



Analysis of Solar Flat-plate Collectors

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Content of lectures today

- design tool KOLEKTOR for theoretical analysis of flat-plate collectors
 - introduction into software
 - downloading, installation, support files, ...
- theoretical modelling of collector heat output „step by step“
 - external energy balance of absorber
 - internal energy balance of absorber
- what influences annual energy yields of collector
- examples solved with use of KOLEKTOR and annual simulation in TRNSYS



Design Tool KOLEKTOR 2.2 for Virtual Prototyping of Solar Flat-plate Collectors

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Background & Motivation

Lack of software for solar thermal collector modeling:

- detailed parameters of solar collector
 - detailed calculation of heat transfer
 - user friendly
 - general use
 - freely available [CoDePro \(Madison\)](#), [TRNSYS Type 103 \(CSTB\)](#)
-
- wide application range for FP collectors
(evacuated, building integrated, transparent cover structures, HT fluids)
 - versatile for different heat transfer models (convection, sky radiation)



Model inputs and outputs

Inputs:

- detailed parameters of individual parts of solar collector geometry, thermophysical parameters, optical parameters
- climatic conditions: ambient temperature, irradiation, wind velocity
- operation conditions: **input temperature t_{in}** , mass flowrate **m** , slope **β**

Outputs:

- efficiency curve **η** (based on aperture area **A_a**)
- output temperature from solar collector **t_{out}**
- detailed temperature distribution in collector, heat transfer coefficients



Principle of calculation

- external balance of absorber

heat flow from absorber surface to ambient

temperature distribution at main collector levels (nodes **p**, **z**, **b**)

overall *U*-value of collector

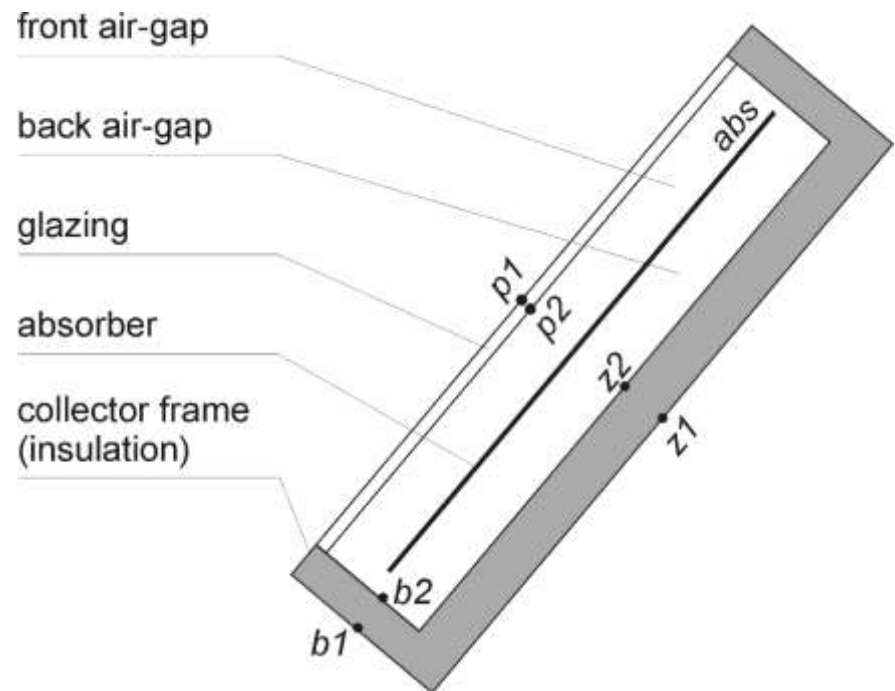
- internal balance of absorber

heat flow from abs.surface to fluid

heat removal factor F_R

absorber temperature t_{abs}

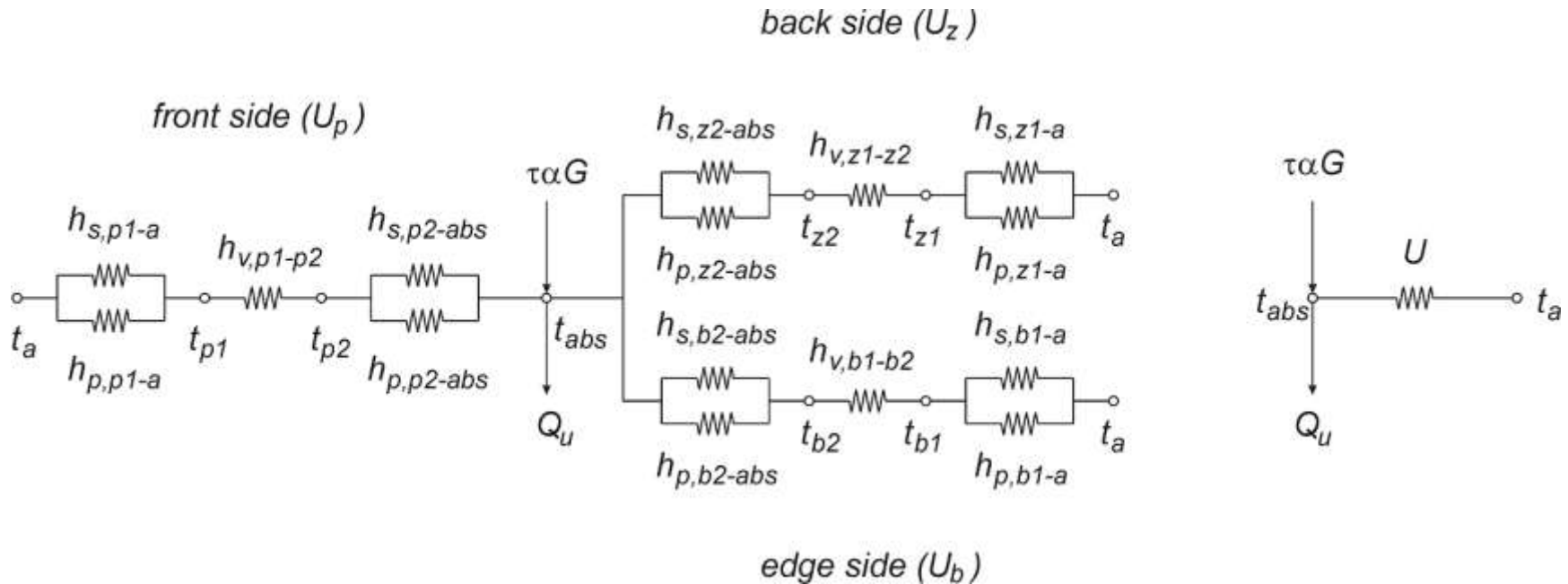
heat gain Q_u



$$\dot{Q}_u = A_a F_R [\tau \alpha G - U(t_{in} - t_a)]$$



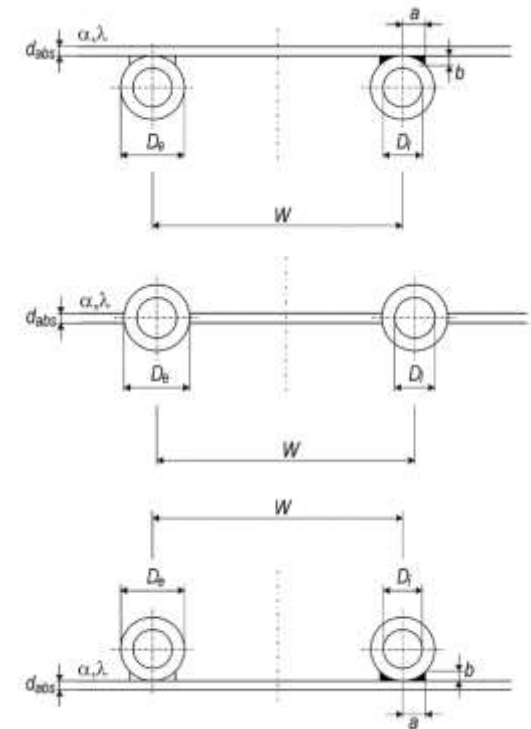
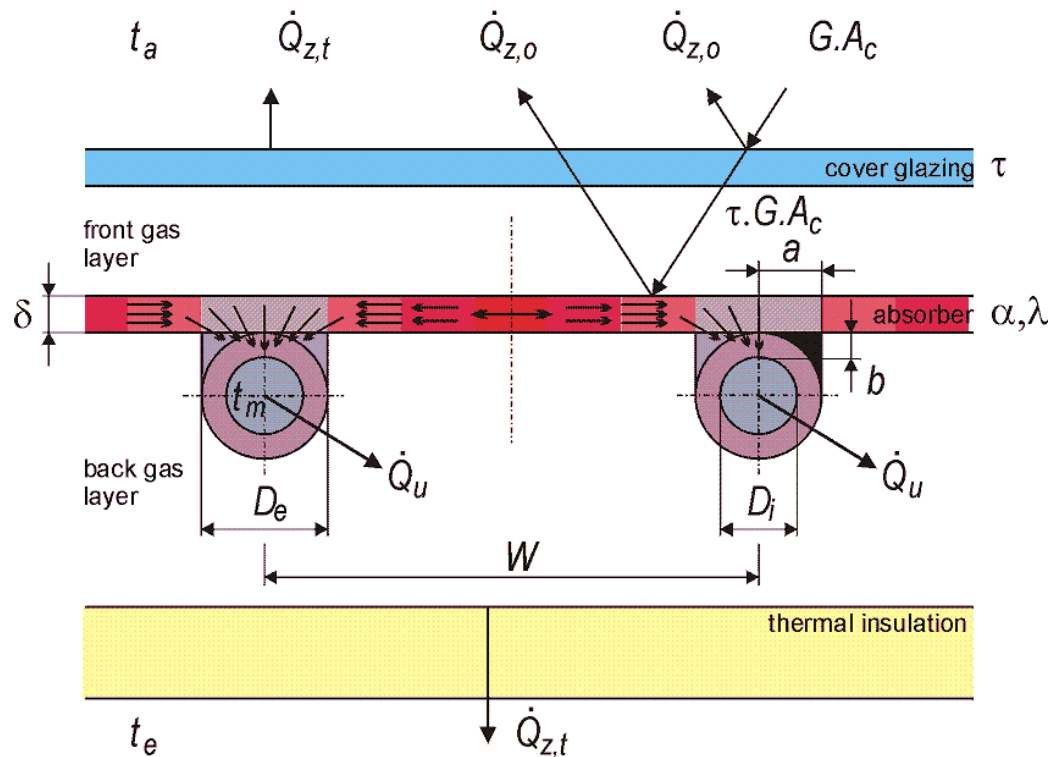
External balance of absorber



- heat transfer coefficients calculation based on temperatures of main nodes
- iteration loop for temperature of nodes (starting values based on t_{abs} , **U-value calculation**, reverse calculation of temperature distribution)
- starting absorber temperature is estimated from **input temperature** ($t_{abs} = t_{in} + 10 \text{ K}$)



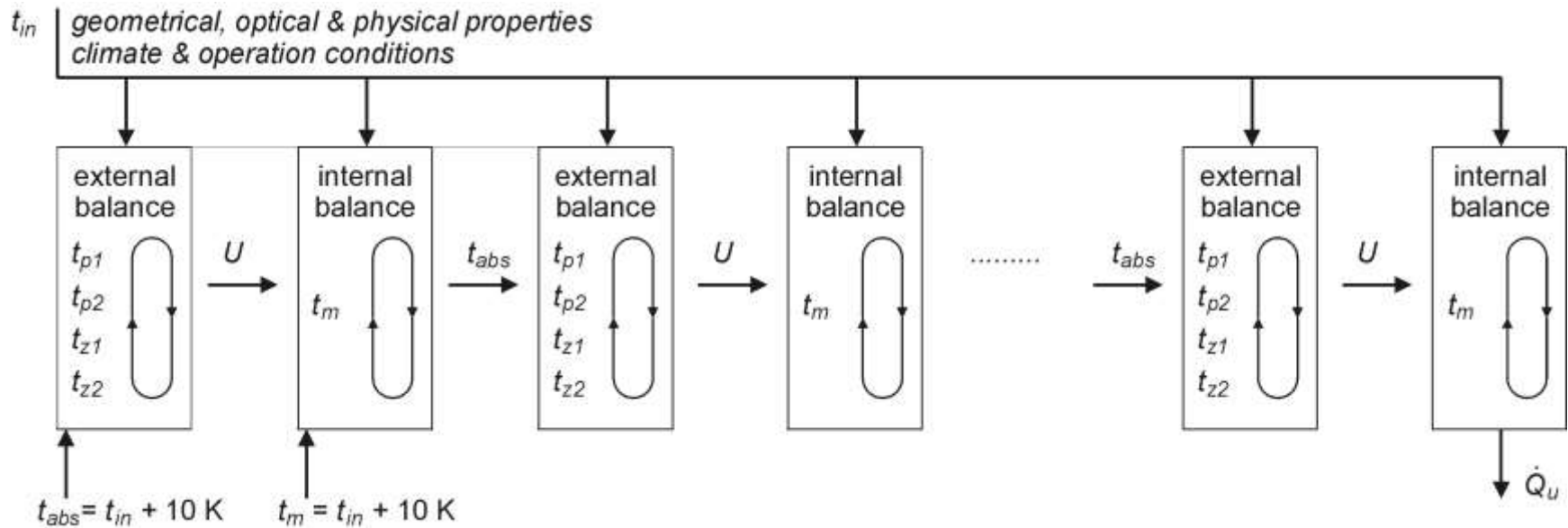
Internal balance of absorber



- heat transfer by fin conduction, bond conduction and forced convection in pipes
- iteration loop for mean fluid temperature (starting values based on t_{in} , F_R calculation, reverse calculation of mean fluid temperature), **absorber temperature calculation**
- starting mean fluid temperature is estimated from input temperature ($t_m = t_{in} + 10 \text{ K}$)



Calculation procedure



external and internal balance iteration loops (5 loops enough)

superior iteration loop governing output / inputs



Design tool KOLEKTOR 2.2 (2009)

- model converted into program based on Visual Basic Studio
- concept of “cards” for data inputs
- selections in rolling windows
- default settings
- saving settings of parameters, loading settings
- installation pack 400 kB (zipped)
- installation for Win XP presume Microsoft.NET Framework installed
- new Windows include the Framework environment



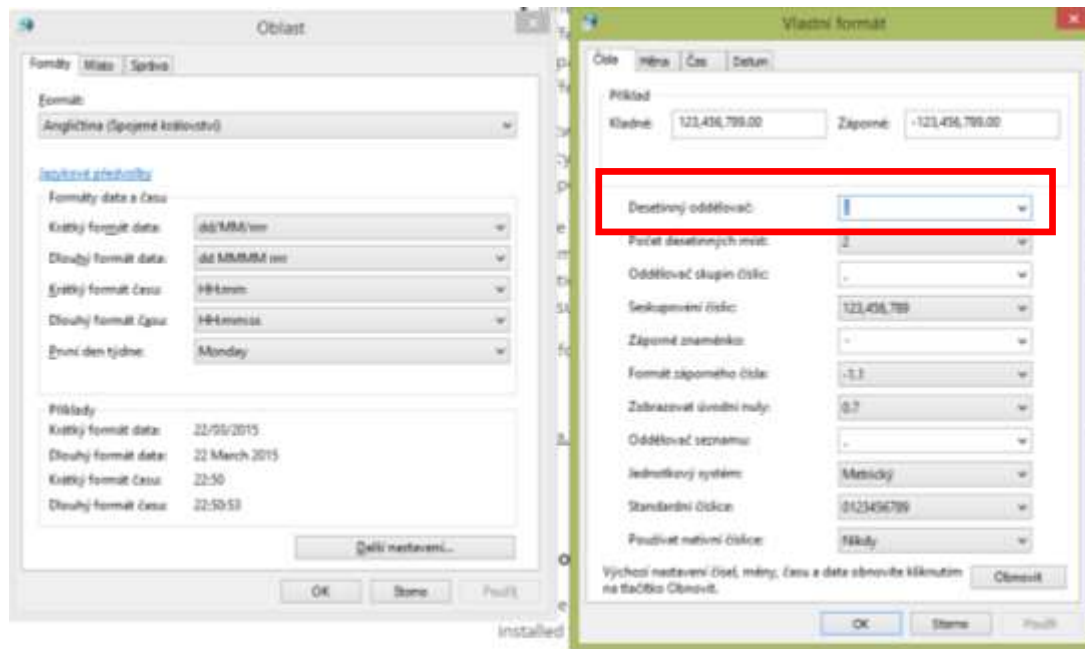
Features and availability

- user-friendly software KOLEKTOR 2.2 is useful for analysis, design and prototyping
- several experimental validations have been performed based on commercial collectors testing
- software tool KOLEKTOR 2.2 is freely available at:
http://users.fs.cvut.cz/tomas.matuska/?page_id=194
- mathematical reference handbook as **pdf**
 - theoretical background of the tool
 - downloadable



Preparation for installation

- **local settings in Windows - change to Great Britain settings**
- e.g. windows 8 – Control Panel – Language
- change of datum, time or number format
- further settings – **using dot in decimal values**



do it now ...



Download KOLEKTOR and install now ...

- http://users.fs.cvut.cz/tomas.matuska/?page_id=194
- download **kolektor22.zip**
- unzip it Program files – folder Kolektor will be created
- start setup.exe – start installation process
- setup also opens the program
- for Windows versions higher than XP **you don't need**
Microsoft.NET Framework should be included in ...



Design tool KOLEKTOR 2.2 (2009)





Design tool KOLEKTOR 2.2

Kolektor 2.2 File Calculation Help

Design parameters Absorber Glazing and insulation Calculation

Operation and climatic conditions

Input fluid temperature	t_{in}	50	°C
Specific fluid mass flow rate	m'	0.02	kg/s/m ²
Global solar irradiation	G	800	W/m ²
Ambient temperature	t_a	20	°C
Ambient relative humidity	ϕ_a	50	%
Wind velocity	w	4	m/s
Collector slope	β	45	deg
Envelope thermal resistance	R_k	6	m ² K/W

Collector dimensions

Gross height	L_g	2	m
Gross width	H_g	1	m
Gross area	A_g	2	m ²
Aperture height	L_a	2	m
Aperture width	H_a	1	m
Aperture area	A_a	2	m ²
Envelope dimensions		2 x 1	m

Type of collector installation

☐ Separate
☒ Integrated into building envelope

Collector depth

Absorber-glazing gap thickness	d_p	20	mm
Absorber-frame gap thickness	d_z	20	mm
Collector depth	B	0.09	m
Edge sides area	A_b	0.57	m ²

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Design tool KOLEKTOR 2.2

Kolektor 2.2 File Calculation Help

Design parameters Absorber Glazing and insulation Calculation

Absorber parameters

Material: Copper Solar absorptance: α_{abs} 0.95

Thermal conductivity: λ_{abs} 390 W/mK Front surface emissivity: $\varepsilon_{abs,p}$ 0.05

Thickness: d_{abs} 0.2 mm Back surface emissivity: $\varepsilon_{abs,z}$ 0.5

Pipe register parameters

Length of riser pipes: L 2 m Collector mass flow rate: M' 0.04 kg/s

Number of riser pipes: ntp 10 pcs Pipe mass flow rate: $M1'$ 0.004 kg/s

Distance between riser pipes (fin): W 100 mm

Pipe external diameter: D_e 10 mm

Pipe internal diameter: D_i 8 mm

Type of bond: Upper

Average bond width: a 3 mm

Average bond thickness: b 3 mm

Bond thermal conductivity: λ_{sp} 300 W/mK

Bond thermal conductance: C_{sp} 300 W/mK

Heat transfer fluid

Fluid type: Water Water

Mixing ratio: 0 % 100 %

Freezing temperature: t_f 0 °C

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Design tool KOLEKTOR 2.2

Kolektor 2.2 File Calculation Help

Design parameters Absorber Glazing and insulation Calculation

Glazing parameters

Material: Glass

Thickness: d_{gl} 4 mm

Normal solar transmittance: τ_n 0.92

Normal solar reflectance: ρ_n 0.06

Diffuse solar reflectance: ρ_d 0.6

External surface emissivity: ε_{p1} 0.85

Internal surface emissivity: ε_{p2} 0.85

Thermal properties

☒ Thermal conductivity

☐ Thermal resistance

Thermal conductivity (polynomic): λ 0.8 W/mK

$\lambda = \lambda_0 + \lambda_1 t + \lambda_2 t^2$

λ_1 0 W/mK²

λ_2 0 W/mK³

Frame / insulation parameters

Material: Polyurethane

Thickness: d_{fr} 50 mm

Thermal conductivity: λ_{fr} 0.035 W/mK

Thermal resistance: R_{fr} 1.43 m²K/W

External frame surface emissivity: $\varepsilon_{f,z1}$ 0.5

Internal frame surface emissivity: $\varepsilon_{f,z2}$ 0.5

Gas filling of collector interior

Type of gas: Air

Gas pressure: 100 kPa

Optical efficiency of collector

Effective α_p product: 0.874

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Design tool KOLEKTOR 2.2

Kolektor 2.2 File Calculation Help

Design parameters Absorber Glazing and insulation Calculation

GLAZING **ABSORBER** **FRAME / INSULATION**

$t_a = 20 \text{ } ^\circ\text{C}$
 $t_{p1} = 88.81 \text{ } ^\circ\text{C}$
 $t_{p2} = 97.94 \text{ } ^\circ\text{C}$
 $t_{out} = 393.1 \text{ } ^\circ\text{C}$
 $t_{z2} = 368.3 \text{ } ^\circ\text{C}$
 $t_{z1} = 30.56 \text{ } ^\circ\text{C}$
 $t_a = 20 \text{ } ^\circ\text{C}$

Radiation p1 - a: EN 6946, $h_s = 6.848 \text{ W/m}^2\text{K}$
 Convection p1 - a: McAdams, $h_p = 19.7 \text{ W/m}^2\text{K}$ for all w
 Radiation abs - p2: $F' = 0.914$, $F_R = 0.887$, $h_s = 1.616 \text{ W/m}^2\text{K}$
 Convection abs - p2: Niemann, $h_p = 4.892 \text{ W/m}^2\text{K}$ for slope 45°
 Radiation abs - z2: $h_s = 20.43 \text{ W/m}^2\text{K}$
 Convection abs - z2: Niemann, $h_p = 2.655 \text{ W/m}^2\text{K}$ for any slope
 Radiation z1 - a: $h_s = 2.679 \text{ W/m}^2\text{K}$
 Convection z1 - a: McAdams, $h_p = 19.7 \text{ W/m}^2\text{K}$

$t_{abs} = 378.6 \text{ } ^\circ\text{C}$
 $t_m = 401.0 \text{ } ^\circ\text{C}$

$p1$ $p2$ $t_{in} = 409 \text{ } ^\circ\text{C}$ $z1$ $z2$ $t_{stg} = 211 \text{ } ^\circ\text{C}$

Forced convection in pipes: Laminar (Shah), Turbulent (Colburn), h_i (Laminar) = 517 $\text{W/m}^2\text{K}$
 Iteration: Number of loops = 10
 Calculation: ☐ For given t_{in} , ☒ Efficiency curve calculation

Calculate

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Default example – usual collector

- download as **default.kol** File – Open – default.kol
http://users.fs.cvut.cz/tomas.matuska/?page_id=194 as zip file
- main default collector parameters
 - solar glazing , transmittance 91 %
 - standard flat-plate collector with selective coating:
 $\varepsilon = 5 \%$ $\alpha = 95 \%$
 - cooper absorber 0.2 mm, risers 10/8 mm, distance 112 mm
 - absorber – glazing gap 20 mm, absorber – insulation gap 5 mm
 - insulation thickness 30 mm, mineral wool
 - slope of collector 45°



Calculation possibilities in collector

- **calculation for given t_{in}**
- analysis of heat transfer at individual parts of collector
- you can play with models ... and see the impact



Calculation possibilities in collector

- **efficiency curve calculation**
run calculation
- range if t_{in} from 10 °C to 400 °C
to cover also high-temperature collectors
- results can be saved to file = text file, columns separated by semicolon ;
- get the efficiency coefficients η_0 , a_1 , a_2 by use of **evaluation.xls**
http://users.fs.cvut.cz/tomas.matuska/?page_id=194
- **important** – set the dots for decimals also in Excel settings



Solar DHW simulation in TRNSYS

- **download** example SDHW – simple solar system, modified for this Solnet course
- climate data Wurzburg (in data folder)
- daily load 200 l, cold water 10 °C, hot water 55 °C
- collector area 4 m², storage tank 200 l, no pipes ... simplified
- **annual energy yields for changed construction of collector**
- reference case:
 - annual yields of collector **1887 kWh/a**
 - solar fraction **50 %**



Analysis of Solar Flat-plate Collectors – part 1

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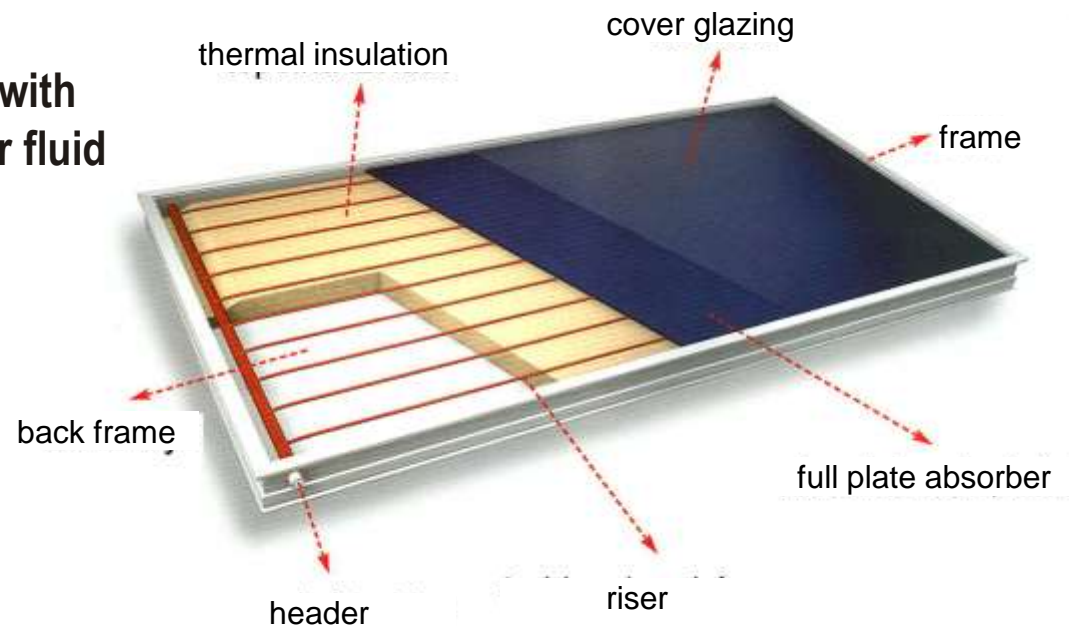
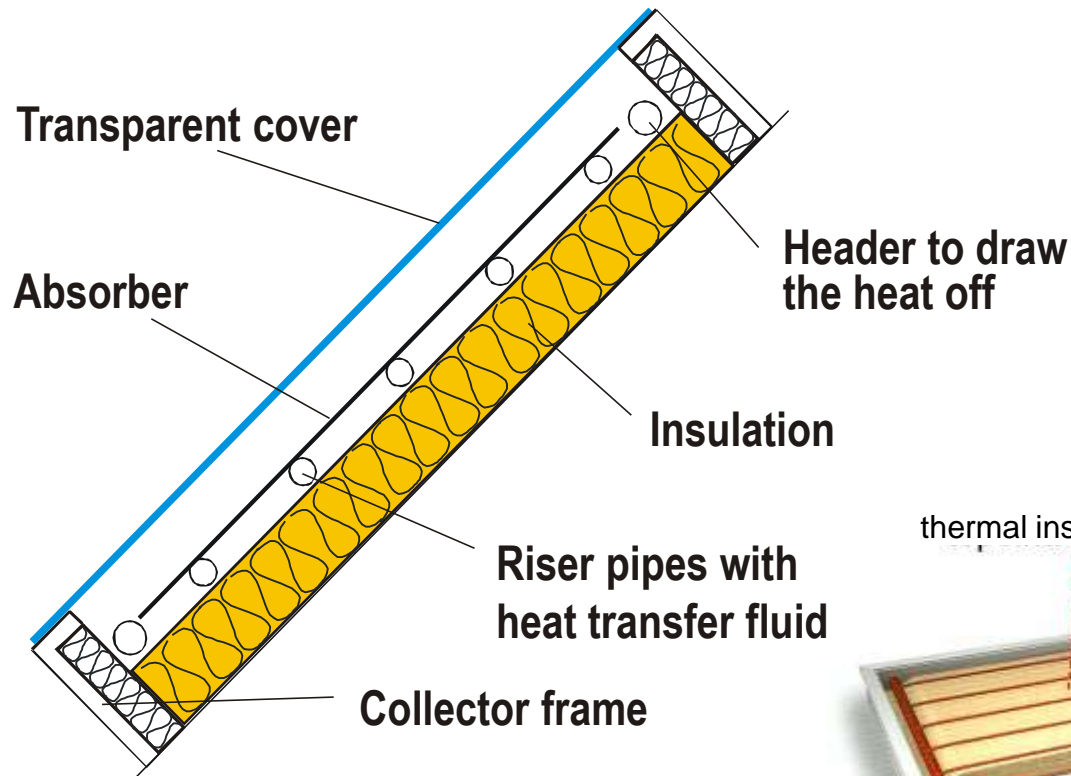


