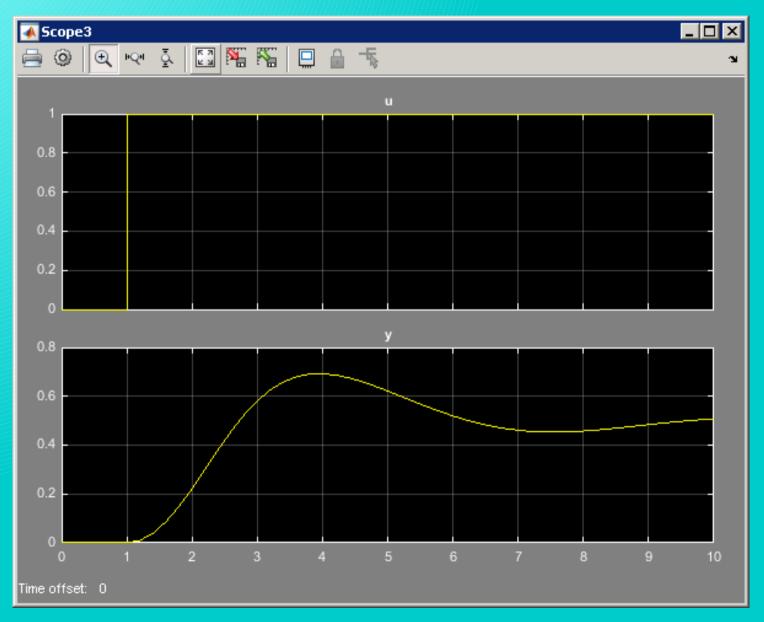
$$2\ddot{y}+3\dot{y}|y|+2y=u$$

$$\underbrace{\ddot{y}}_{2} = \frac{u - 3 \dot{y}|y| - 2 y}{2}$$

Conversion of a differential equation into a Simulink model $\ddot{y} = \frac{u - 3\dot{y}|y|}{2}$

... that leads to a model:





Individual task

Create a Simulink model reprenting following differential equation:

\ddot{y} +5,5 \ddot{y} +3,5 \ddot{y} +5 \ddot{y} + \dot{y} +y=u