Content

- how to calculate thermal output of solar collector on theoretical basis
 - from detailed data on construction
 - at given operation conditions
 - with use of different alternative models of heat transfer phenomena
- to predict the influence of
 - change in construction of the collector
 - operation conditions
- on efficiency curve
- on annual energy yields of the collector

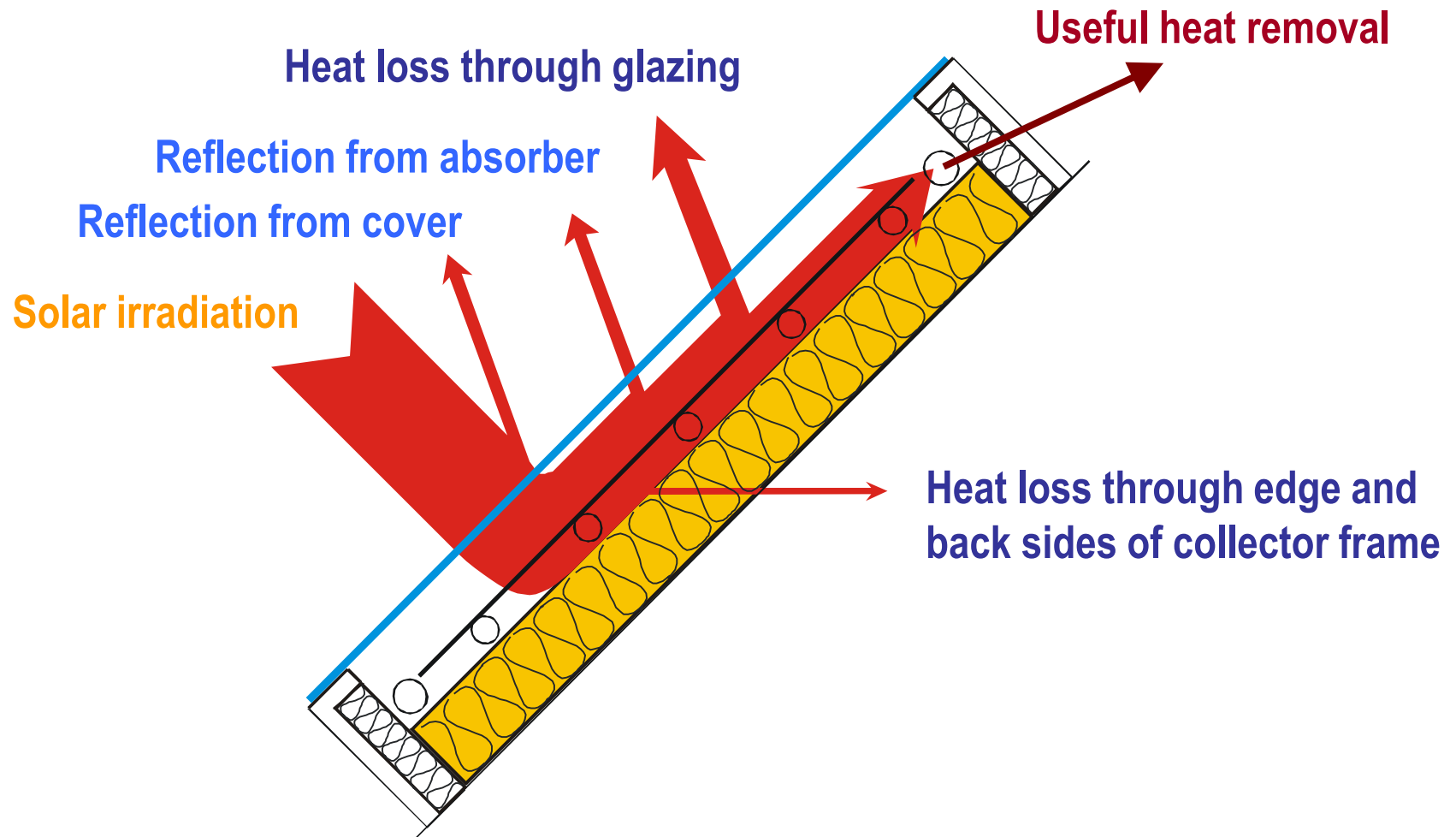


Solar thermal flat-plate collector





Solar collector energy balance





Solar collector energy balance

- **External energy balance of absorber**
 - heat flow from absorber surface to ambient environment
 - heat losses of the collector
 - quality of solar collector envelope

- **Internal energy balance of absorber**
 - heat flow from absorber surface into heat transfer fluid
 - ability to transfer heat and remove it from collector
 - quality of absorber construction



External energy flows balance of absorber

$$\frac{dQ}{dt} = \dot{Q}_s - \dot{Q}_{l,o} - \dot{Q}_{l,t} - \dot{Q}_u \quad \text{general description}$$

$$\text{steady state } dQ/dt = 0 \quad \dot{Q}_u = \dot{Q}_s - \dot{Q}_{l,o} - \dot{Q}_{l,t}$$

Q_s solar energy input [W]

$$Q_s = G.A_c$$

$Q_{l,o}$ optical losses [W]

$$Q_{l,o} = Q_s - Q_s(\tau\alpha)_{ef}$$

$Q_{l,t}$ thermal losses [W]

$$Q_{l,t} = U.A_c (t_{abs} - t_a)$$

Q_u useful heat removed from collector [W]

$$Q = Mc(t_{out} - t_{in})$$



External energy balance: efficiency

useful heat output:

$$\dot{Q}_u = GA_c(\tau\alpha)_{ef} - UA_c(t_{abs} - t_a)$$

efficiency:

$$\eta = \frac{\dot{Q}_u}{\dot{Q}_s} = \frac{\dot{Q}_u}{GA_c} = \frac{GA_c(\tau\alpha)_{ef} - UA_c(t_{abs} - t_a)}{GA_c}$$

$$\eta = (\tau\alpha)_{ef} - U \frac{(t_{abs} - t_a)}{G}$$



Efficiency formulas

$$\eta = (\tau\alpha)_{\text{ef}} - U \frac{(t_{\text{abs}} - t_a)}{G}$$

external balance, losses

$$\eta = F' \left[(\tau\alpha)_{\text{ef}} - U \frac{(t_m - t_a)}{G} \right]$$

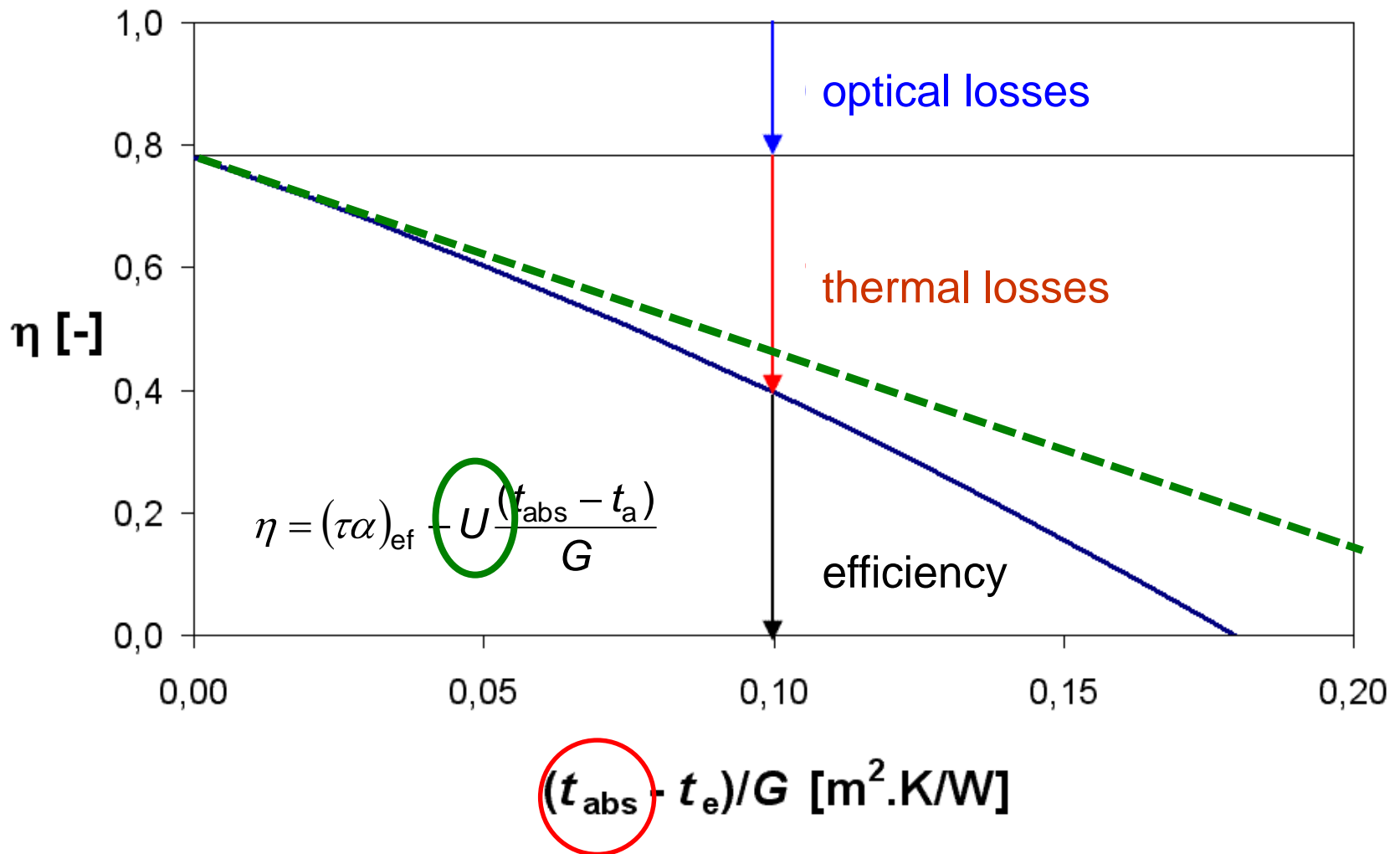
+ internal balance
influence of absorber design
European standards

$$\eta = F_R \left[(\tau\alpha)_{\text{ef}} - U \frac{(t_{\text{in}} - t_a)}{G} \right]$$

+ influence of flowrate,
specific heat of fluid
US standards

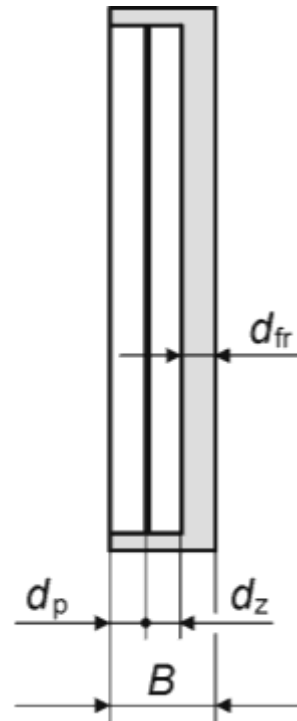
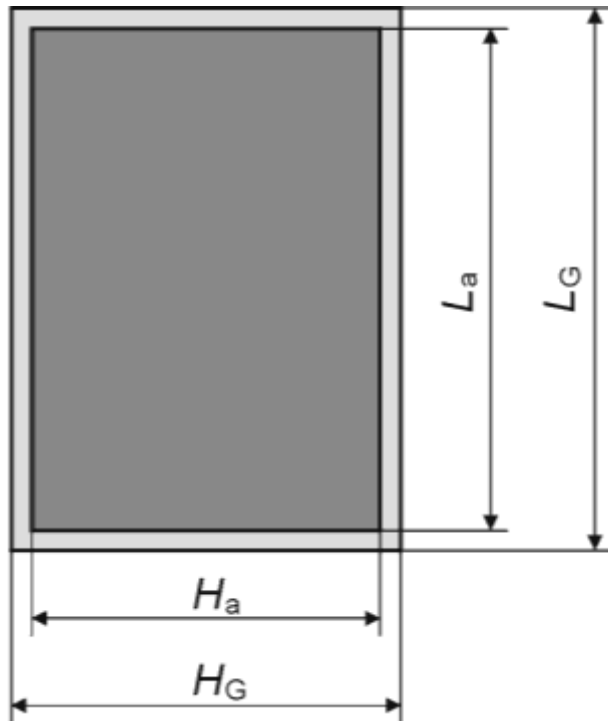


Solar collector efficiency (based on t_{abs})





Reference area for calculations



gross area: A_G

maximum area = $H_G \cdot L_G$

edge side area: A_b

$(2H_G + 2L_G) \cdot B$

aperture area: A_a

area of glazing = $H_a \cdot L_a$



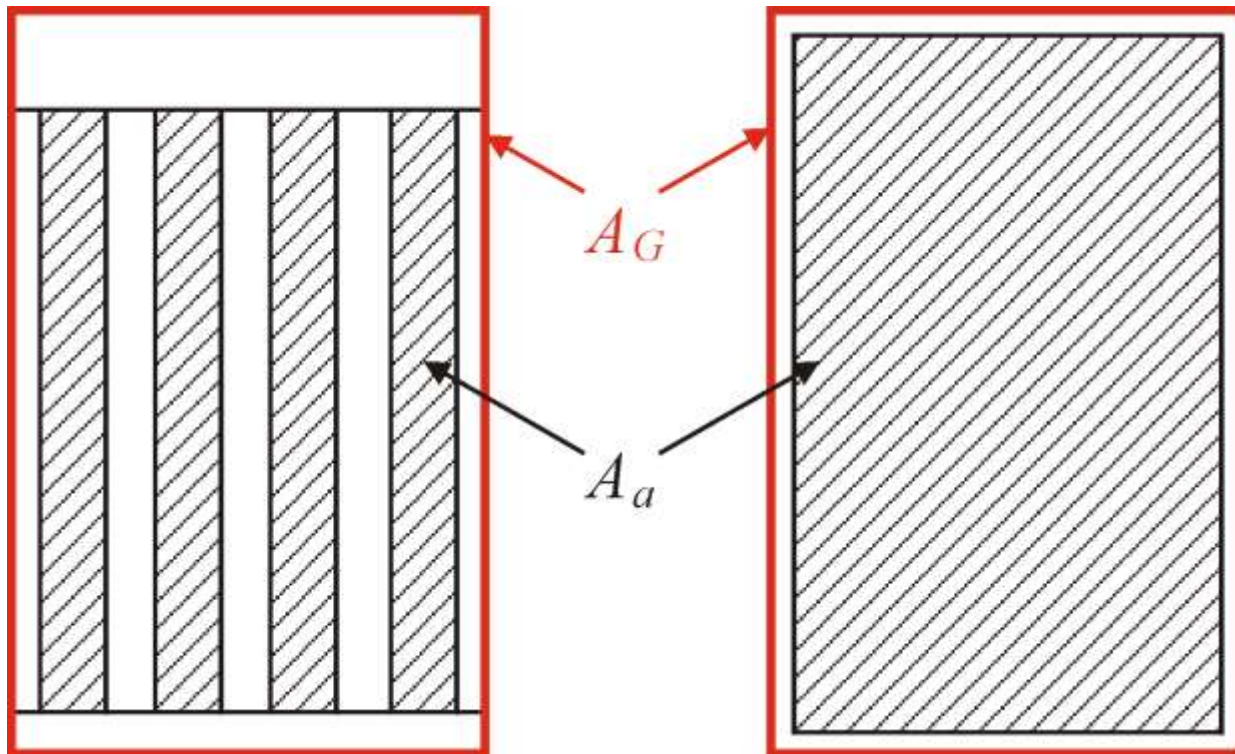
Reference area - comparison

Collector testing standards relates collector efficiency to:

- aperture area A_a EN 12975-2
 - absorber area A_A
 - gross area A_G **EN ISO 9806**
-
- aperture area: for comparison of collector properties or **design**
 - gross area: for decision on roof production **potential**
for comparison of collector with different **active** areas

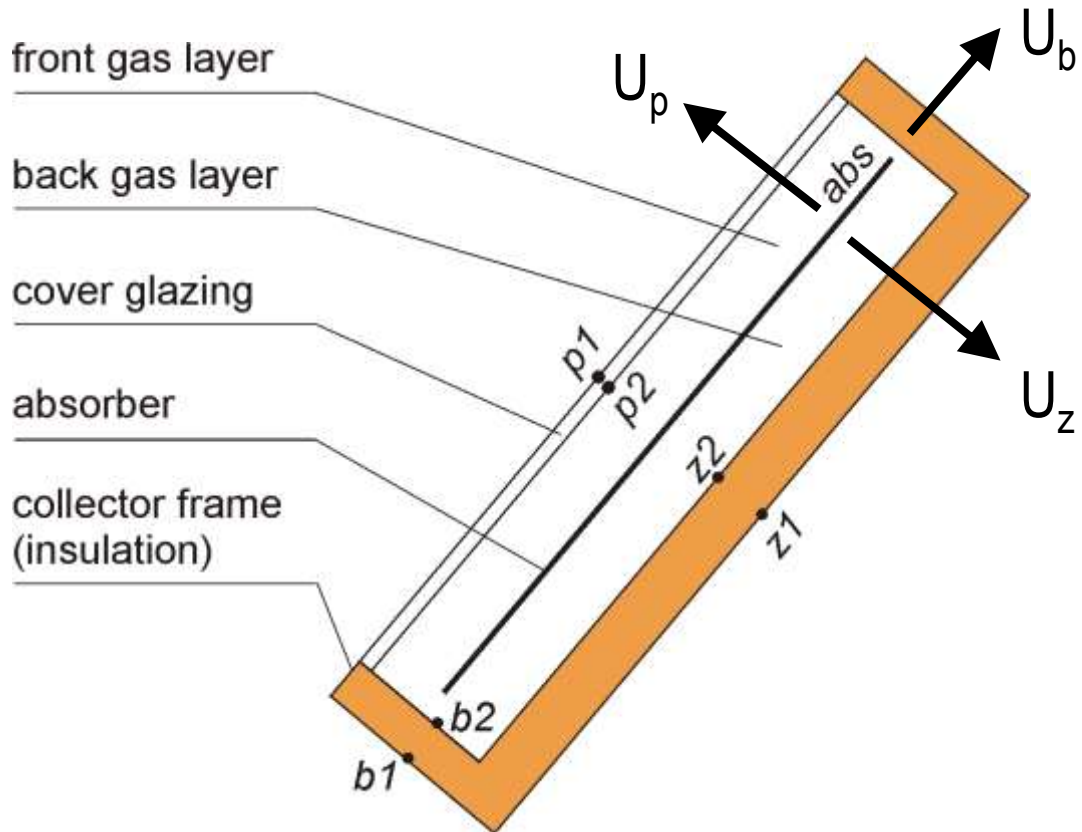


Reference area - comparison





External energy balance: detailed



U_p = front U -value

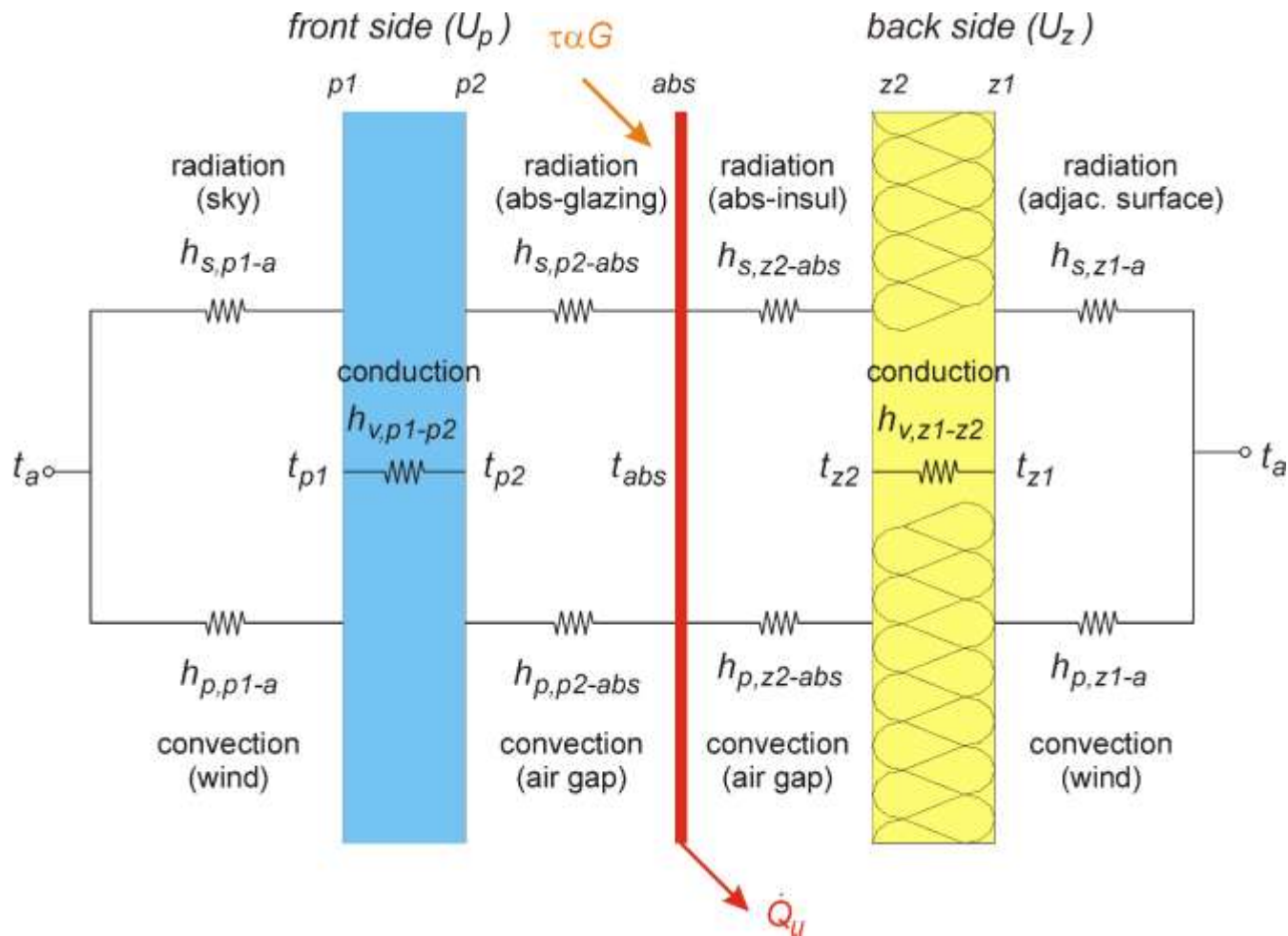
U_z = back U -value

U_b = side U -value

$$\dot{Q}_u = GA_a(\tau\alpha)_{ef} - U_p A_G(t_{abs} - t_a) - U_z A_G(t_{abs} - t_a) - U_b A_b(t_{abs} - t_a)$$



Scheme of external balance



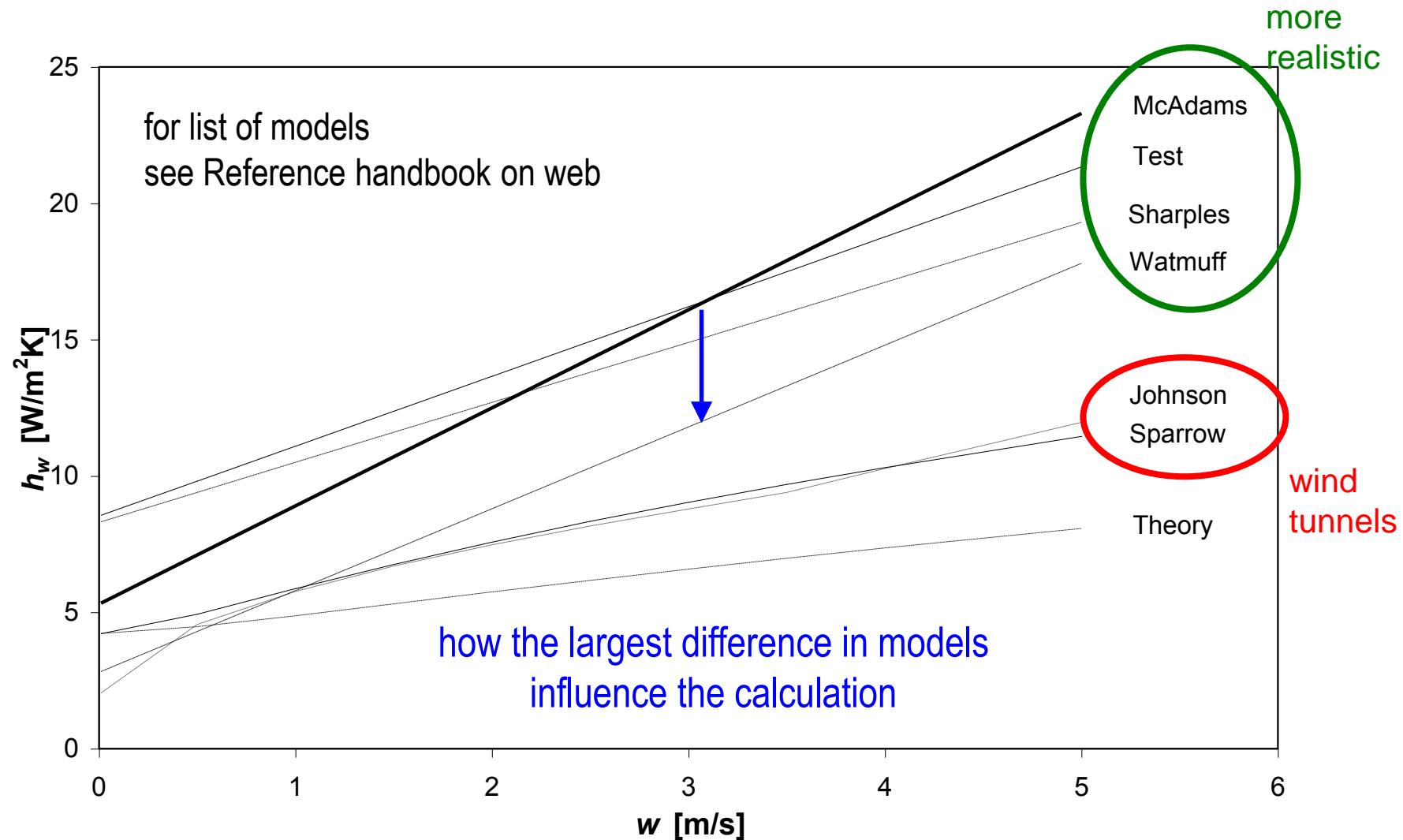


Wind convection

- Wind induced convection heat transfer from cover to ambient:
 - mix of natural and forced convection
 - turbulent environment
 - very dependent on location, terrain morphology, barriers, etc.
- Number of models existing for number of boundary conditions
 - wind tunnel measurements (low turbulence)
 - outdoor experiments (on roof, on ground, urban, countryside)
- Most of wind convection models
 - empirical linear function
$$h_w = a + bw$$



Wind convection





Wind convection for $w = 3 \text{ m/s}$

- how can the model influence calculated output temperature?
- run KOLEKTOR programme
- open **default.kol**
- Design parameters wind velocity $w = 3 \text{ m/s}$
- Calculation card select **Calculation for given t_{in}**
 select McAdams ... Calculate
 select Watmuff ... Calculate

McAdam's correlation

$$h_w = 16.1 \text{ W/m}^2\text{K}$$

$$t_{\text{out}} = 55.6 \text{ }^\circ\text{C}$$

Watmuff correlation

$$h_w = 11.3 \text{ W/m}^2\text{K}$$

$$t_{\text{out}} = 55.7 \text{ }^\circ\text{C}$$

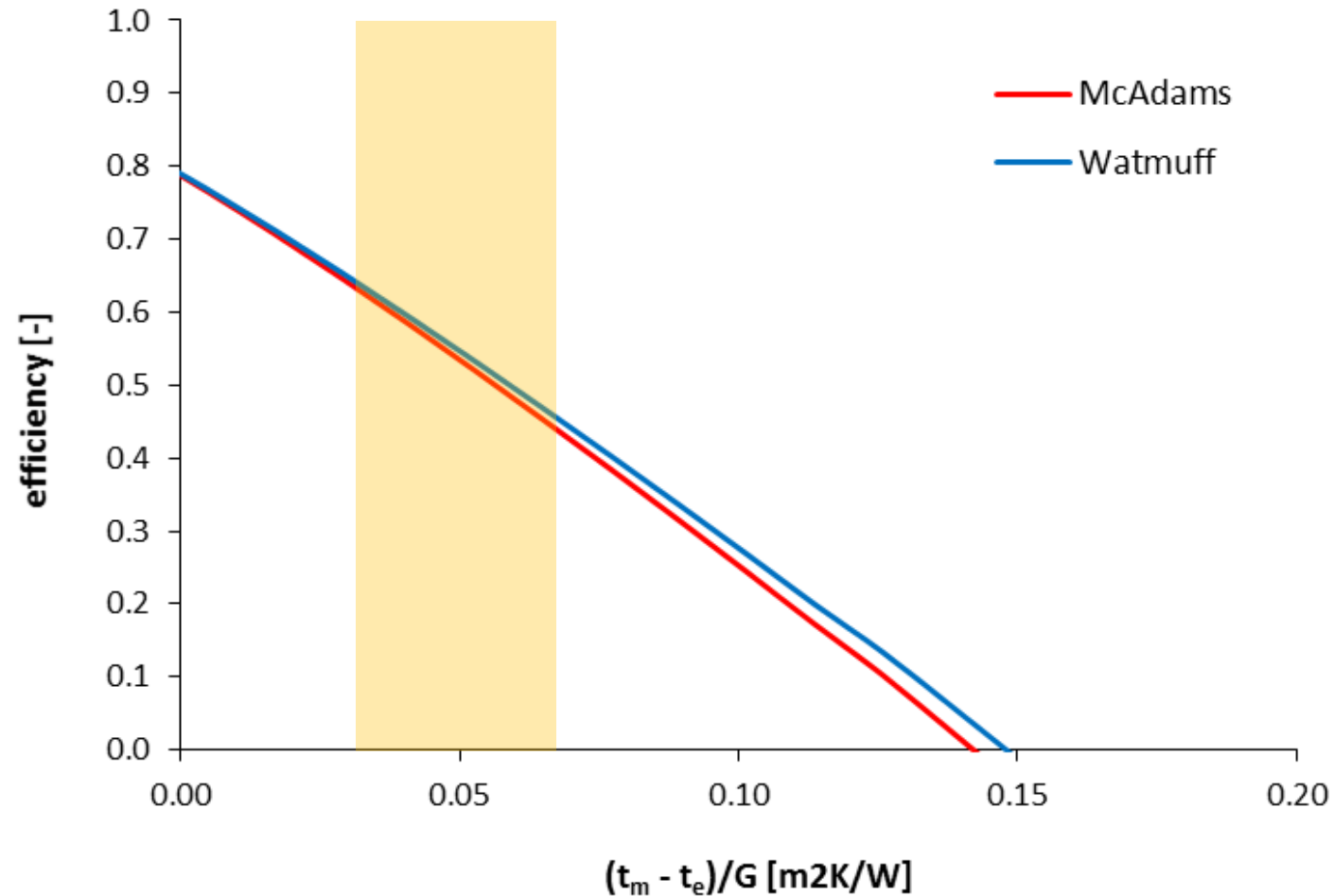


Wind convection for $w = 3 \text{ m/s}$

- **how can the model selection influence the efficiency curve?**
- Calculation card select Efficiency curve calculation
- select McAdams Calculate, Results export to file
- select Watmuff Calculate, Results export to file
- open Evaluation.xls
- make copies of the sheets
- open res files in excel, mind the semicolons as separators
- **compare the efficiency curves based on $(t_m - t_e)/G$**



Wind convection for $w = 3$ m/s



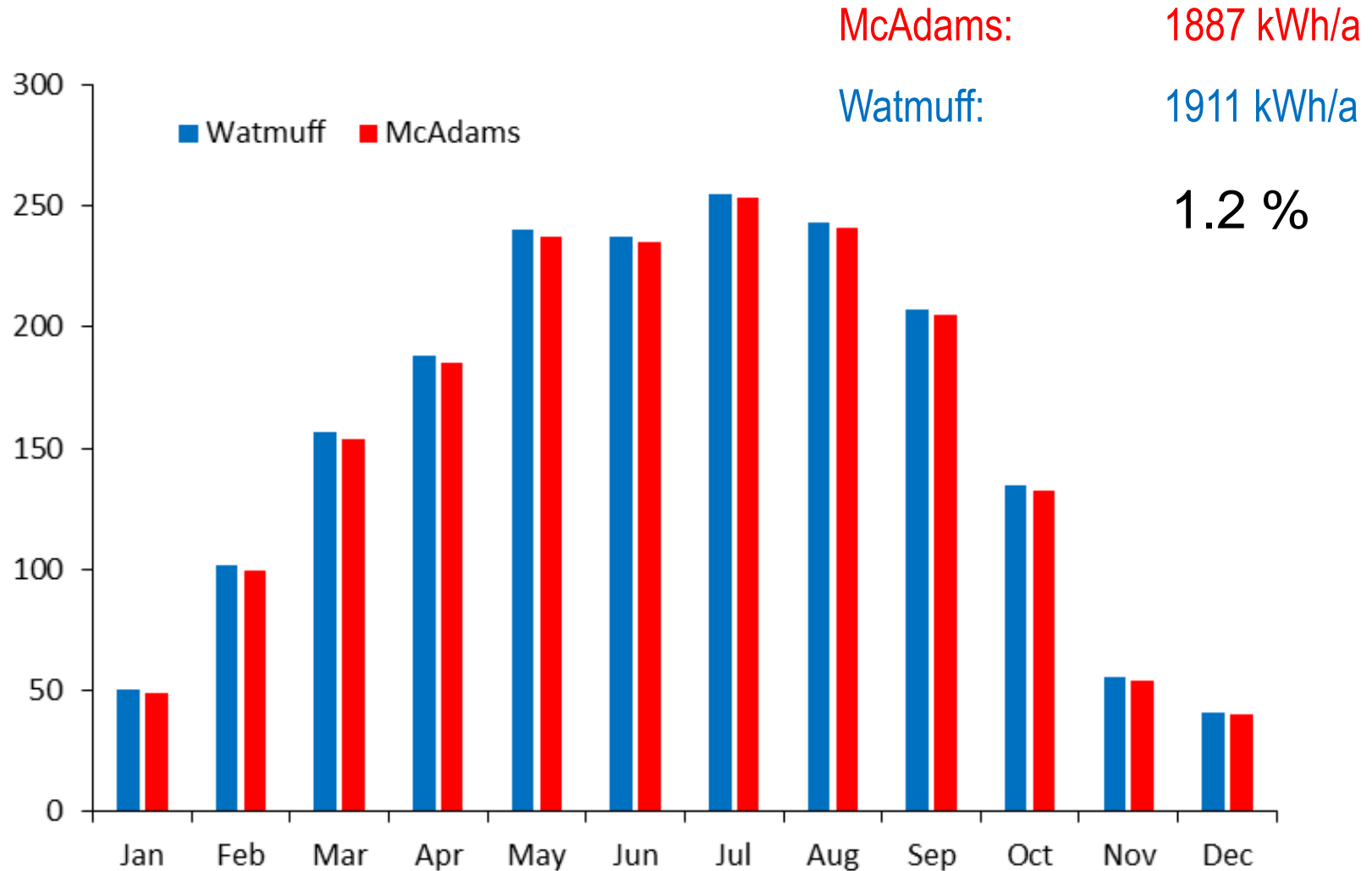


Wind convection for $w = 3$ m/s

- how can the model selection influence the annual energy yields?
 - McAdams $\eta_0 = 0.789$ $a_1 = 4.857$ $a_2 = 0.006$
 - Watmuff $\eta_0 = 0.791$ $a_1 = 4.664$ $a_2 = 0.006$
- open studio SDHW-SOLNET in TRNSYS
- make a change of coefficients in KOLEKTOR type
- results of collector yield find under Totals.txt
- compare the annual sums for both alternatives



Wind convection for $w = 3$ m/s



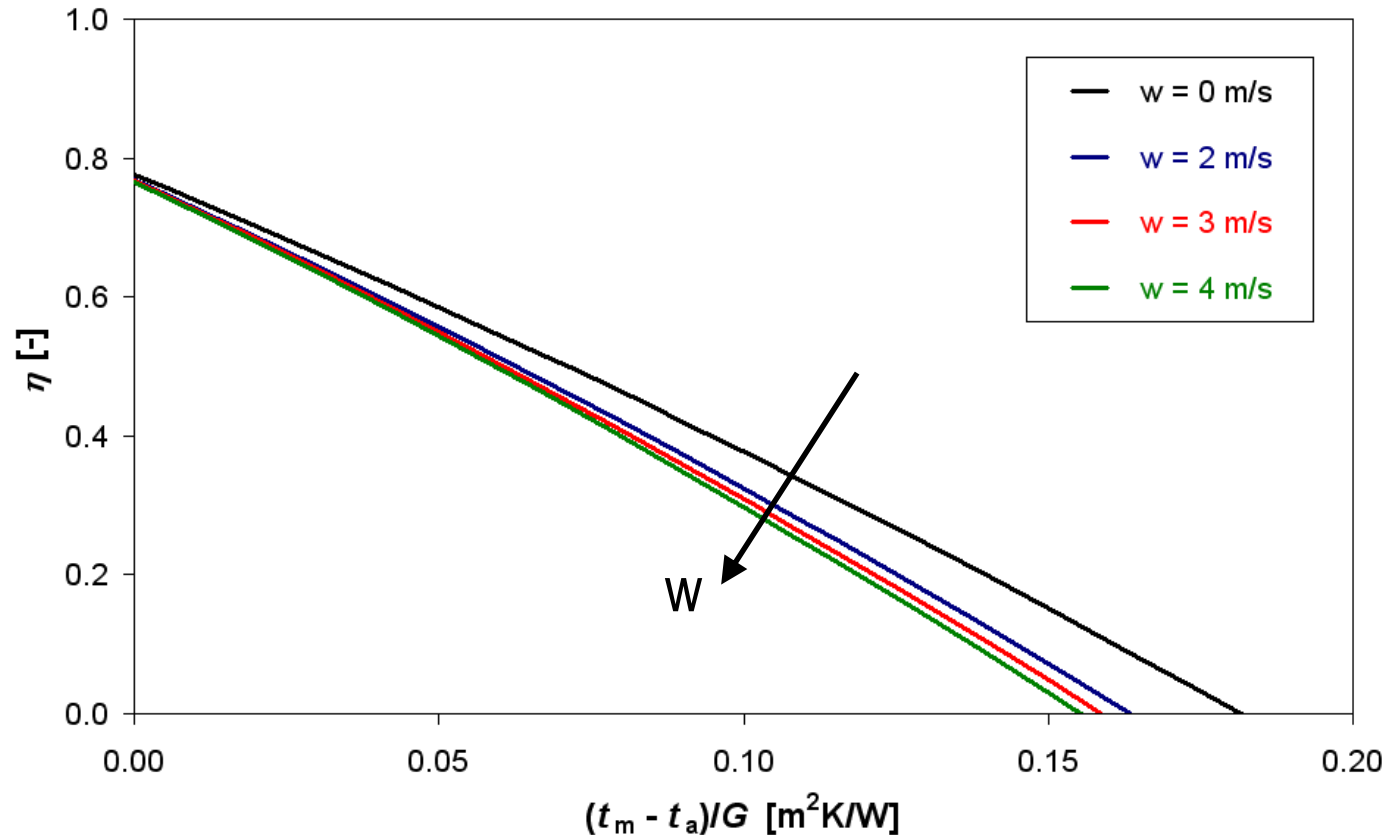


Wind convection for $w = 3 \text{ m/s}$

- **selection of the wind convection models**
- **minor influence** even if two models with largest difference selected
 - valid for usual quality flat-plate collectors (as our reference is)
- **negligible difference** for **high quality** flat-plate collectors
- **very critical** for unglazed collectors modelling
- less critical for PV modules modelling
 - reduced influence on electric yields via temperature coefficients



High wind velocity as test condition



testing standard: air velocity during the testing procedure $w > 3$ m/s
use of artificial wind needed!



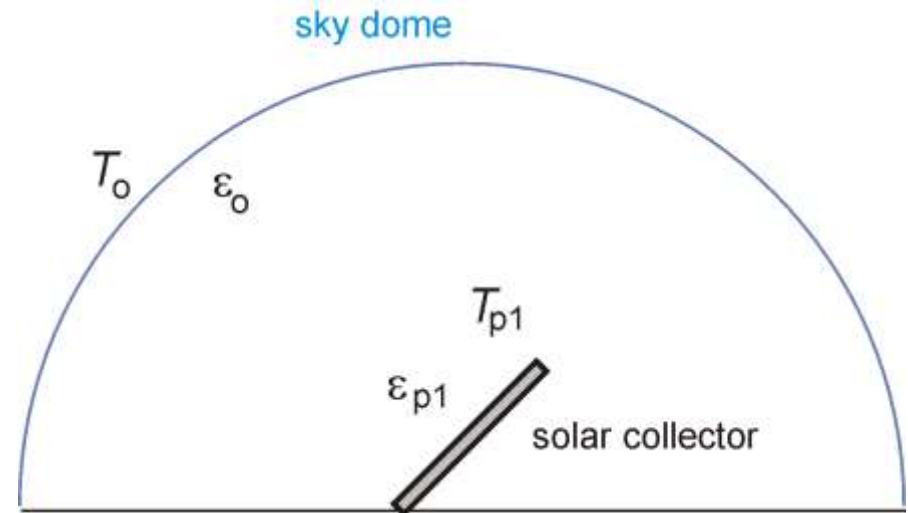
Sky radiation

Radiation heat exchange

$$q_{p1-o} = \varepsilon_{p1} \sigma (T_{p1}^4 - T_o^4) \quad [\text{W/m}^2]$$

Sky temperature, sky emittance

$$T_o^4 = \varepsilon_o T_a^4 \quad [\text{K}]$$



Sky radiation heat transfer coefficient related to ambient temperature

$$h_{s,p1-a} = \varepsilon_{p1} \sigma \frac{T_{p1}^4 - T_o^4}{T_{p1} - T_a} \quad [\text{W/m}^2\text{K}]$$



Sky temperature models

Number of models for sky temperature T_o calculation based on:

- | | cloudy sky | clear sky |
|----------------------------------|-------------|--|
| ■ ambient temperature T_a | $T_o = T_a$ | $T_o = 0.0552 (T_a)^{1.5}$
(Swinbank, 1963) |
| ■ dew point temperature T_{dp} | | |
| ■ water vapour pressure p_d | | |
| ■ sky clearness index K_o | | |
- for more see
Reference handbook on web
- clear sky conditions
 - cloudy sky conditions



Sky temperature models

Sky temperature calculation based on:

$$T_o = T_a$$

$$e_{p1} = 0.85, t_{p1} = 40 \text{ }^{\circ}\text{C}, t_a = 20 \text{ }^{\circ}\text{C}$$

$$h_{s,p1-a} = 5.38 \text{ W/m}^2\text{K}$$

$$e_{p1} = 0.10, t_{p1} = 40 \text{ }^{\circ}\text{C}, t_a = 20 \text{ }^{\circ}\text{C}$$

$$h_{s,p1-a} = 0.63 \text{ W/m}^2\text{K}$$

$$T_o = 0.0552 (T_a)^{1.5}$$

$$t_o = 3.9 \text{ }^{\circ}\text{C}$$

$$h_{s,p1-a} = 8.97 \text{ W/m}^2\text{K}$$

$$h_{s,p1-a} = 1.06 \text{ W/m}^2\text{K}$$

considerable decrease of heat transfer coefficient if low-e coating
does it mean also improvement of collector performance?



Coupling sky radiation + wind convection

heat transfer from glazing exterior surface: **proportions**

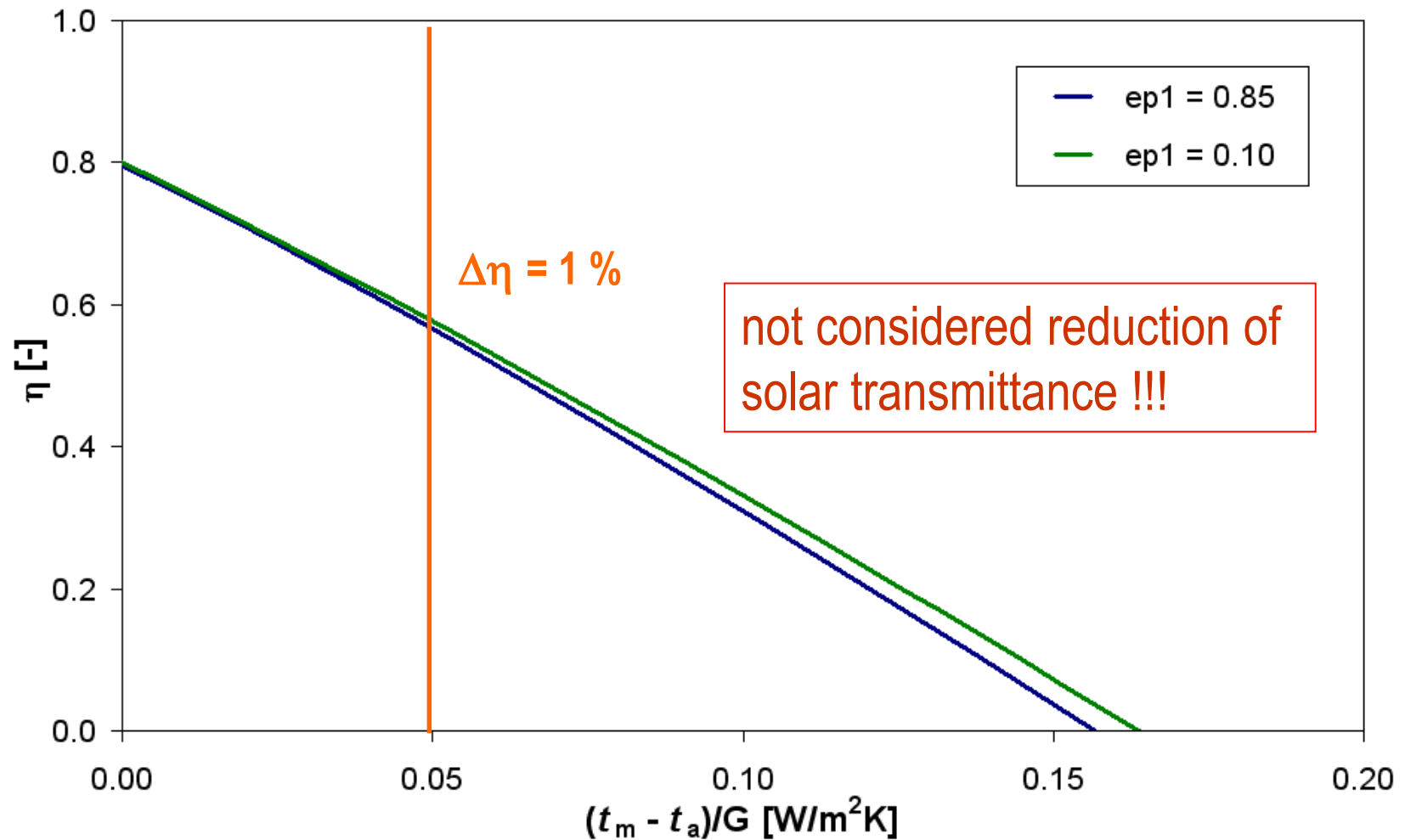
$$q = q_s \text{ (sky radiation)} + q_p \text{ (wind convection)}$$

w [m/s]	h_s [W/m ² K]	h_p [W/m ² K]	$h_s + h_p$ [W/m ² K]
0	5.1 / 0.6	5.3	10.4 / 5.9
2	5.0 / 0.6	12.5	17.5 / 13.1
4	5.0 / 0.6	19.7	24.7 / 20.3
6	5.0 / 0.6	26.2	31.2 / 26.8

convection heat transfer is dominant (if wind is present ...)

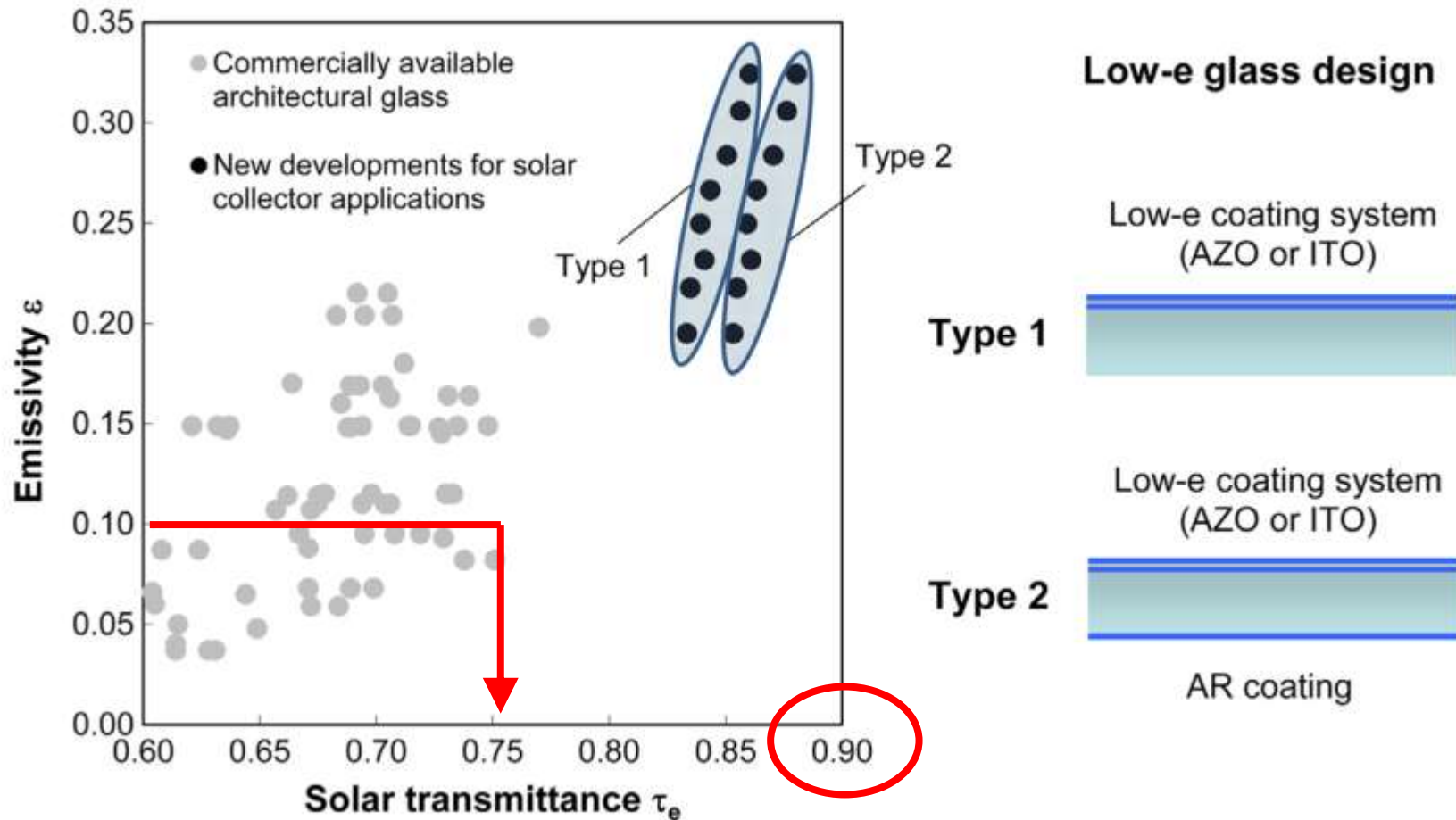


Influence of sky radiation reduction





Influence of sky radiation reduction





Conduction through cover glazing

heat conductance

$$h_{gl} = h_{v,p1-p2} = \frac{\lambda_{gl}}{L_{gl}} \quad [\text{W/m}^2\text{K}]$$

single glazing: glass: $\lambda_{gl} = 0.8 \text{ W/mK}$, $L_{gl} = 4 \text{ mm}$

$$h_{gl} = 200 \text{ W/m}^2\text{K}$$

PC: $\lambda_{gl} = 0.2 \text{ W/mK}$, $L_{gl} = 4 \text{ mm}$

$$h_{gl} = 50 \text{ W/m}^2\text{K}$$

practically negligible

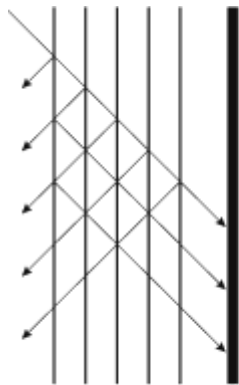


Conduction through cover glazing

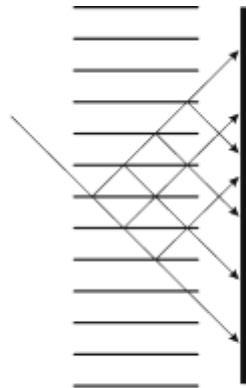
■ transparent insulation structures

- channel structures: $h_{gl} = 2 \text{ to } 8 \text{ W/m}^2\text{K}$
- honeycombs: $h_{gl} = 1 \text{ to } 2 \text{ W/m}^2\text{K}$
- aerogels: $h_{gl} = \text{less than } 1 \text{ W/m}^2\text{K}$

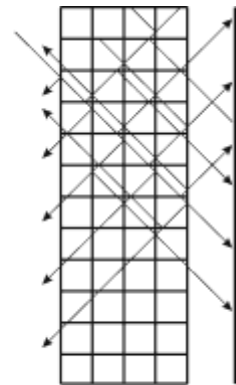
**function of mean
temperature**



a



b



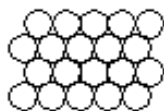
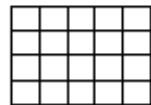
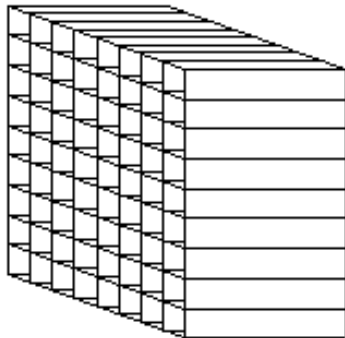
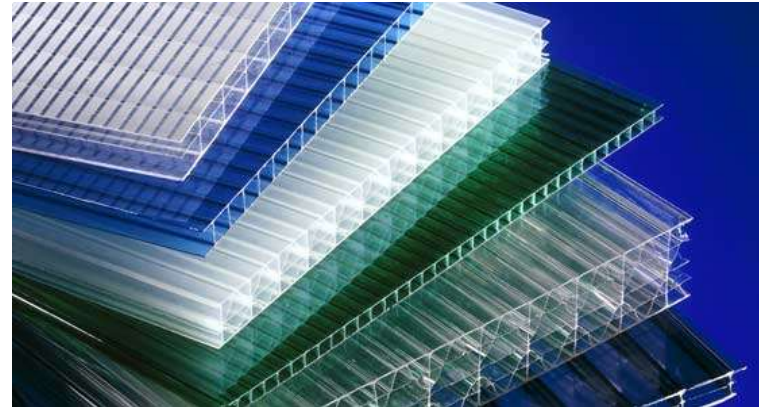
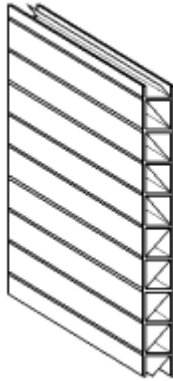
c



d



Conduction through cover glazing

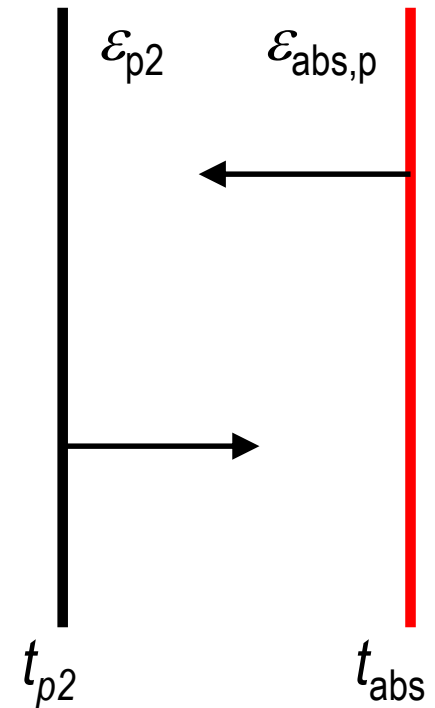




Radiation between absorber and cover

Radiation heat exchange

$$q_{s,abs-p2} = \sigma \frac{T_{abs}^4 - T_{p2}^4}{\frac{1}{\varepsilon_{p2}} + \frac{1}{\varepsilon_{abs,p}} - 1} \quad [W/m^2]$$

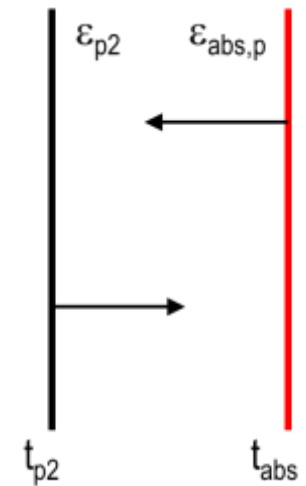




Radiation between absorber and cover

influence of absorber emissivity

t_{abs}	40 °C		
t_{p2}	20 °C		
$\varepsilon_{\text{abs,p}}$	0.85	0.10	0.05
ε_{p2}	0.85	0.85	0.85
$h_{\text{s,p1-a}}$	4.7 W/m ² K	0.6 W/m ² K	0.3 W/m ² K





Spectrally selective absorber

- how can the absorber emissivity influence the thermal performance of the solar collector?
- influence on efficiency curve
- influence on the yields
- are low-emittance coating for absorbers needed?
- compare $\epsilon_{\text{abs}} = 0.85$ $\epsilon_{\text{abs}} = 0.10$ $\epsilon_{\text{abs}} = 0.05$



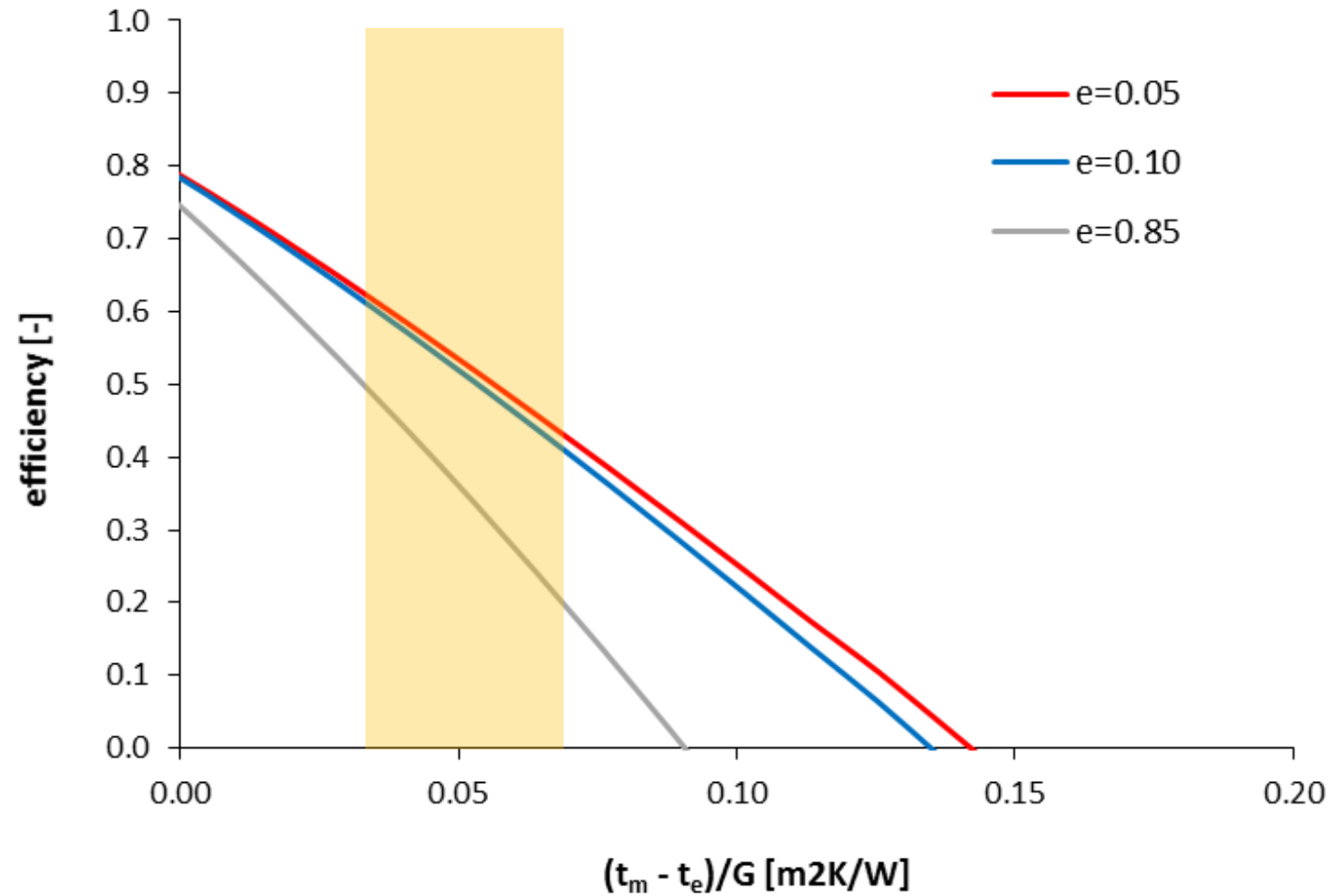
Spectrally selective absorber

- run KOLEKTOR programme, open **default.kol**
- Absorber card change **Front surface emissivity**
- Calculation card select Efficiency curve calculation
Calculate, Export results

- open Evaluation.xls
- make copies of the sheets for three alternatives
- open res files in excel, mind the semicolons as separators
- **compare the efficiency curves based on $(t_m - t_e)/G$**



Spectrally selective absorber





Spectrally selective absorber

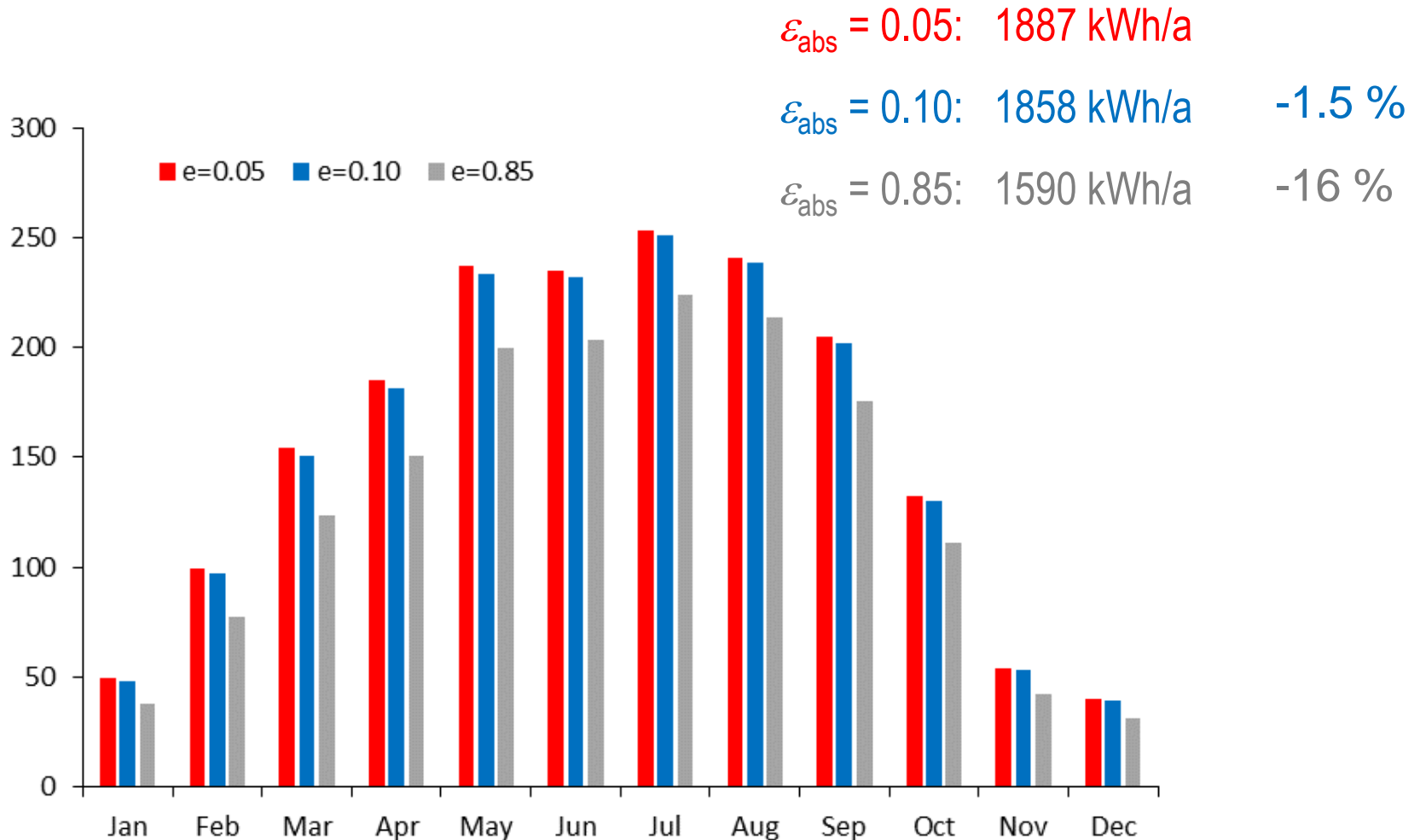
- how can the absorber emissivity influence the annual energy yields of collector?

■ $\varepsilon_{\text{abs}} = 0.05$	$\eta_0 = 0.789$	$a_1 = 4.857$	$a_2 = 0.006$
■ $\varepsilon_{\text{abs}} = 0.10$	$\eta_0 = 0.785$	$a_1 = 5.006$	$a_2 = 0.008$
■ $\varepsilon_{\text{abs}} = 0.85$	$\eta_0 = 0.744$	$a_1 = 6.773$	$a_2 = 0.020$

- open studio SDHW-SOLNET in TRNSYS
- make a change of coefficients in KOLEKTOR type
- results of collector yield find under Totals.txt
- **compare the annual sums for both alternatives**



Spectrally selective absorber





Spectrally selective absorber

- new **cermet coatings** with extremely low-emittance **are about 1.5 % better** than old-fashioned **galvanic** coatings
- there could be no fear about nonuniformity of coating emittance at the whole absorber area
 - it does not matter for annual effectivity
 - facts above valid for **domestic hot water systems**
- **significant difference** for high emittance coatings
- **very critical** for high temperature operation – much higher impact on the annual yields



Natural convection in the air gap

coupled convection and conduction heat transfer in closed gas layer

$$h_{p+v} = Nu_L \frac{\lambda_g}{L} \quad [W/m^2K]$$

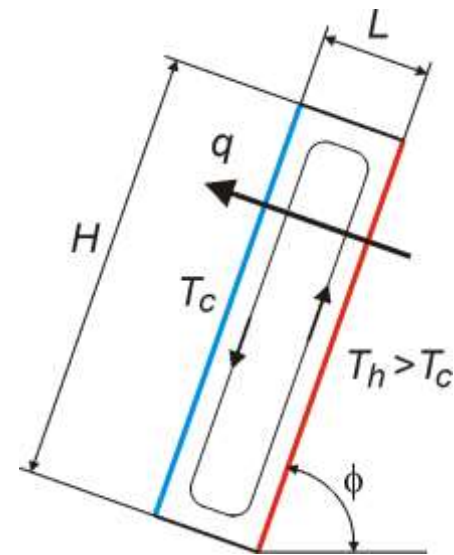
Characteristic dimension:
thickness of gas layer L

Nusselt number:

characterization of conduction heat transfer $\rightarrow \lambda_g/L$

enhancement by fluid convection (driven by buoyancy) $\rightarrow Nu_L$

definition: ratio of the total heat transfer to conductive heat transfer





Convection in the air gap - criteria

Nusselt number: $Nu_L = f(Gr_L, Pr)$

Grashof number: $Gr_L = \beta \frac{g L^3 \Delta t}{\nu^2} = \frac{2}{(T_h + T_c)} \cdot \frac{g L^3 (t_h - t_c)}{\nu^2}$

ratio of the buoyancy to viscous force acting on a fluid

Prandtl number: $Pr = \frac{\nu}{a} = \frac{\nu \rho c}{\lambda}$

express conformity of velocity and temperature fields,
ratio of momentum diffusivity (kinematic viscosity) to thermal diffusivity



Convection in the air gap - criteria

Rayleigh number: $Ra = Gr \cdot Pr = \frac{\beta g L^3 (t_h - t_c)}{\nu \alpha}$

ratio of buoyancy forces to thermal and momentum diffusivities of fluid

for standard conditions

$$400 < Gr < 60\,000$$

$$0.72 < Pr < 0.73$$

$$300 < Ra < 44\,000$$



Structure of the convection models

Hollands:

$$Nu_L = 1 + 1.44 \left[1 - \frac{1708}{Ra_L \cos \phi} \right]^+ \left(1 - \frac{(\sin 1.8\phi)^{1.6} 1708}{Ra_L \cos \phi} \right) + \left[\left(\frac{Ra_L \cos \phi}{5830} \right)^{1/3} - 1 \right]^+$$

Buchberg:

$$Nu_L = 1 + 1.446 \left(1 - \frac{1708}{Ra_L \cos \phi} \right)^+$$

$$Nu_L = 0.157 (Ra_L \cos \phi)^{0.285}$$

Randall:

$$Nu_L = 0.118 [Ra_L \cos^2(\phi - 45)]^{0.29}$$

Niemann:

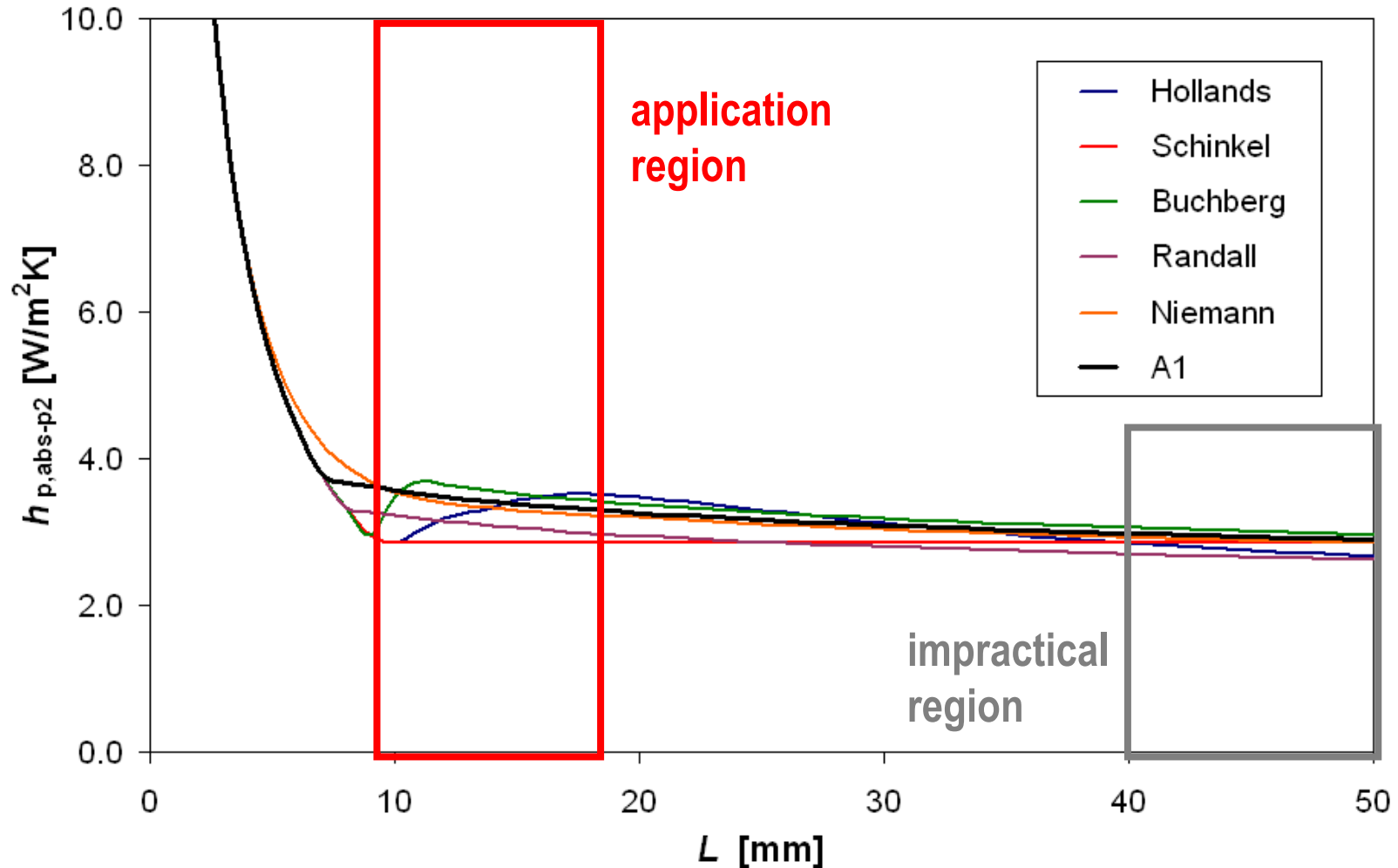
$$Nu_L = 1 + \frac{m(Ra_L)^K}{Ra_L + n}$$

for more see
Reference handbook on web



Convection in the air gap – optimum L

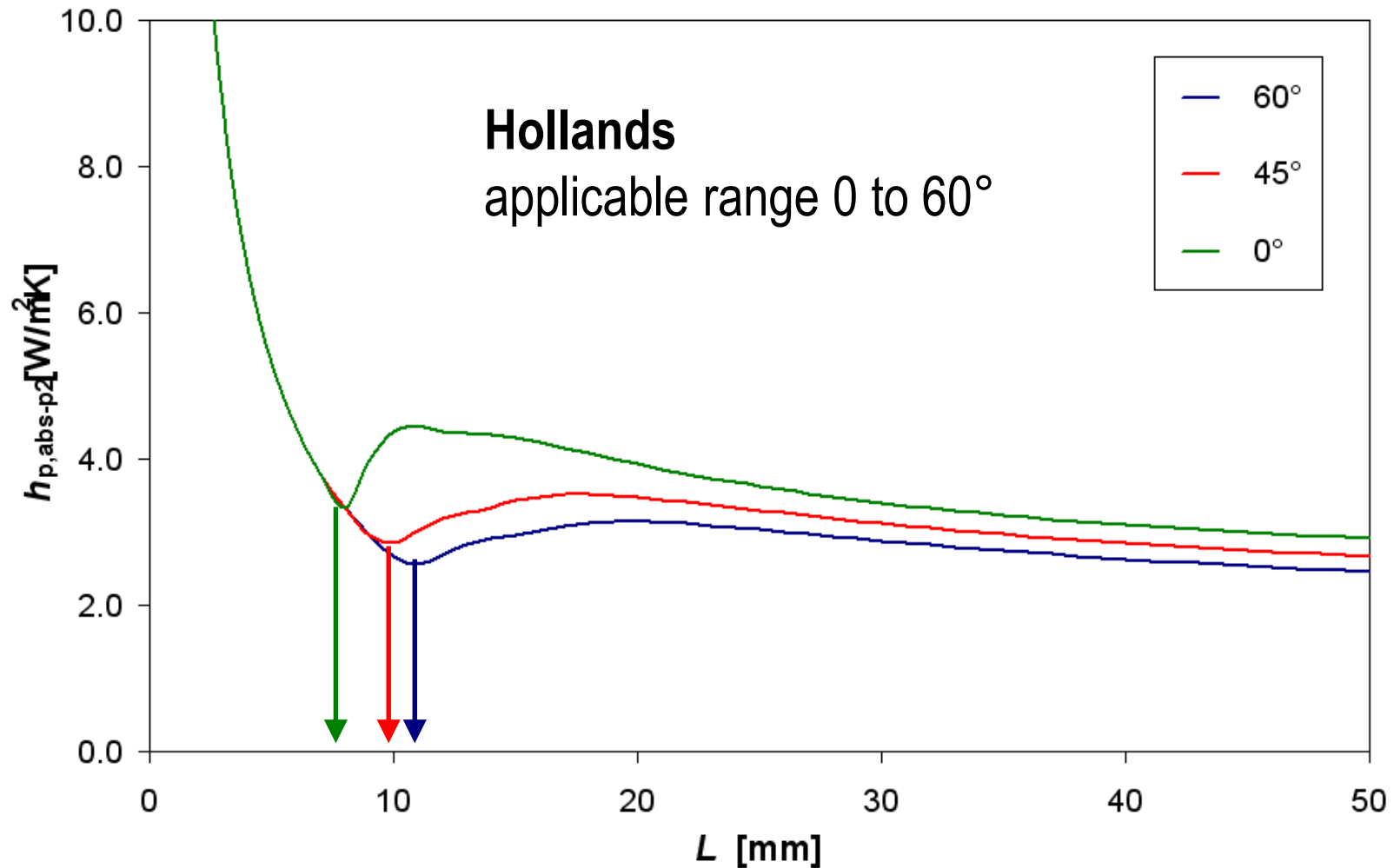
slope 45°, absorber 60 °C, glass 20 °C





Slope dependence

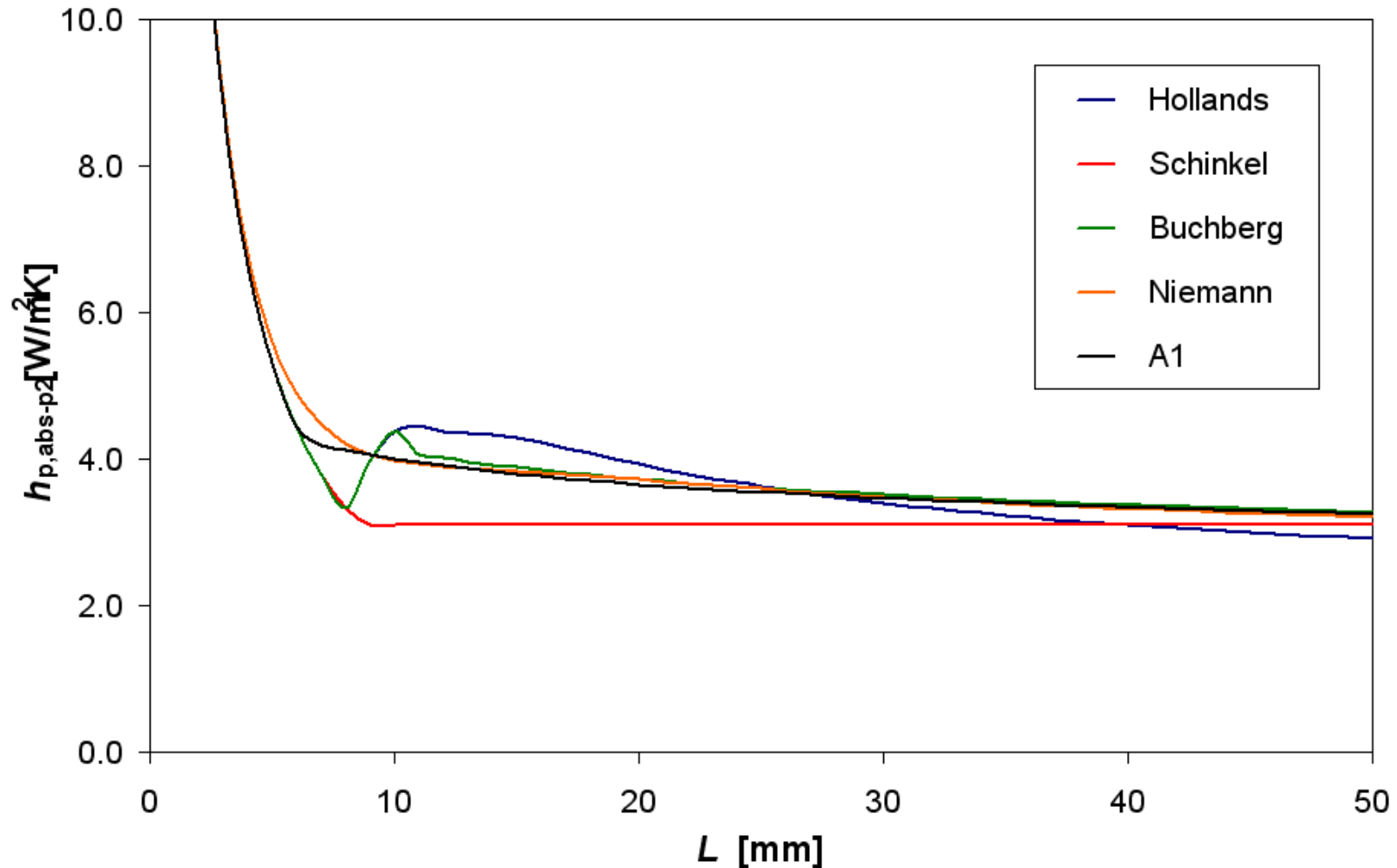
absorber 60 °C, glass 20 °C





Slope dependence 0°

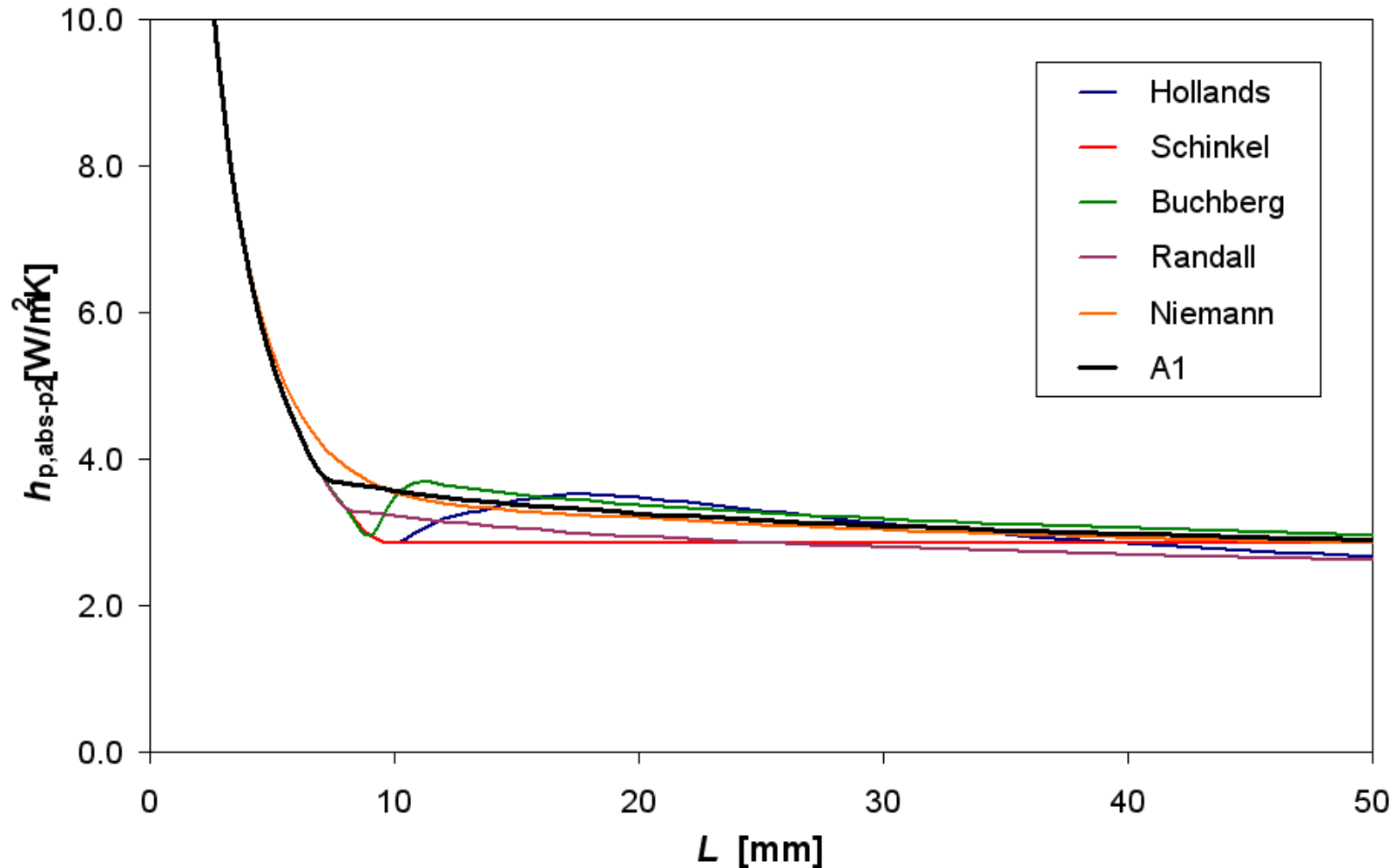
absorber 60 °C, glass 20 °C





Slope dependence 45°

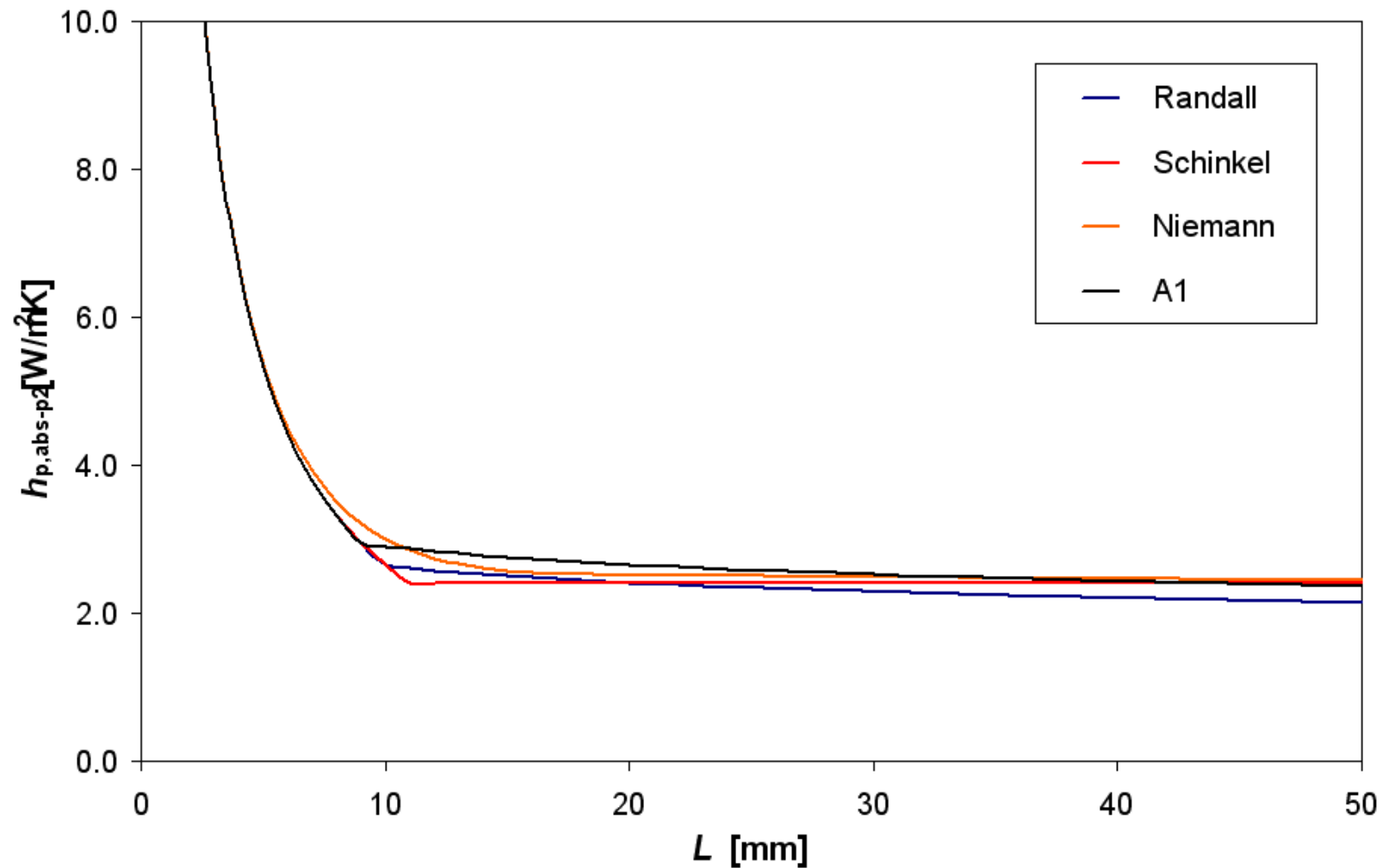
absorber 60 °C, glass 20 °C





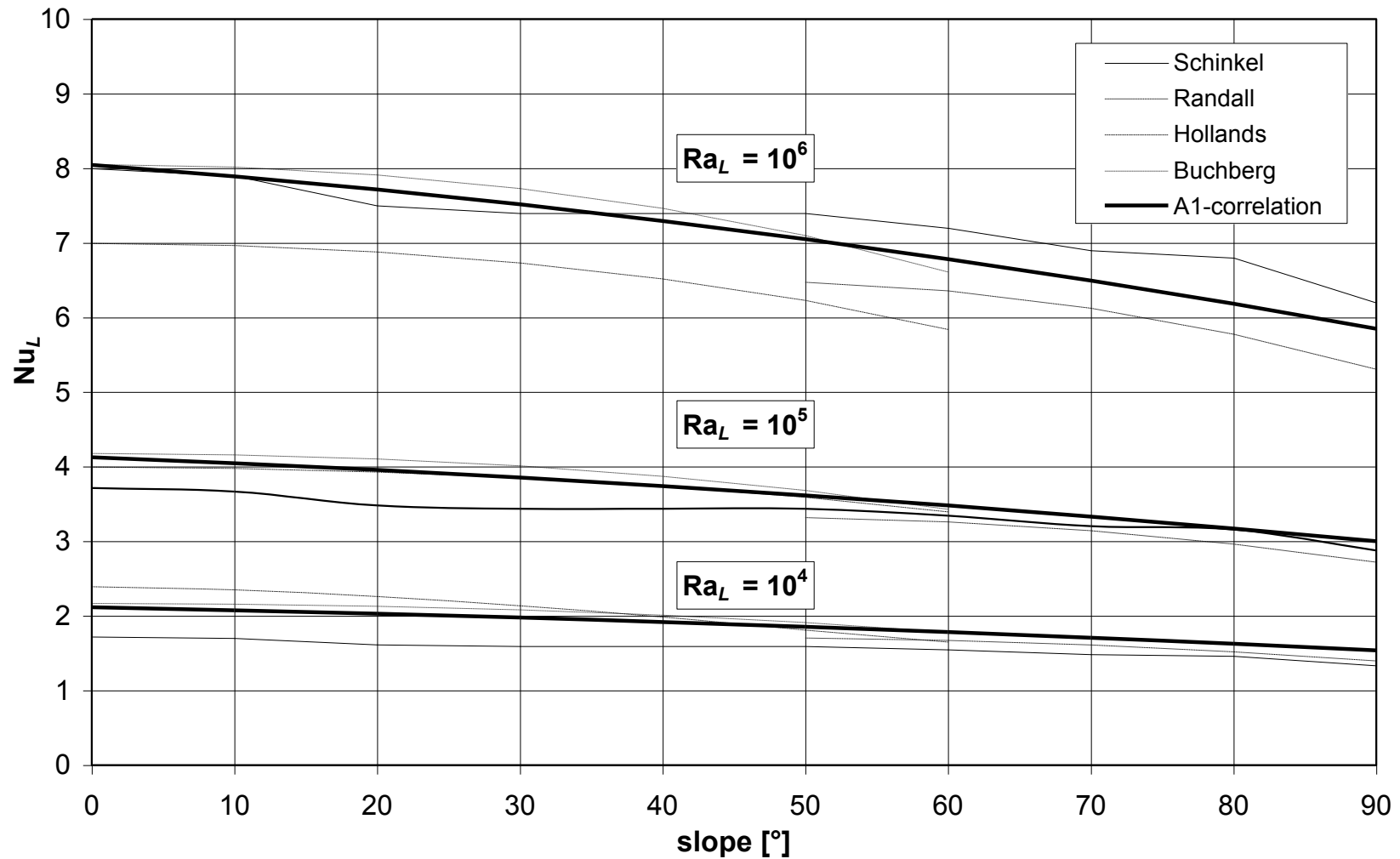
Slope dependence 90°

absorber 60 °C, glass 20 °C



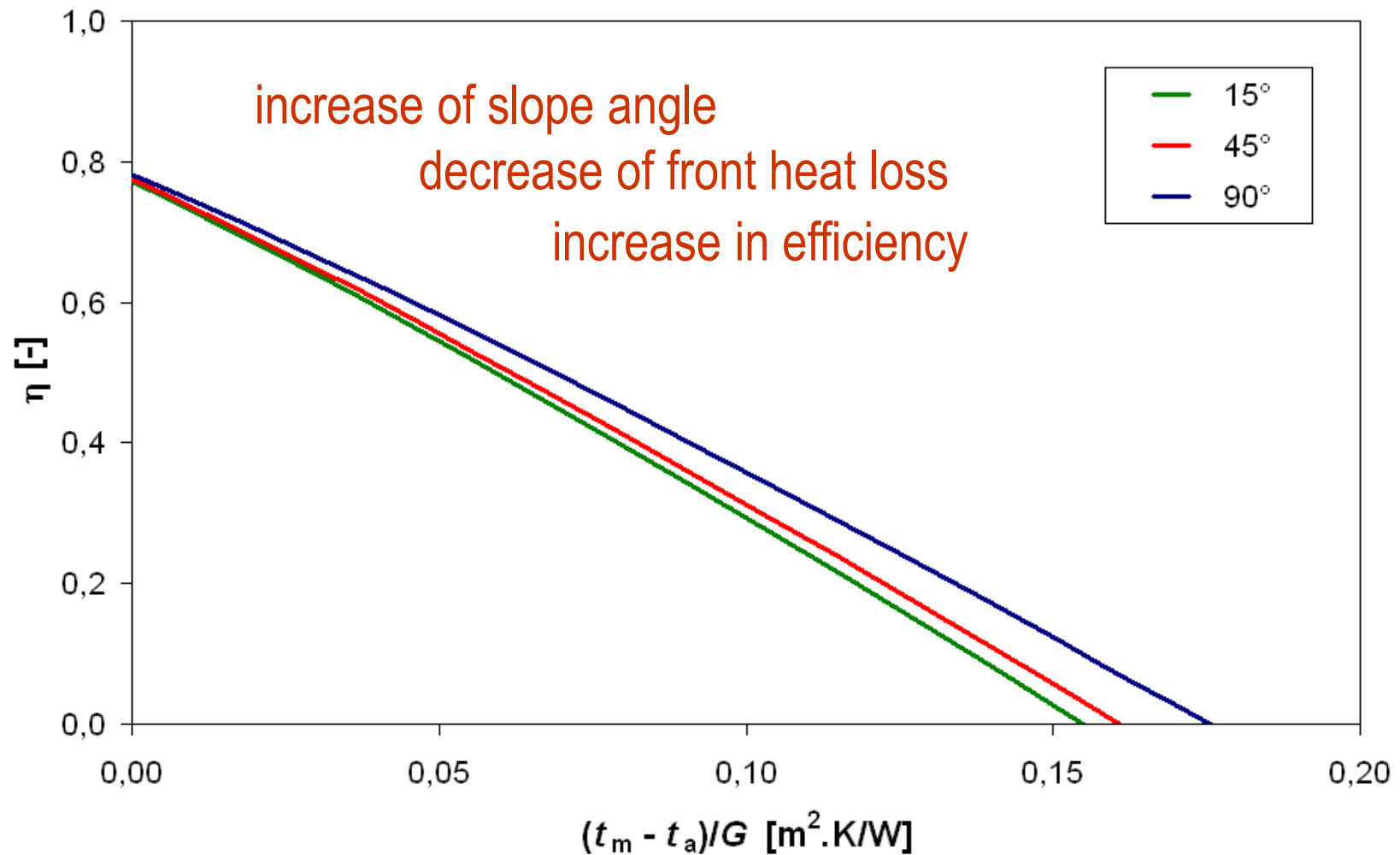


Convection in inclined air layer





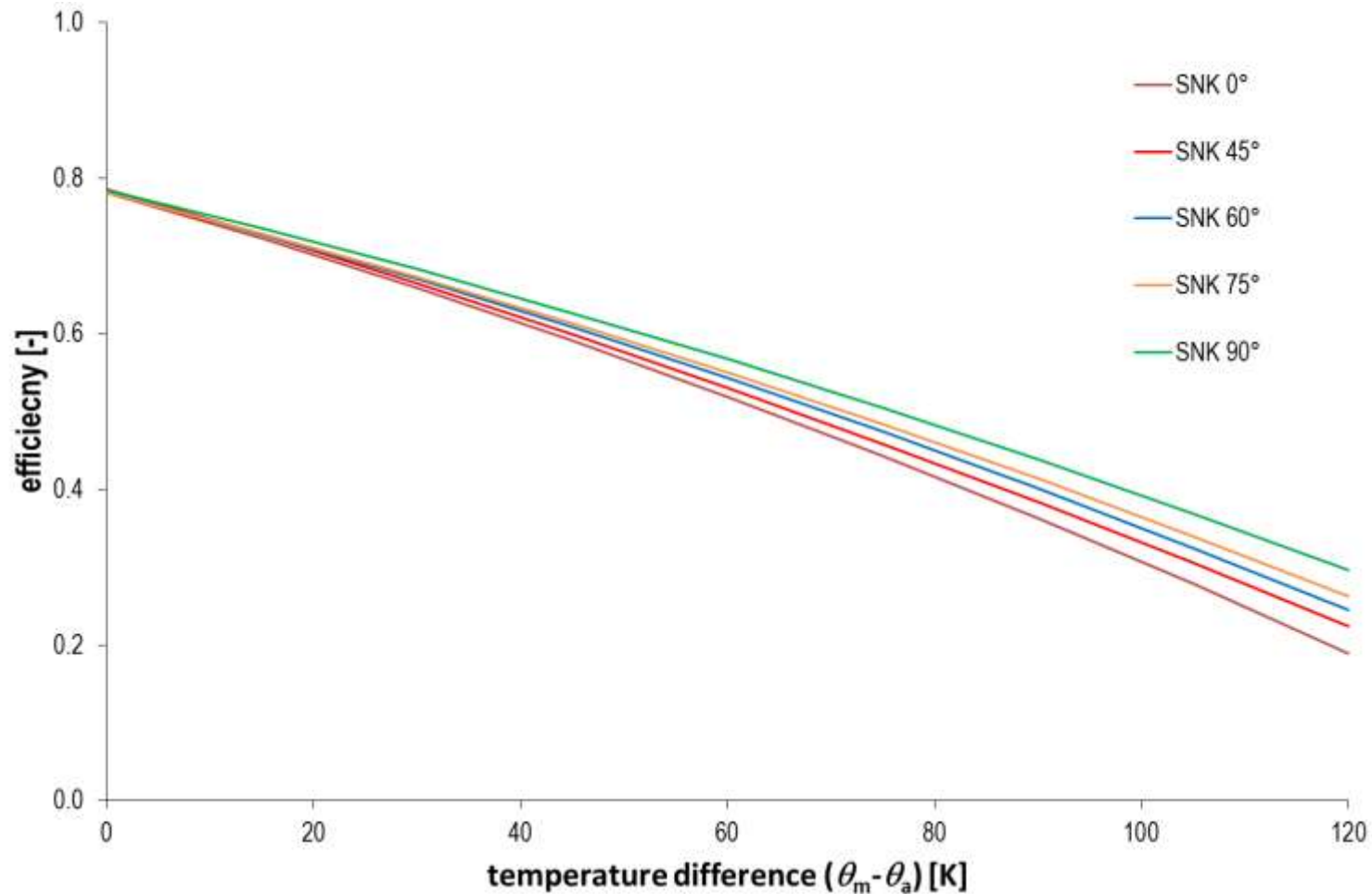
Slope impact on collector efficiency





Slope impact on collector efficiency

results from testing at cca 1000 W/m²



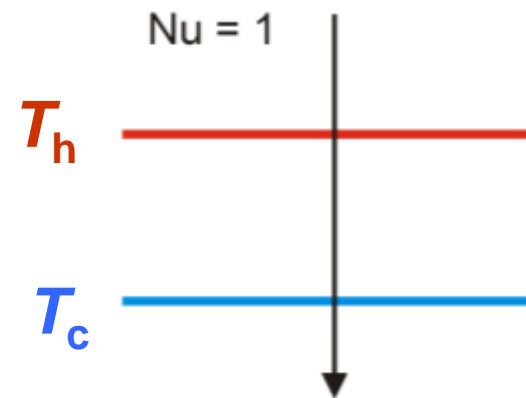
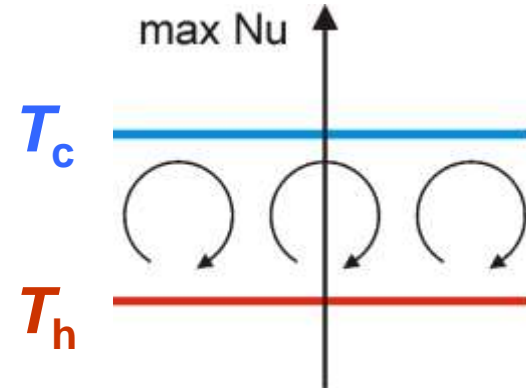
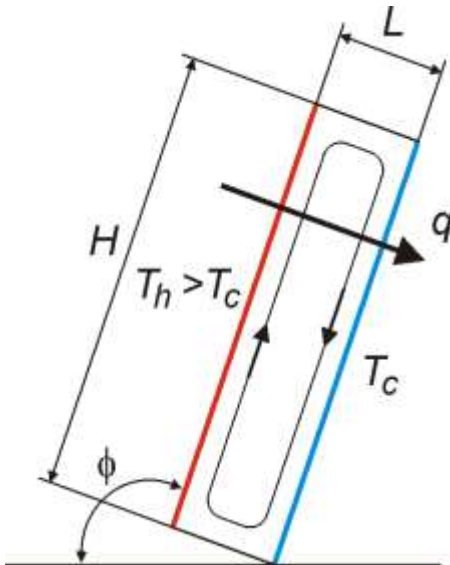


Convection in the back air gap

in the range $90 < \phi < 180^\circ$

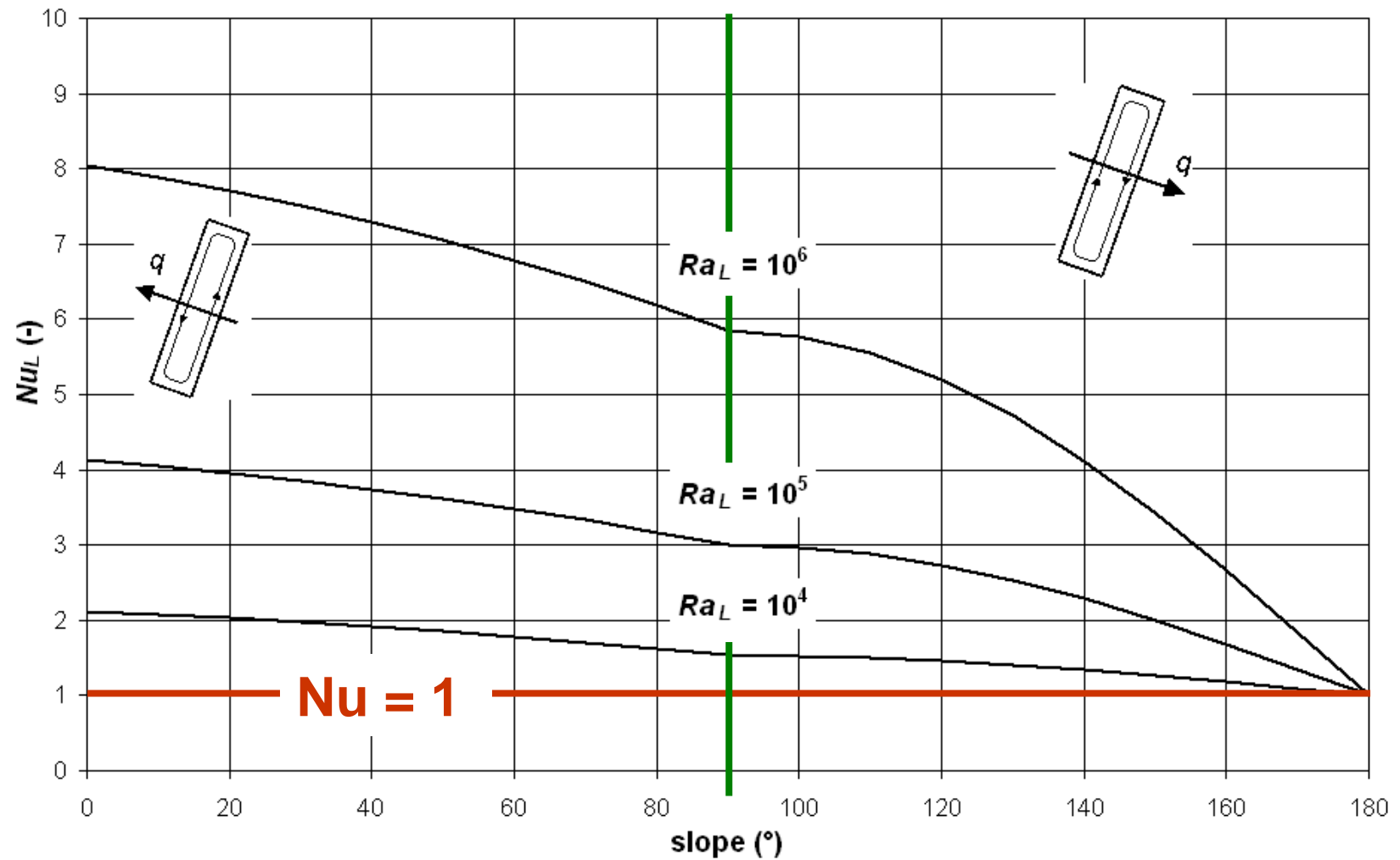
$$Nu_L = 1 + [Nu_L(\phi = 90^\circ) - 1] \sin \phi$$

Arnold (1975)





Convection vs. slope





Radiation between absorber and frame

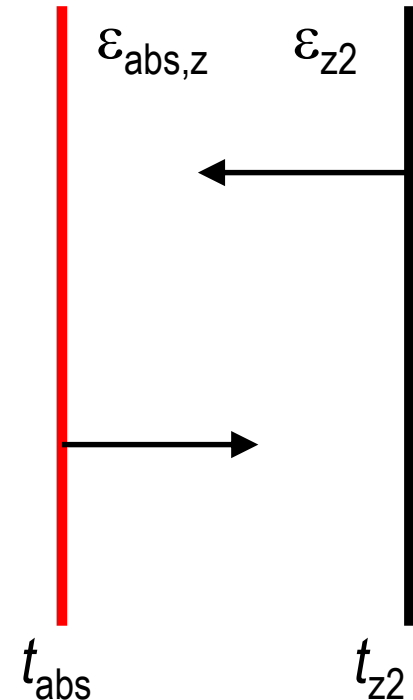
Radiation heat exchange

$$q_{s,abs-z2} = \sigma \frac{T_{abs}^4 - T_{z2}^4}{\frac{1}{\varepsilon_{z2}} + \frac{1}{\varepsilon_{abs,z}} - 1}$$

treatment of insulations:

aluminium foil

applied to mineral wool



$$\varepsilon_{z2} = 0.1$$

is it needed?



Radiation between absorber and frame

example: internal frame insulation surface emittance ε_{z2}

$t_{\text{abs}} = 60 \text{ }^{\circ}\text{C}$, $t_a = 20 \text{ }^{\circ}\text{C}$, back insulation 30 mm, air gap d_{z2}

case 1: $d_{z2} = 20 \text{ mm}$

$$\varepsilon_{z2} = 0.5 \quad U_z = 1.10 \text{ W/m}^2\text{K}$$

$$\varepsilon_{z2} = 0.1 \quad U_z = 0.96 \text{ W/m}^2\text{K}$$

15 %

case 2: $d_{z2} = 5 \text{ mm}$

$$\varepsilon_{z2} = 0.5 \quad U_z = 1.22 \text{ W/m}^2\text{K}$$

$$\varepsilon_{z2} = 0.1 \quad U_z = 1.17 \text{ W/m}^2\text{K}$$

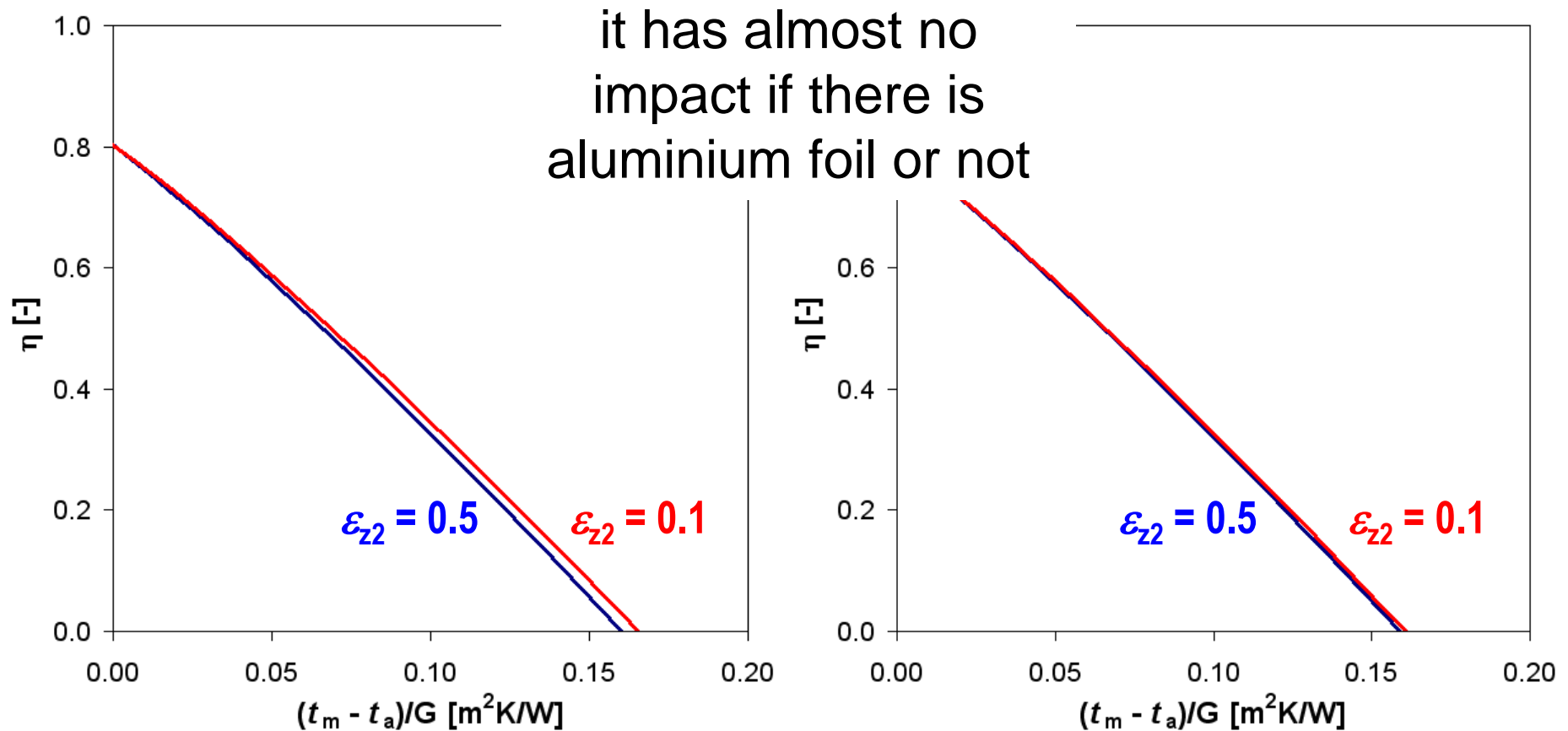
4 %



Radiation between absorber and frame

back air gap 20 mm

back air gap 5 mm





Heat conduction through frame insulation

heat conductance of insulation layer

$$h_{\text{ins}} = h_{\text{v},z1-z2} = \frac{\lambda_{\text{ins}}}{L_{\text{ins}}} \quad [\text{W}/\text{m}^2\text{K}]$$

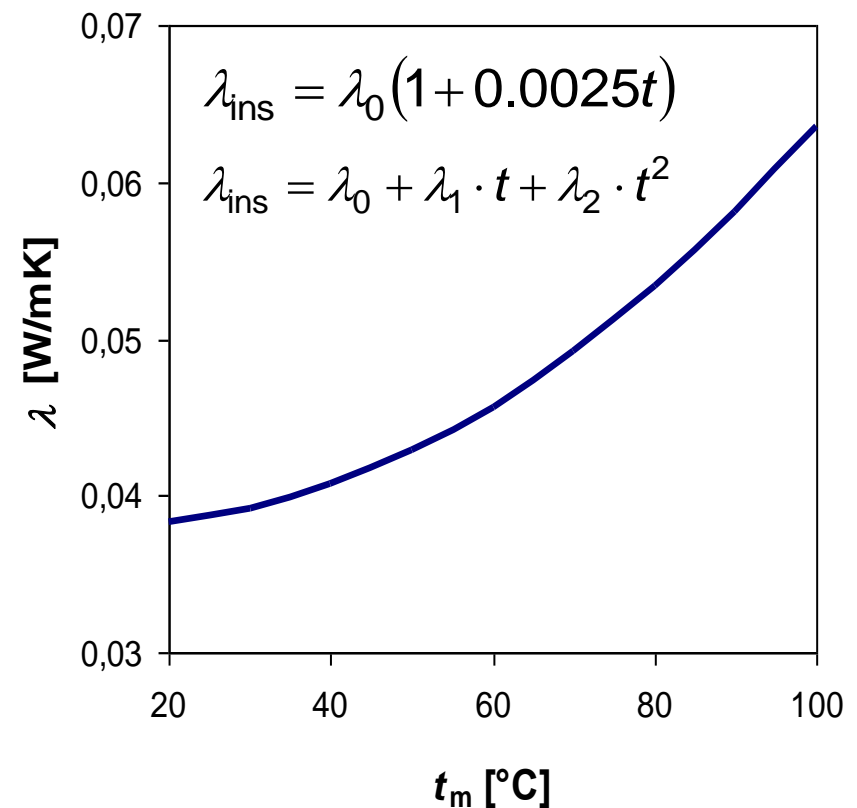
insulation – thermal conductivity:

mineral wool: $\lambda = 0.045 \text{ W/mK}$

PUR foam: $\lambda = 0.035 \text{ W/mK}$

polystyren: **weak resistance
to thermal load**

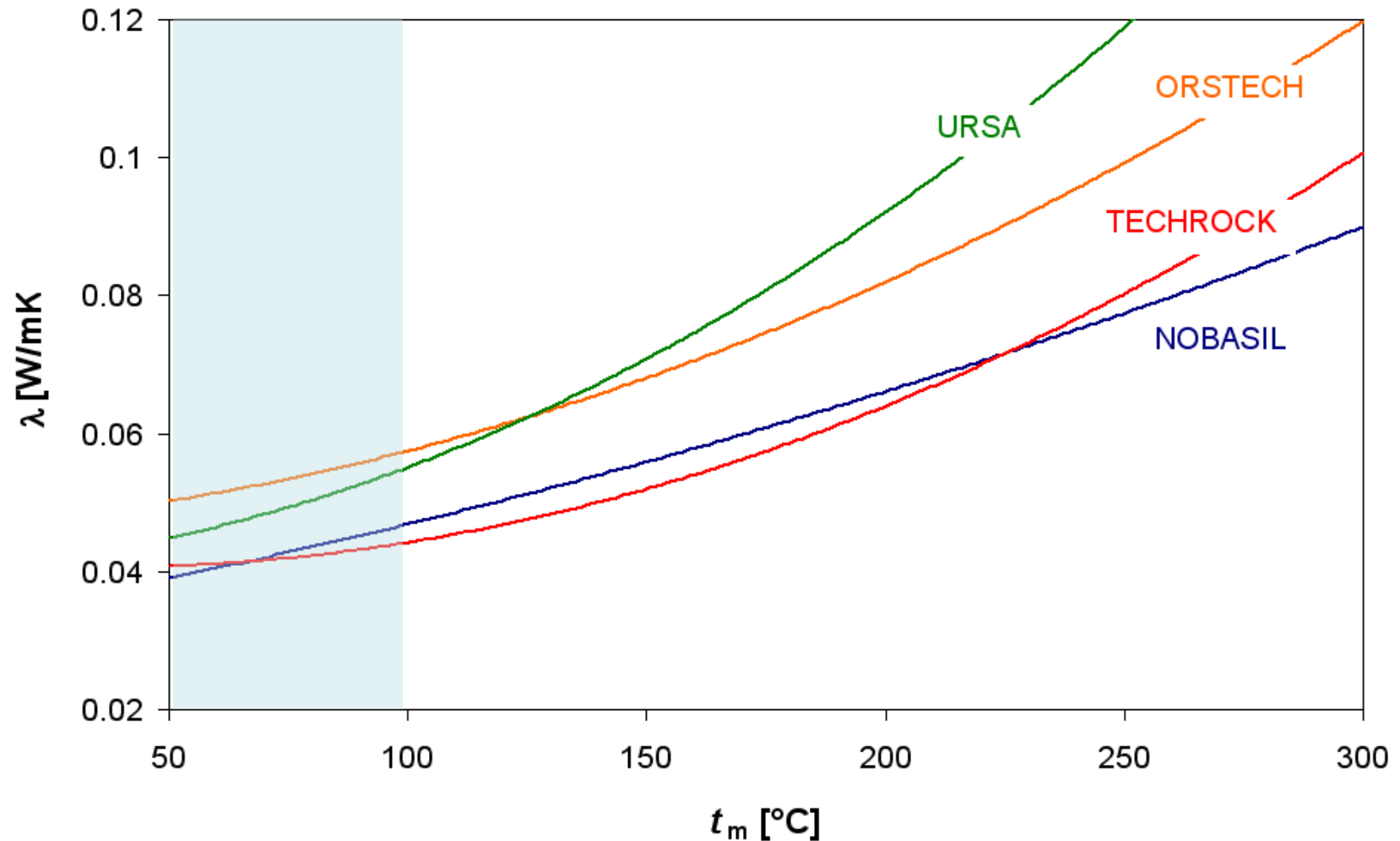
thermal conductivity $\lambda = f(t)$





Thermal conductivity of mineral wool

polynomic function





Insulation thickness in collector

- how can the thickness of insulation influence the thermal performance of the solar collector?
- influence on efficiency curve
- influence on the yields
- **what insulation thickness is reasonable?**
- compare 20 mm **30 mm** 50 mm

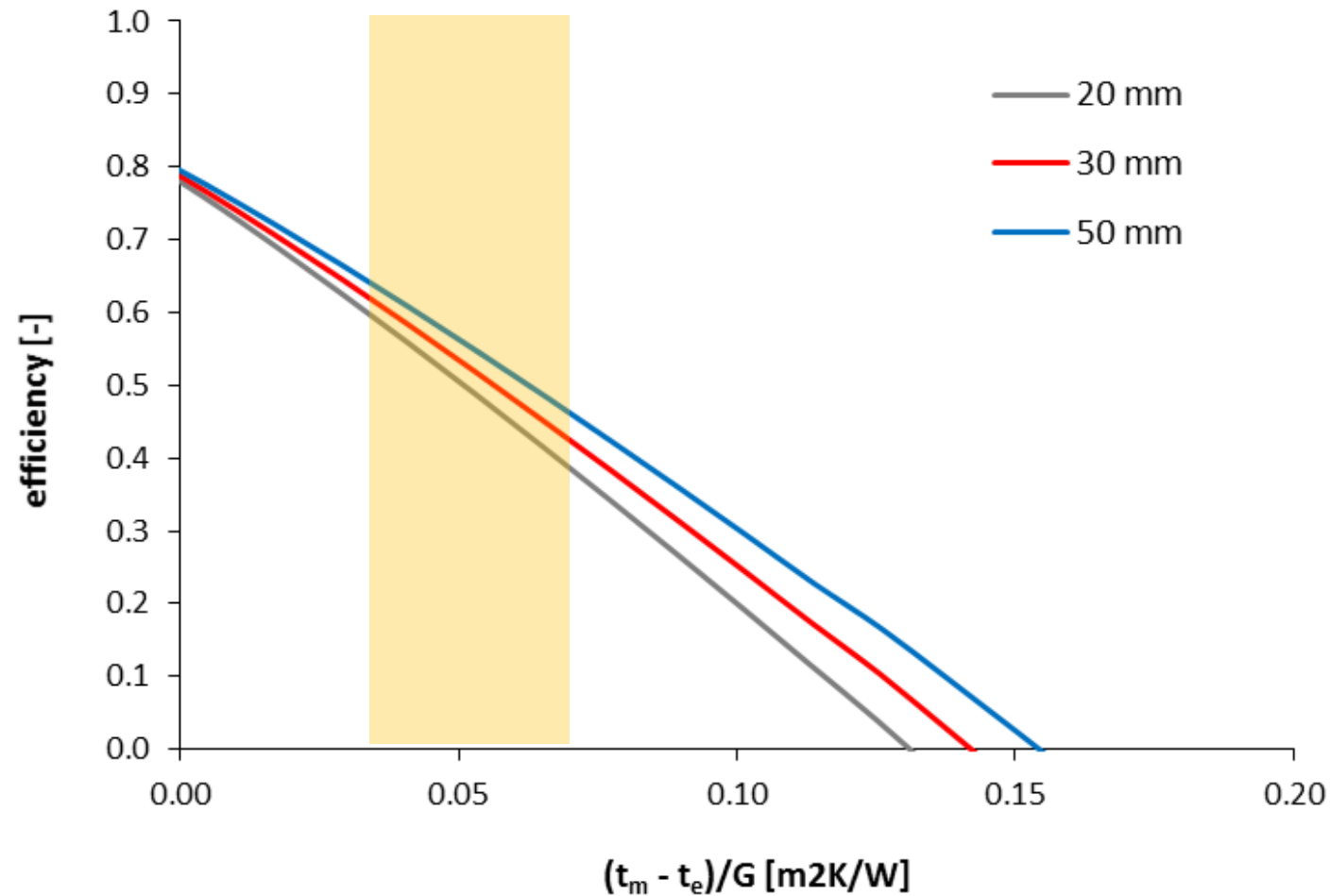


Insulation thickness in collector

- run KOLEKTOR programme, open **default.kol**
- Glazind & insulation card change **Insulation thickness**
- Calculation card select Efficiency curve calculation
Calculate, Export results
- open Evaluation.xls
- make copies of the sheets for three alternatives
- open res files in excel, mind the semicolons as separators
- **compare the efficiency curves based on $(t_m - t_e)/G$**



Insulation thickness in collector





Insulation thickness in collector

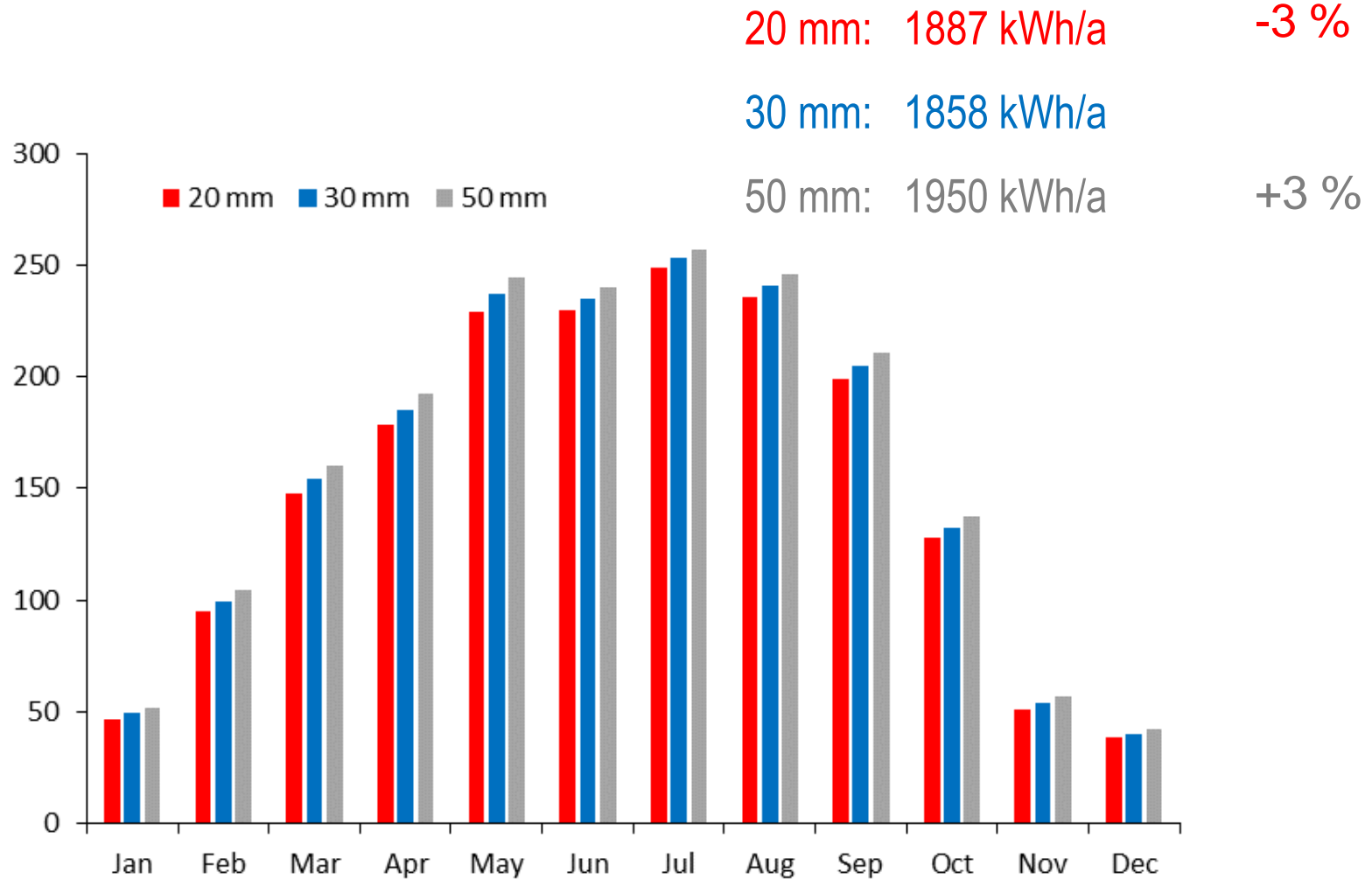
- how can the absorber emissivity influence the annual energy yields of collector?

■ 20 mm	$\eta_0 = 0.782$	$a_1 = 5.272$	$a_2 = 0.007$
■ 30 mm	$\eta_0 = 0.789$	$a_1 = 4.857$	$a_2 = 0.006$
■ 50 mm	$\eta_0 = 0.796$	$a_1 = 4.451$	$a_2 = 0.006$

- open studio SDHW-SOLNET in TRNSYS
- make a change of coefficients in KOLEKTOR type
- results of collector yield find under Totals.txt
- **compare the annual sums for both alternatives**



Insulation thickness in collector





Insulation thickness in collector

- compared to 30 mm of mineral wool double thickness of insulation brings only several percents
- **80 to 90 %** of the collector heat loss is the front side (top) loss
 - increase of insulation on the back side cannot proportionally help
- change of thermal conductivity by tens of percents due degradation will not significantly change the energy yields (by percents)
 - it does not matter for annual effectivity
 - facts above valid for **domestic hot water systems**



Radiation between frame and adj. surface

Radiation heat exchange between frame of collector and roof

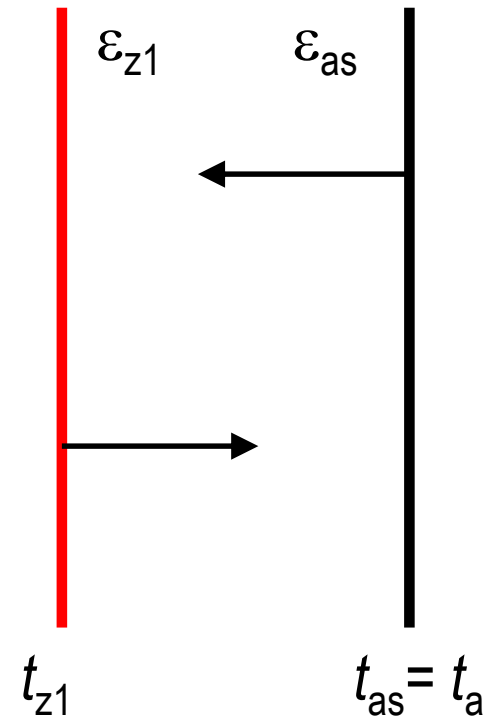
$$q_{s,z1-as} = \sigma \frac{T_{z1}^4 - T_{as}^4}{\frac{1}{\varepsilon_{z1}} + \frac{1}{\varepsilon_{as}} - 1} \quad [\text{W/m}^2]$$

any treatment of external frame
surface is **useless**

wind convection

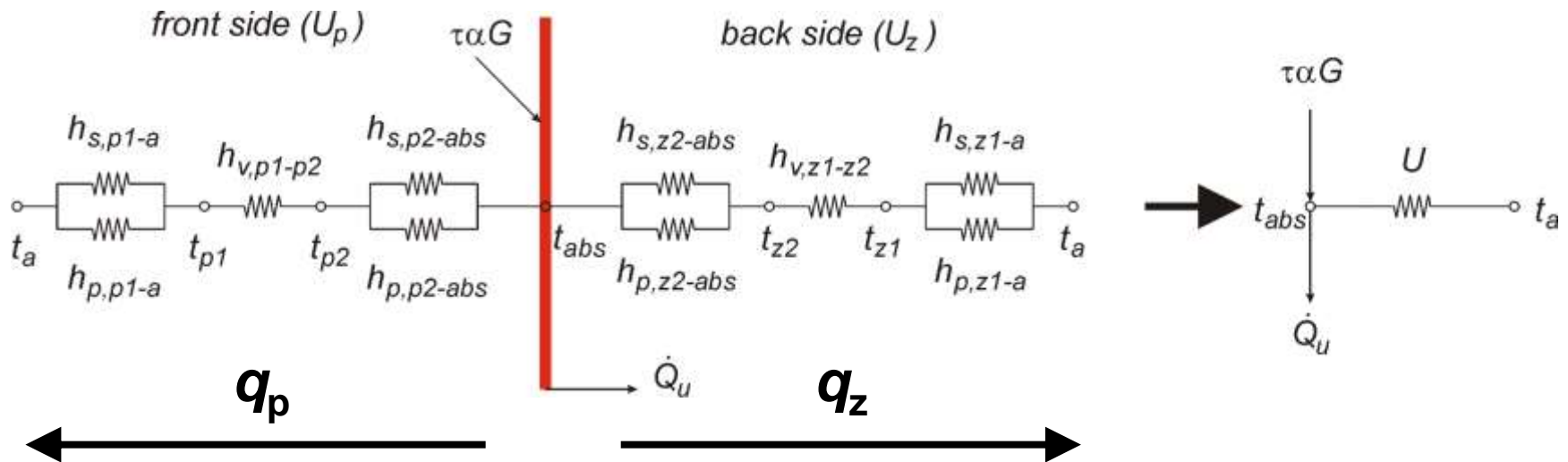
frame insulation

supress any influence





Collector heat loss coefficient: U -value

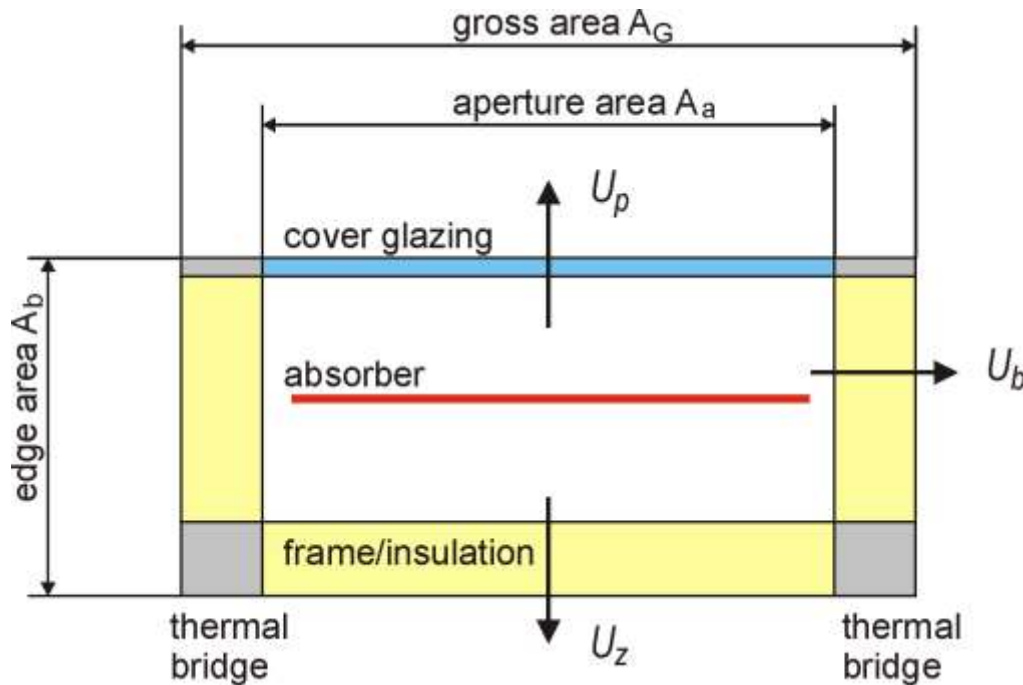


$$U_p = \frac{1}{\frac{1}{h_{s,p1-a} + h_{p,p1-a}} + \frac{1}{h_{v,p1-p2}} + \frac{1}{h_{s,abs-p2} + h_{p,abs-p2}}}$$

$$U_z = \frac{1}{\frac{1}{h_{s,z1-a} + h_{p,z1-a}} + \frac{1}{h_{v,z1-z2}} + \frac{1}{h_{s,abs-z2} + h_{p,abs-z2}}}$$



Collector heat loss coefficient: U-value



$$\dot{Q}_{l,t} = U_G A_G (t_{abs} - t_a)$$

$$\dot{Q}_{l,t} = U_a A_a (t_{abs} - t_a)$$

$$U_G A_G = U_p A_G + U_z A_G + U_b A_b = U_a A_a$$

$$U_a = \left(U_p + U_z + U_z \frac{A_b}{A_G} \right) \frac{A_G}{A_a}$$

for calculations:

U-value related to
aperture area **A_a**



Iterations for temperatures

calculation of heat transfer coefficients:

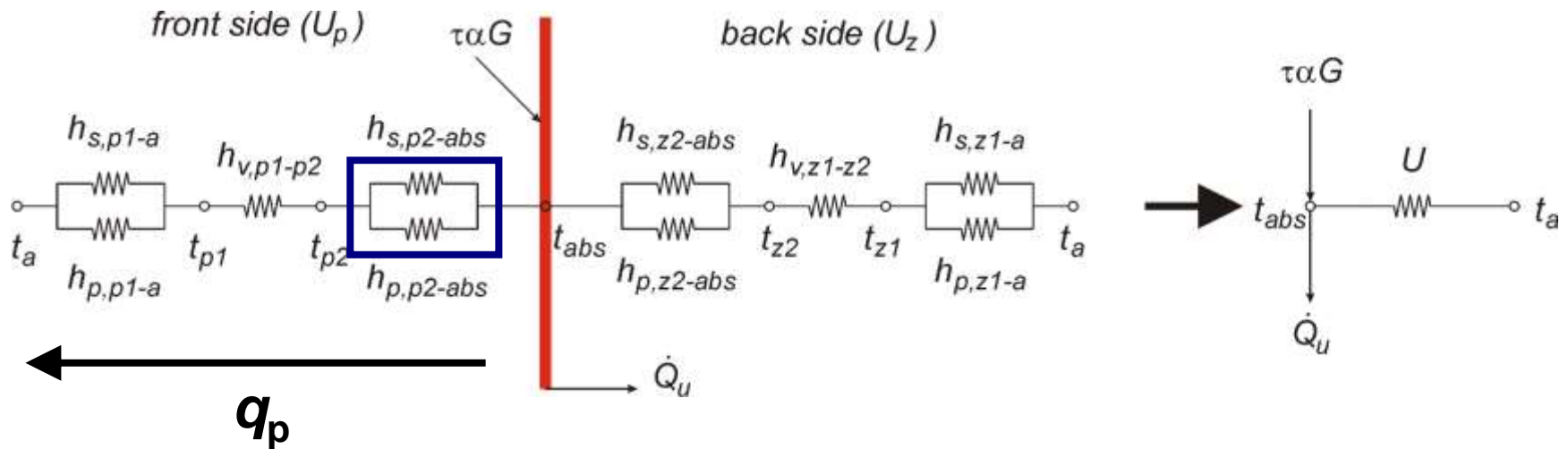
temperatures t_{abs} , t_{p1} , t_{p2} , t_{z1} , t_{z2} , (t_{b1} , t_{b2}) are required
but not available at the start of calculation

example of iterative determination for front heat flow:

1. estimate: $t_{\text{abs}} = t_{\text{in}} + \Delta t$
2. estimate: t_{p1} , t_{p2} $t_{p2} = t_{\text{abs}} - \frac{t_{\text{abs}} - t_a}{3}$ $t_{p1} = t_a + \frac{t_{\text{abs}} - t_a}{3}$
3. calculation of heat transfer coefficients h
4. calculation of overall heat flow rate q_p
5. reverse calculation of temperatures and then repeat from (3.)



Iterations for temperatures



$$q_p = U_p(t_{abs} - t_a)$$

$$q_p = (h_{s,abs-p1} + h_{p,abs-p1})(t_{abs} - t_{p1})$$

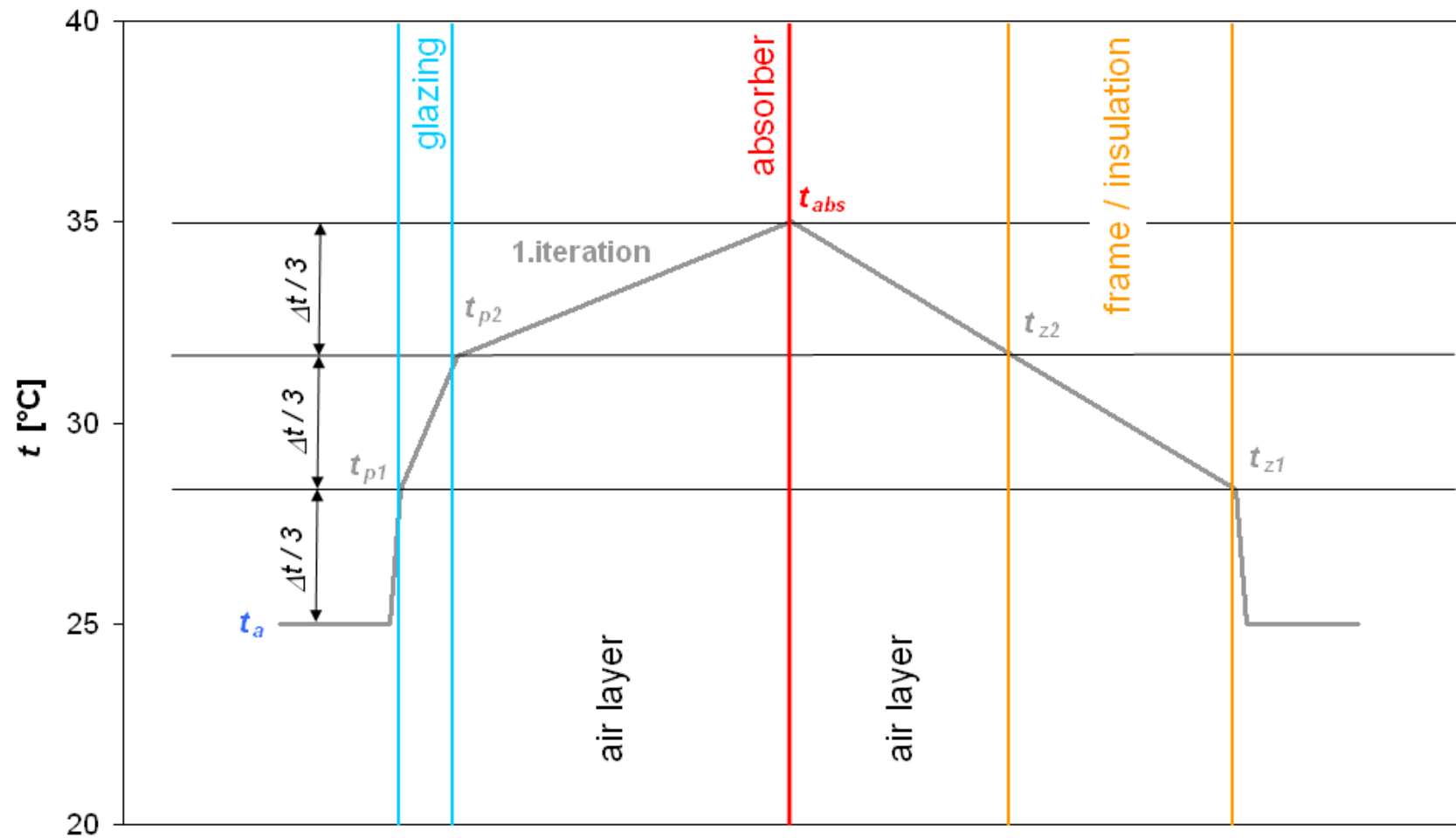
$$q_p = h_{v,p1-p2}(t_{p1} - t_{p2})$$

$$q_p = (h_{s,p2-a} + h_{p,p2-a})(t_{p2} - t_a)$$

temperature difference is
proportional to heat resistance

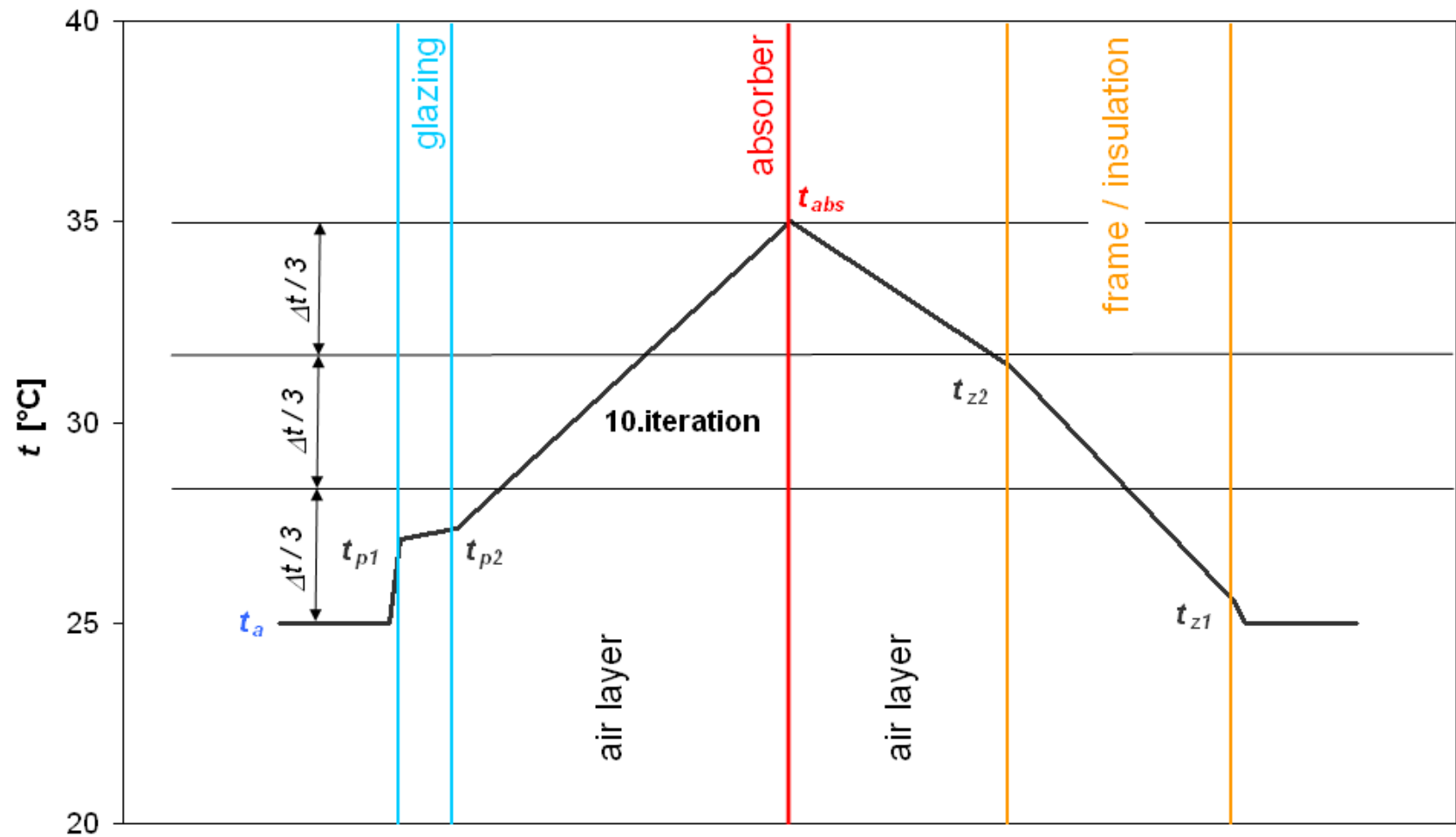


1. estimation of temperatures





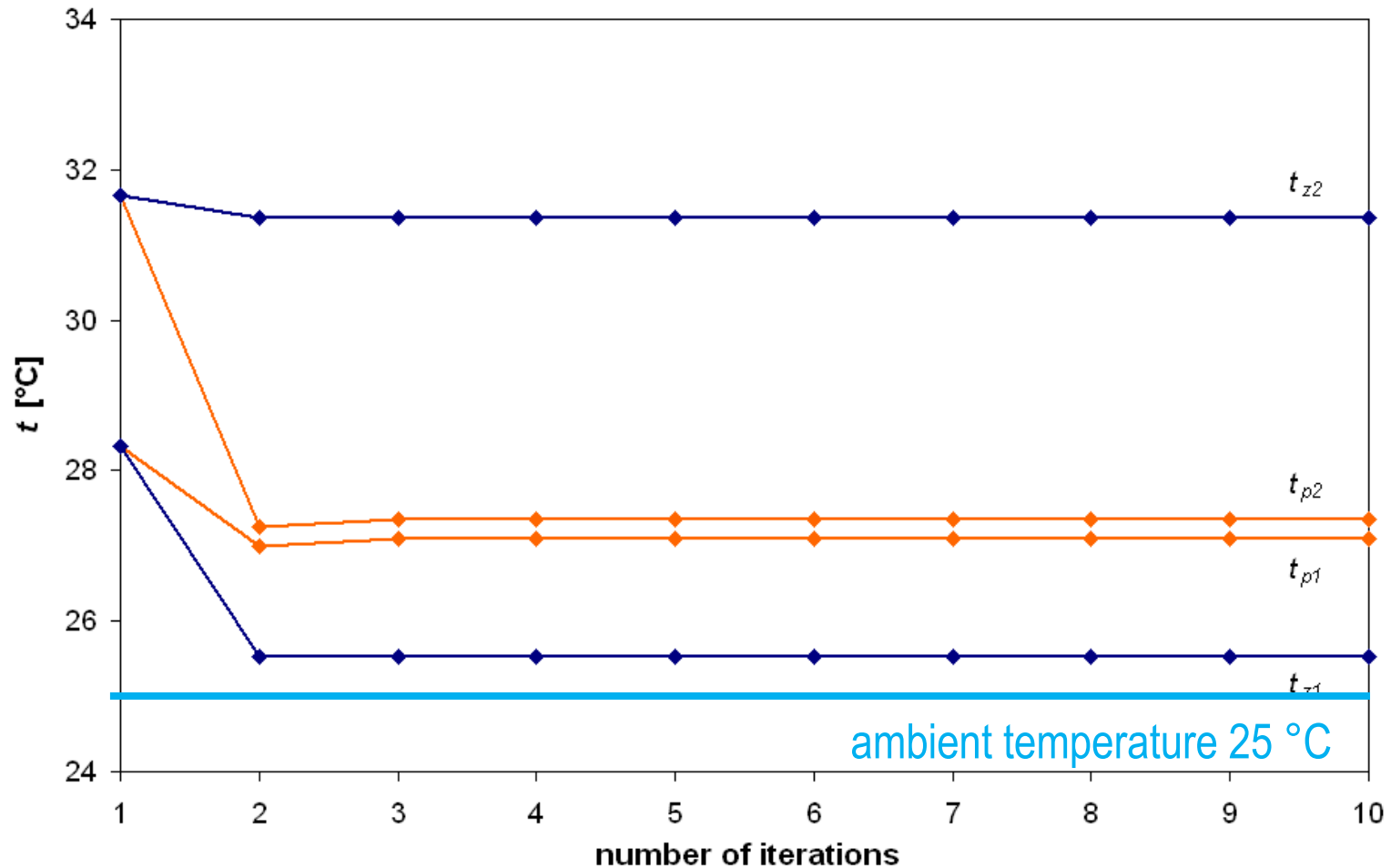
Last iteration





Convergence of calculations

absorber temperature 35 °C





Results of external balance

U-value of solar collector dependent on:

- temperature of absorber
- ambient temperature, wind velocity, sky temperature
- geometry of solar collector
- detailed properties of collector elements, used material (conductivity), surface emittance
- adjacent structure properties (emittance, envelope thermal resistance)



Analysis of Solar Flat-plate Collectors – part 2

Tomáš Matuška

Faculty of Mechanical Engineering

University Centre of Energy Efficient Buildings

Czech Technical University in Prague

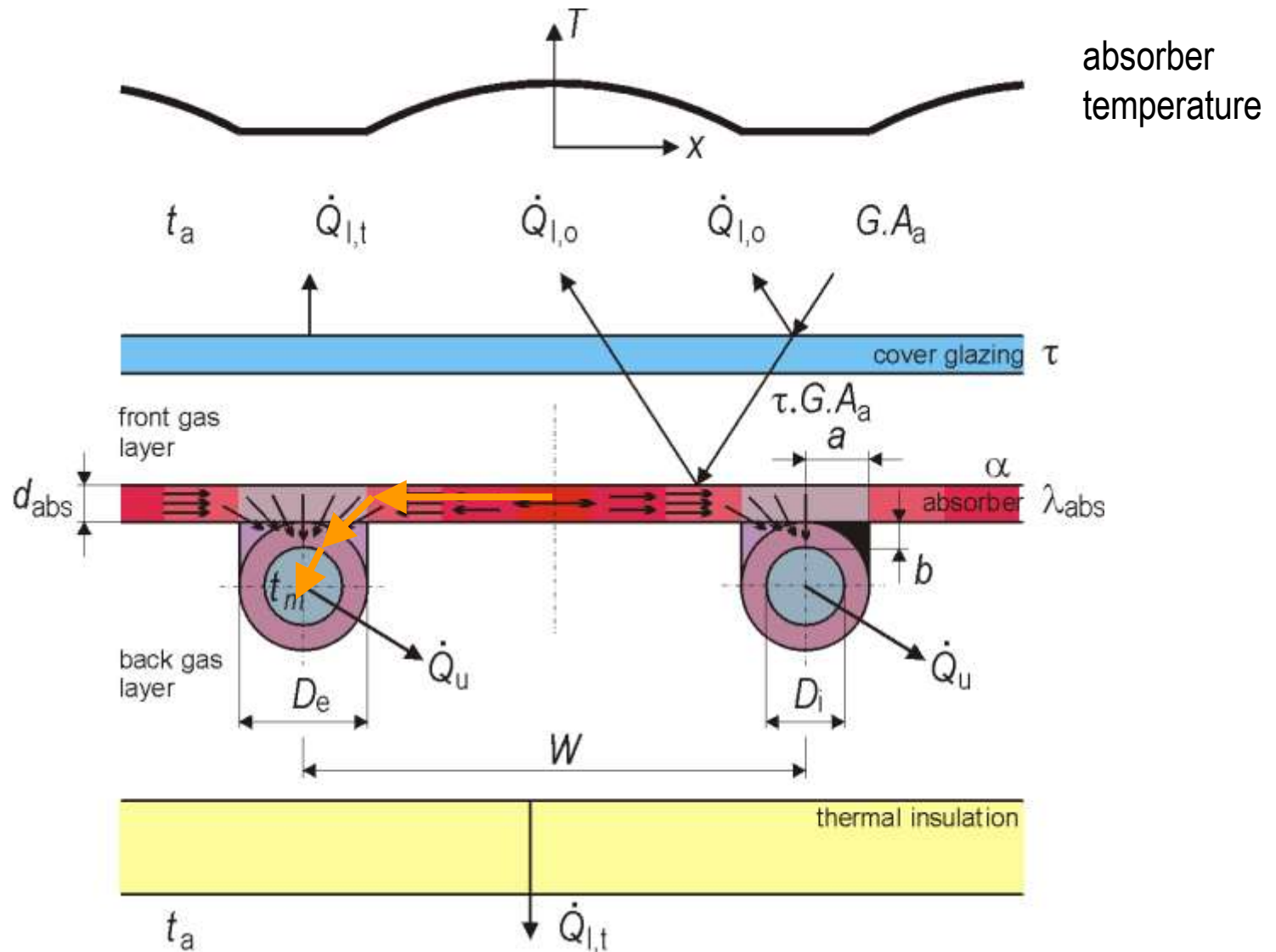


Solar collector energy balance

- **External energy balance of absorber**
 - heat flow from absorber surface to ambient environment
 - heat losses
 - quality of solar collector envelope
- **Internal energy balance of absorber**
 - heat flow from absorber surface into heat transfer fluid
 - ability to transfer heat and remove it from collector
 - quality of absorber construction

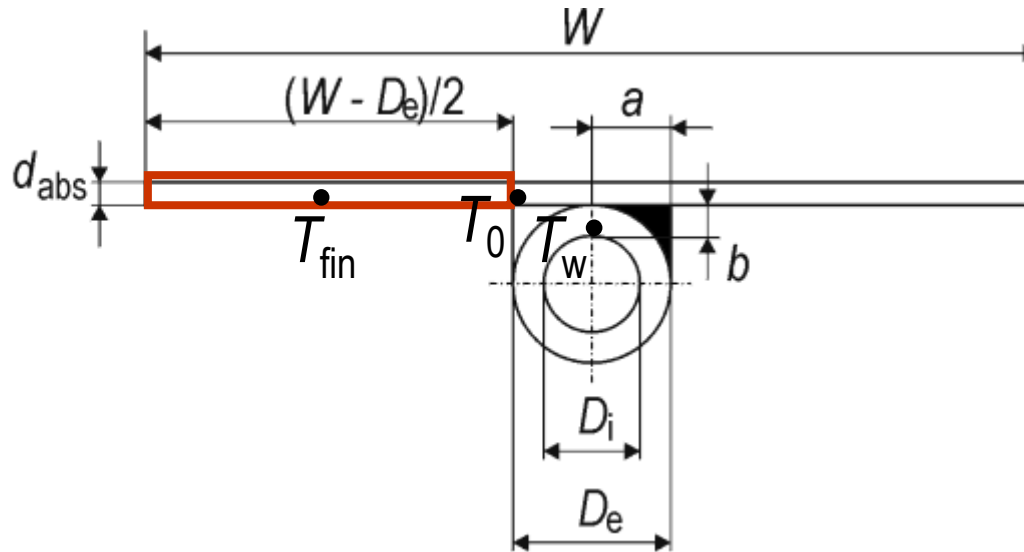


Internal energy balance





Energy balance of absorber fin



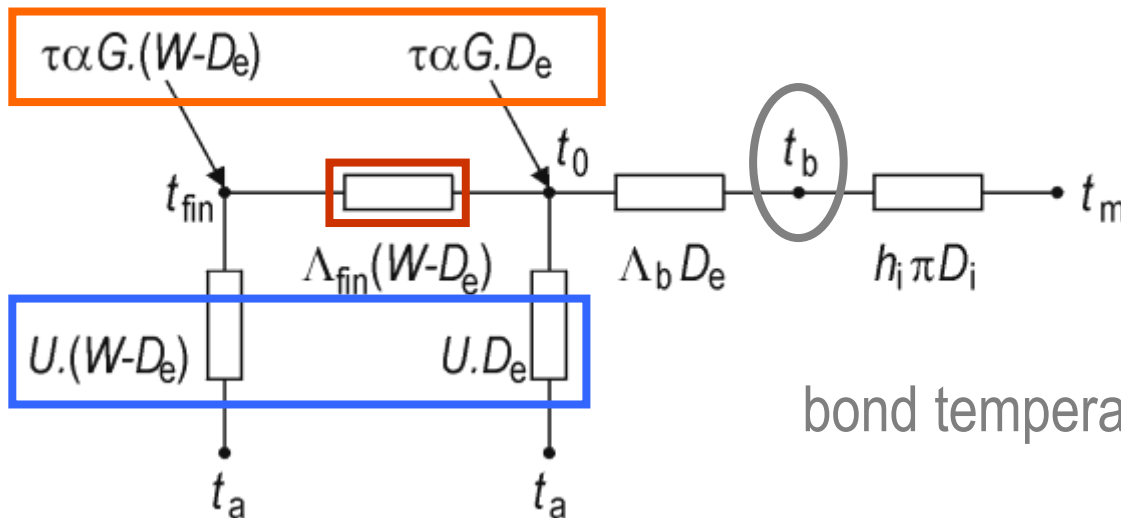
width W = distance
between riser pipes

$$D_e = 2a = 2 \cdot \text{bond width}$$

fin heat transfer Λ_{fin}

bond heat transfer Λ_b

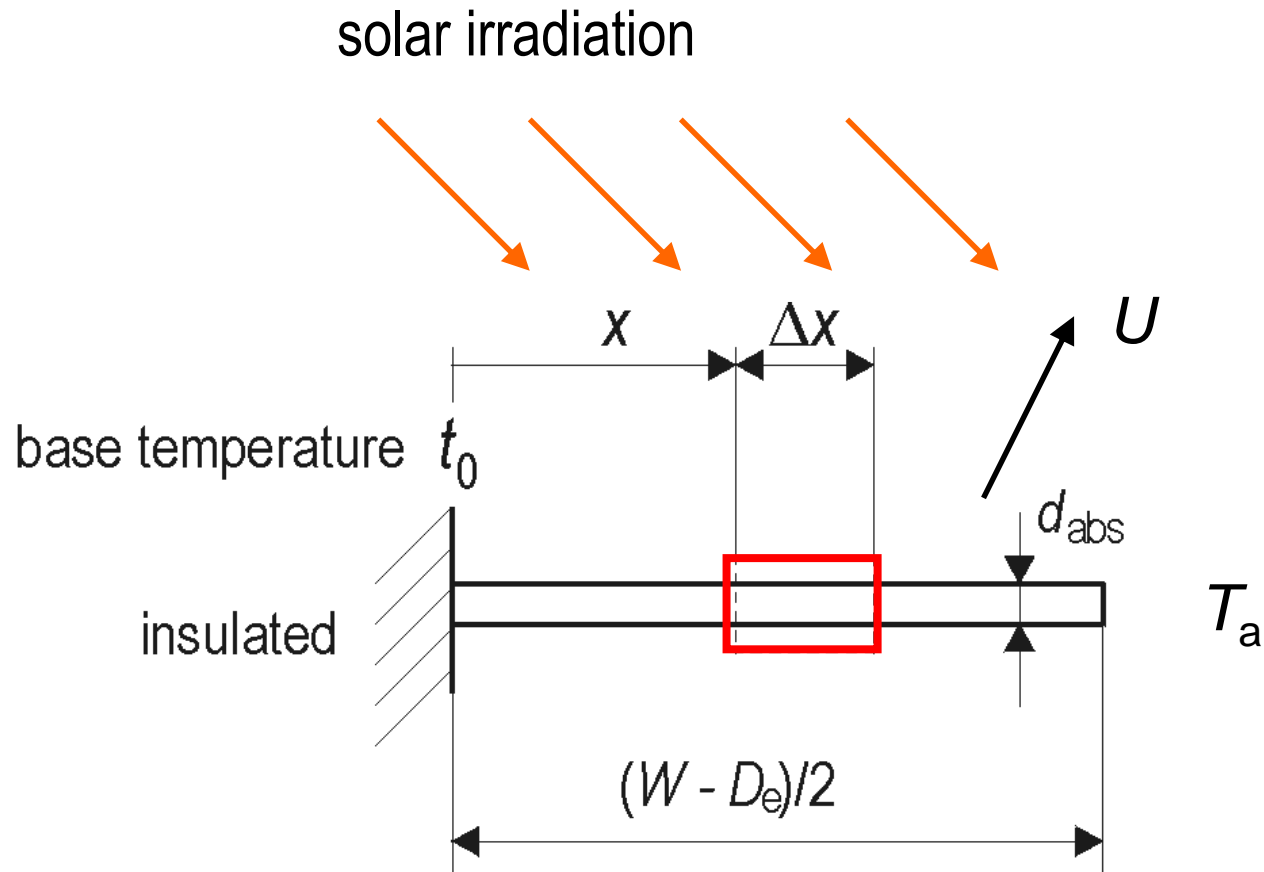
pipe-fluid heat transfer $h_i \pi D_i$



bond temperature $t_b = t_w$ (wall temperature)



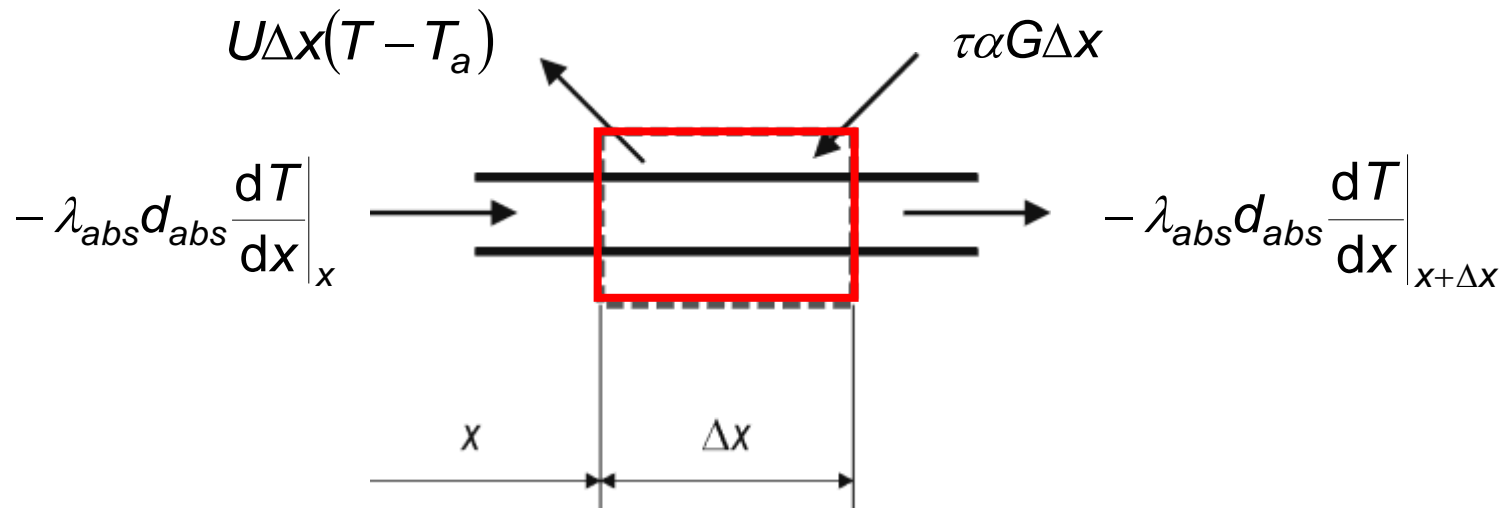
Energy balance of absorber fin



case of standard fin efficiency concept but with solar irradiation known from air-water heat exchangers theory



Energy balance of absorber fin element



derivation of temperature distribution between tubes (in absorber fin)

$$\tau\alpha G\Delta x - U\Delta x(T - T_a) + \left(-\lambda_{abs}d_{abs}\frac{dT}{dx}\right)\bigg|_x - \left(-\lambda_{abs}d_{abs}\frac{dT}{dx}\right)\bigg|_{x+\Delta x} = 0$$

yields in solution of differential
equation of 2nd order

$$\frac{d^2T}{dx^2} = \frac{U}{\lambda_{abs}d_{abs}} \left(T - T_a - \frac{S}{U} \right)$$

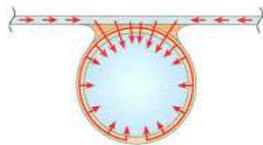


Fin efficiency F

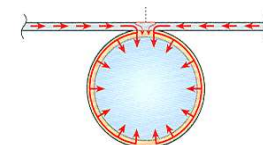
standard fin efficiency
(rectangular profile)

$$F = \frac{\tanh[m(W - D_e)/2]}{m(W - D_e)/2}$$

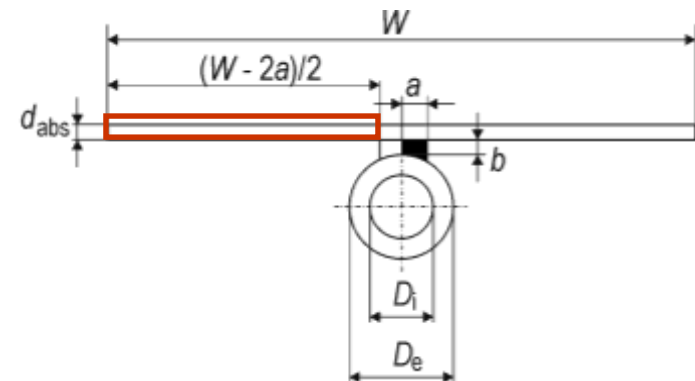
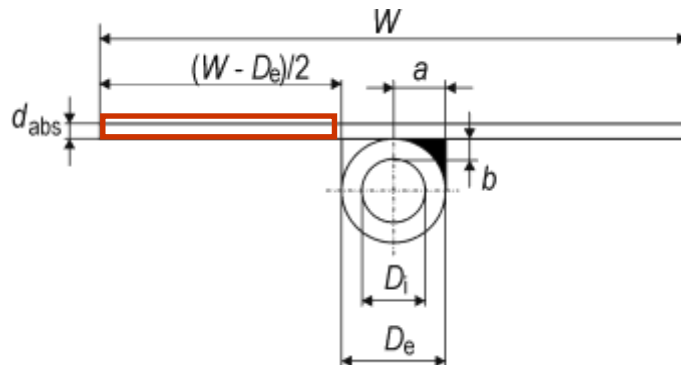
$(W - D_e)/2$ or $(W - 2a)/2$... active fin length



soldering



ultrasonic welding





Fin efficiency F

standard fin efficiency
(rectangular profile)

$$F = \frac{\tanh[m(W - D_e)/2]}{m(W - D_e)/2}$$

$$m = \sqrt{\frac{U}{\lambda_{\text{abs}} d_{\text{abs}}}}$$

U ... collector heat loss considered from absorber surface to ambient
(result from external balance)

significant influence of thermal conductivity and thickness of absorber
conductivity and thickness of absorber are impropotional

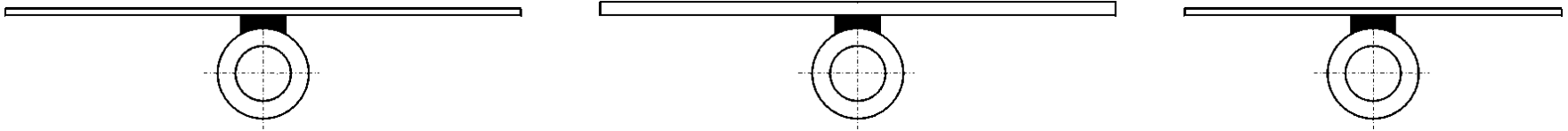
higher fin efficiency = higher heat removal from absorber



Fin efficiency F

reference case: fin efficiency 0.96

copper absorber (390 W/mK), $d_{abs} = 0.2 \text{ mm}$, fin $W^* = W - 2a = 100 \text{ mm}$
 heat loss coefficient $U = 4 \text{ W/m}^2\text{K}$



aluminium (240 W/mK)

$d_{abs} = 0.20 \text{ mm}$, $W^* = 79 \text{ mm}$

$d_{abs} = 0.32 \text{ mm}$, $W^* = 100 \text{ mm}$

steel (80 W/mK)

$d_{abs} = 0.2 \text{ mm}$, $W^* = 45 \text{ mm}$

$d_{abs} = 1.0 \text{ mm}$, $W^* = 100 \text{ mm}$

EPDM (0.14 W/mK) $d_{abs} = 2.0 \text{ mm}$, $W^* = 6 \text{ mm}$



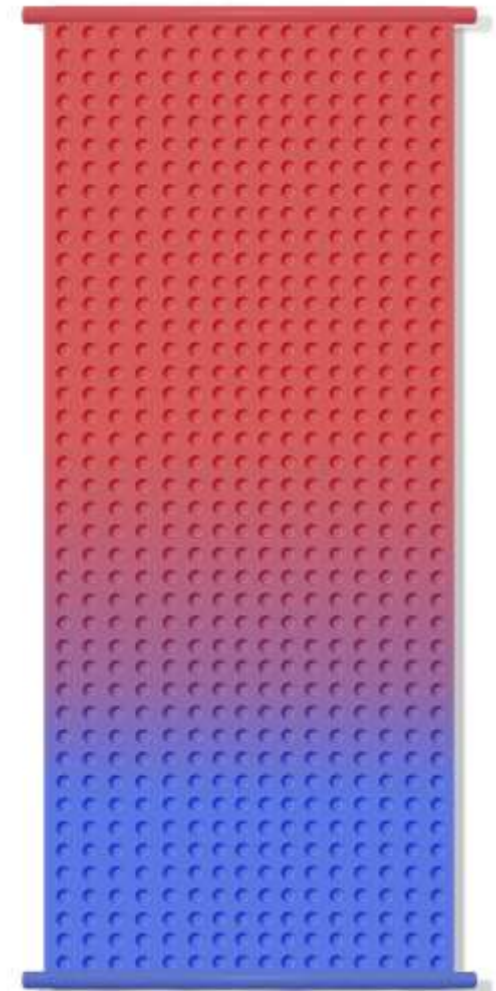
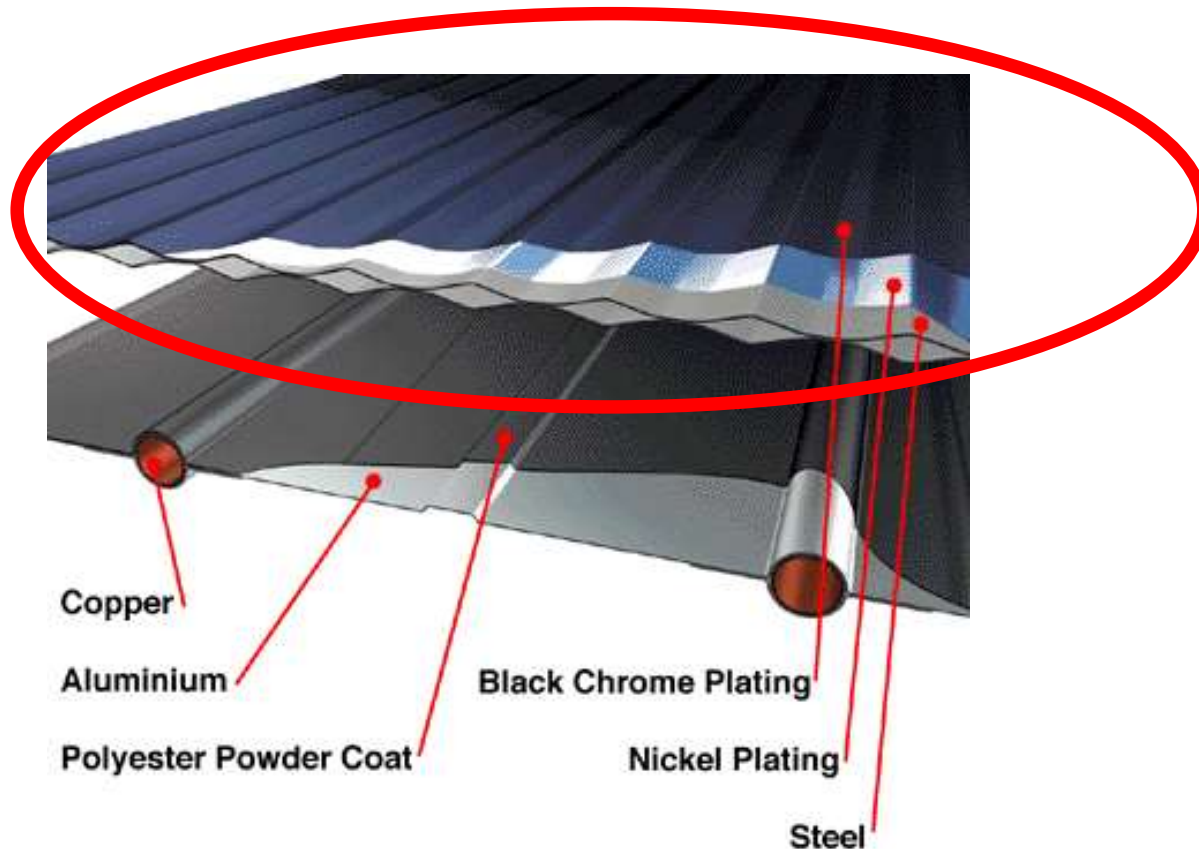
Plastic absorbers





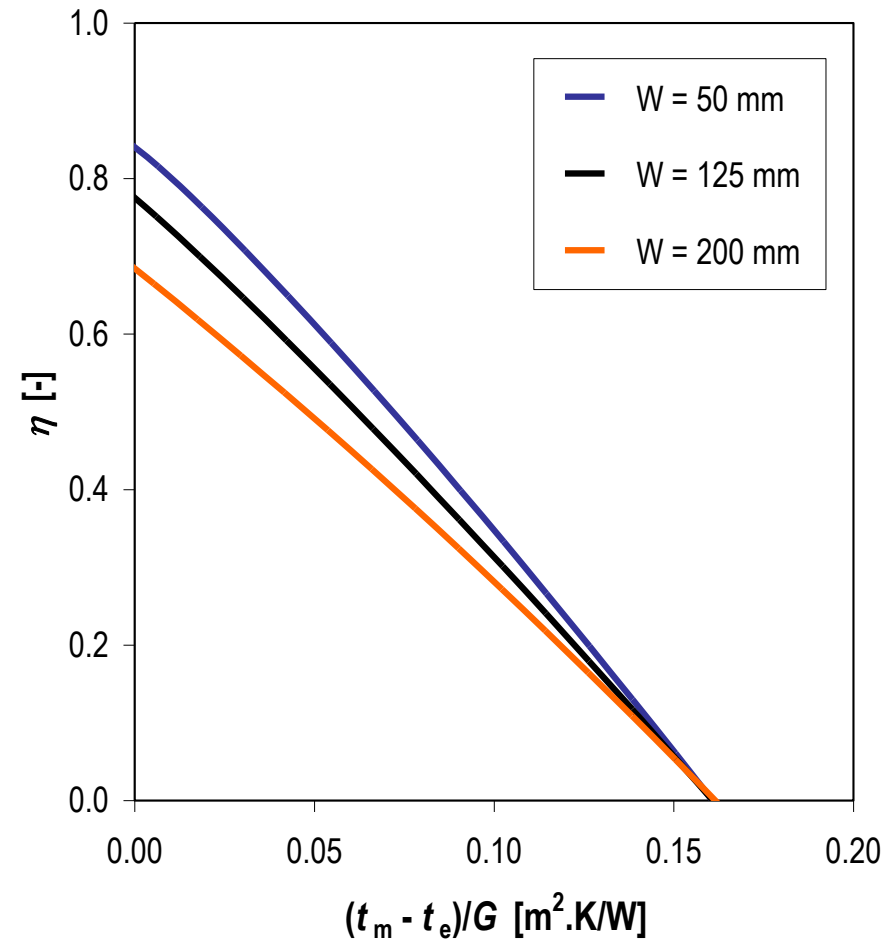
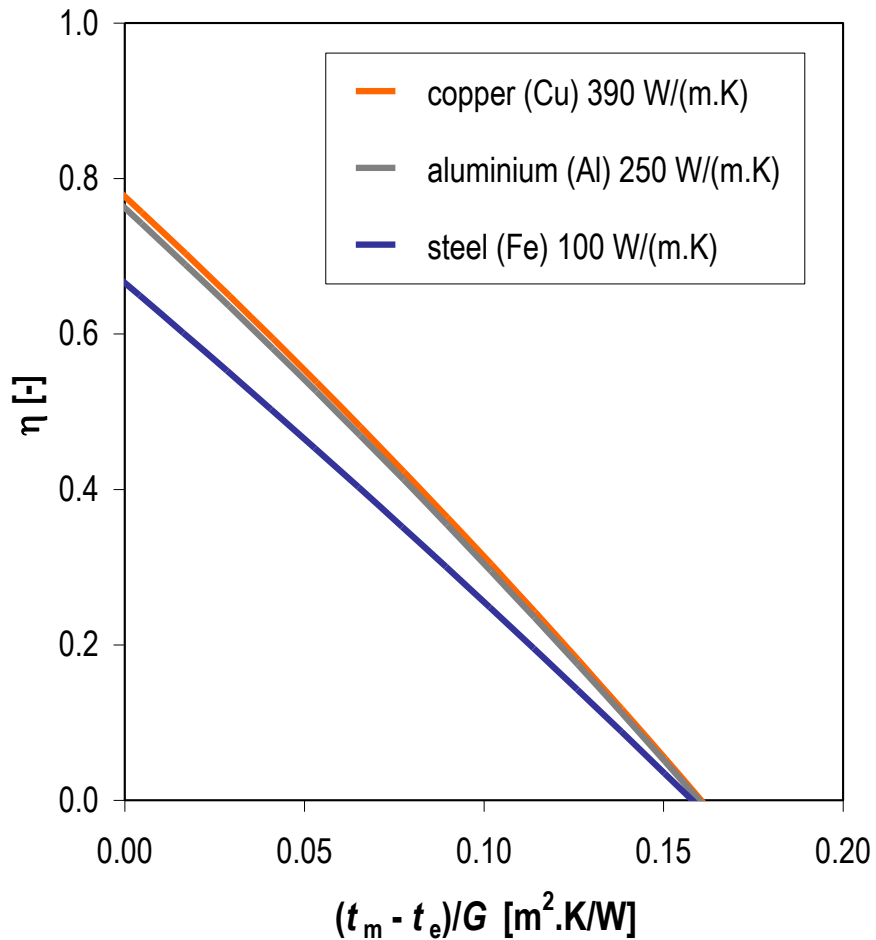
Best absorbers – fully wetted metal sheet

$$F' = 1.0$$





Influence of material and geometry



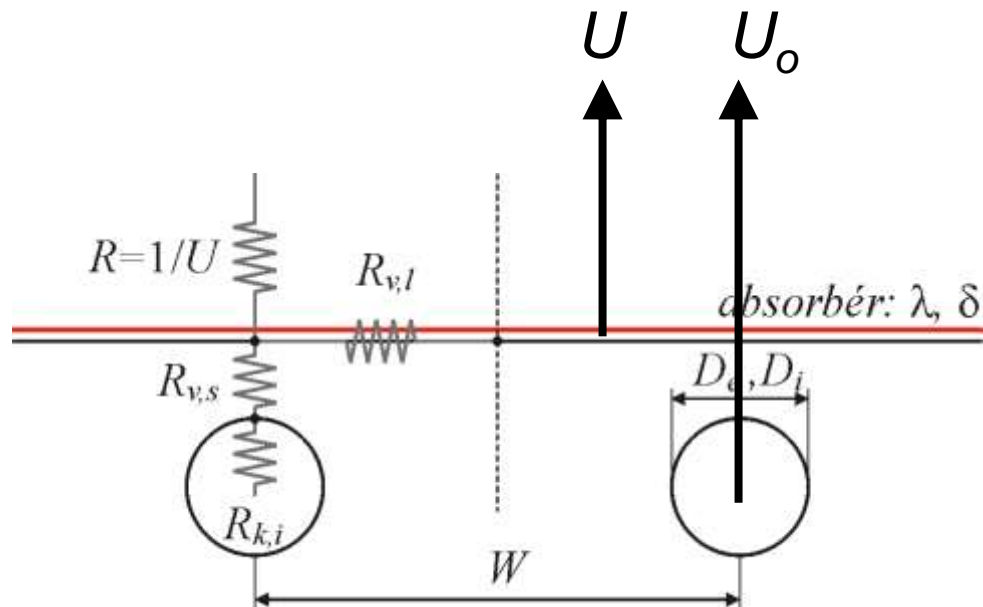


Efficiency factor F'

how efficient is heat transfer from absorber surface to heat transfer fluid ?

$$F' = \frac{U_o}{U} = \frac{\text{liquid to ambient loss}}{\text{abs. surface to ambient loss}}$$

$$\text{or } F' = \frac{\dot{q}_c(t_{abs})}{\dot{q}_c(t_{abs} = t_m)}$$



heat resistances:

conduction through fin

conduction through bond

convection inside pipe



Collector performance based on t_m

useful heat gain from collector

$$\dot{Q}_u = AF'[\tau\alpha G - U(t_m - t_a)]$$

$$t_m = \frac{t_{in} + t_{out}}{2}$$

collector efficiency

$$\eta = F' \left[\tau\alpha - U \frac{t_m - t_a}{G} \right]$$

analogy to experimentally obtained efficiency curve reported by testing institutes

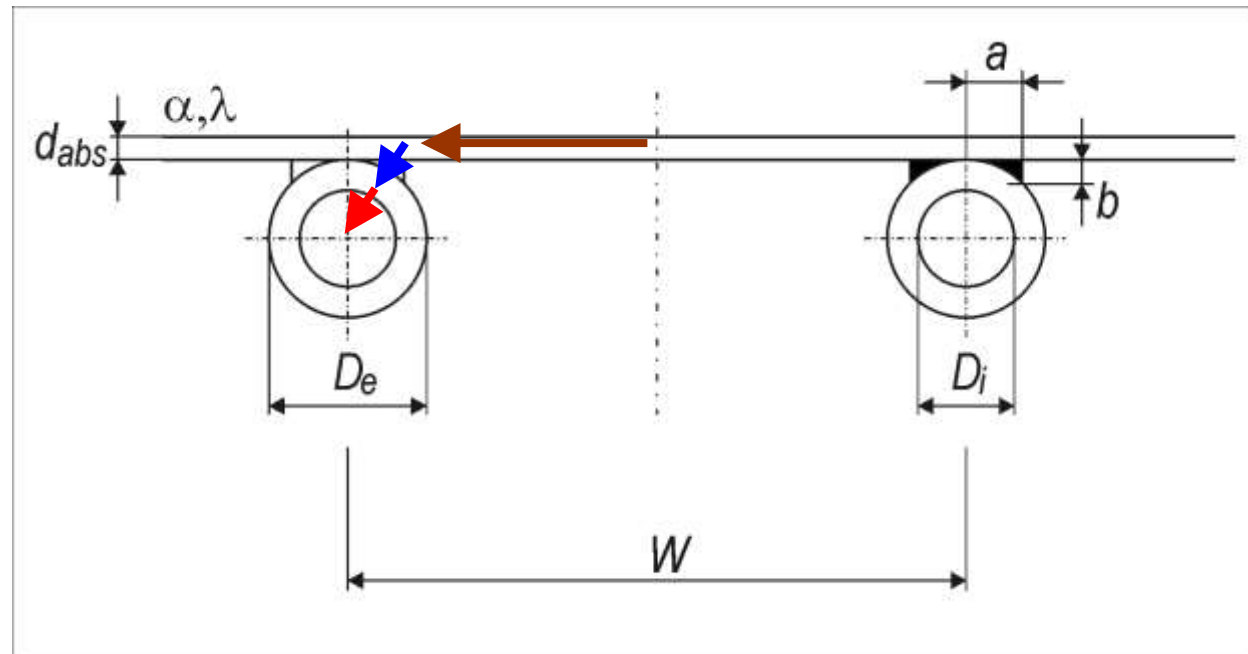
$$\eta = \eta_0 - a_1 \frac{t_m - t_a}{G} - a_2 \frac{(t_m - t_a)^2}{G}$$



Efficiency factor F'

$$F' = \frac{1/U}{W \left[\frac{1}{U[2a + (W - 2a)F]} + \frac{1}{C_b} + \frac{1}{h_{fi} \pi D_i} \right]}$$

function of fin efficiency F



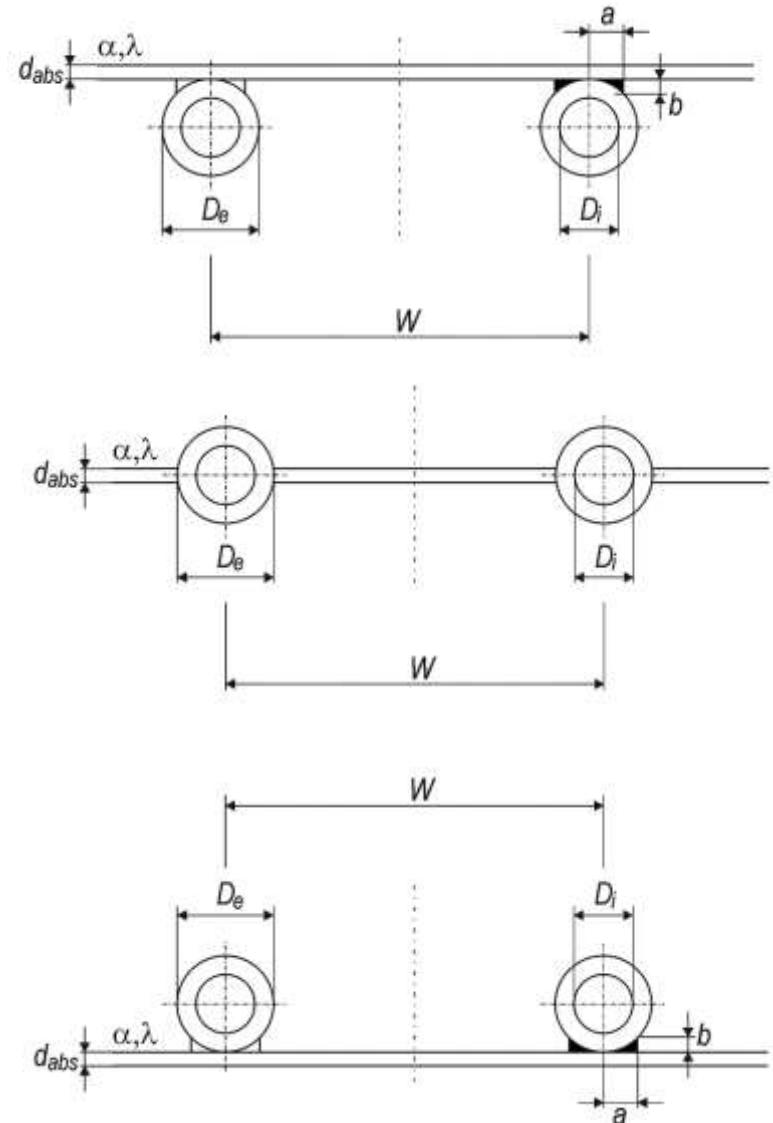


Efficiency factor – absorber designs

$$F' = \frac{1/U}{W \left[\frac{1}{U[2a + (W - 2a)F]} + \frac{1}{C_b} + \frac{1}{h_{fi} \pi D_i} \right]}$$

$$F' = \frac{1/U}{W \left[\frac{1}{U[2a + (W - 2a)F]} + \frac{1}{h_{fi} \pi D_i} \right]}$$

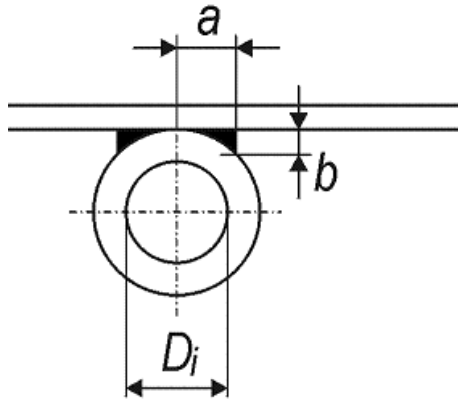
$$F' = \frac{1}{\frac{WU}{h_{fi} \pi D_i} + \frac{1}{\frac{2a}{W} + \frac{WU}{C_b} + \frac{1}{(W - 2a)F}}}$$





Bond conductance

bond conductance – estimated from geometry and quality of contact



$$C_b = \frac{\lambda_b a}{b}$$

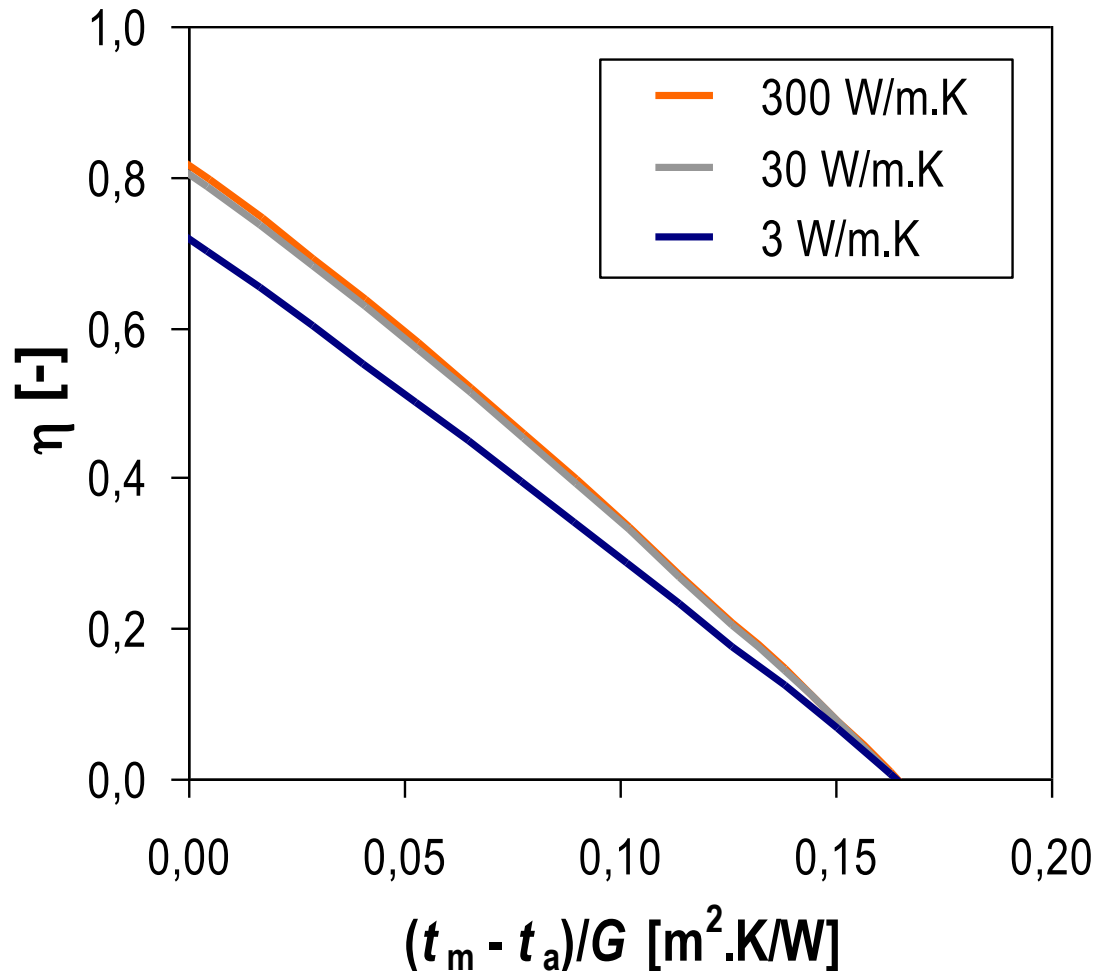
good metal-to-metal contact needed (welding, soldering, pressing)
no clamping of absorber to pipes !

bond conductance > 30 W/mK needed



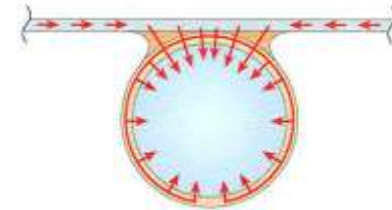
Bond conductance

for $C_b < 30 \text{ W/mK}$ significant reduction of collector performance

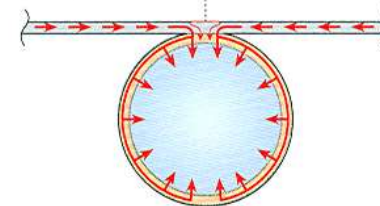


practically no difference between high and middle quality bonds

brazed contact

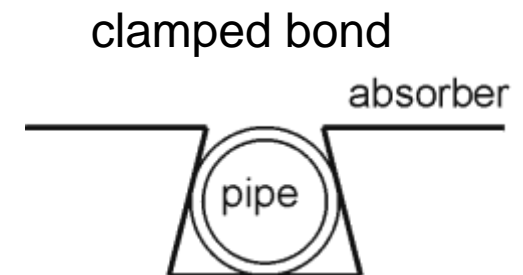
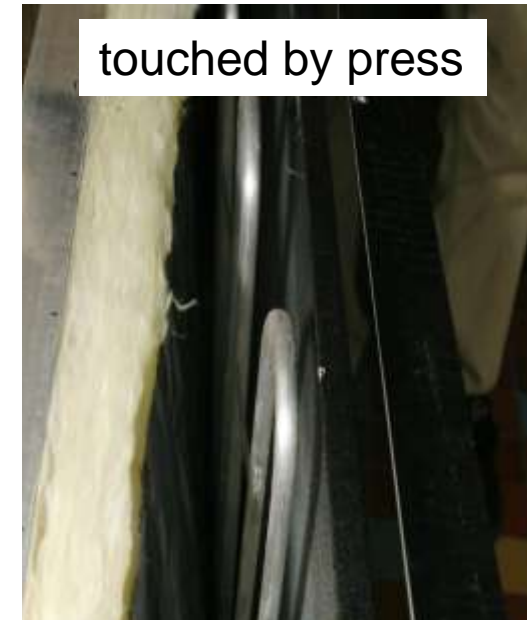
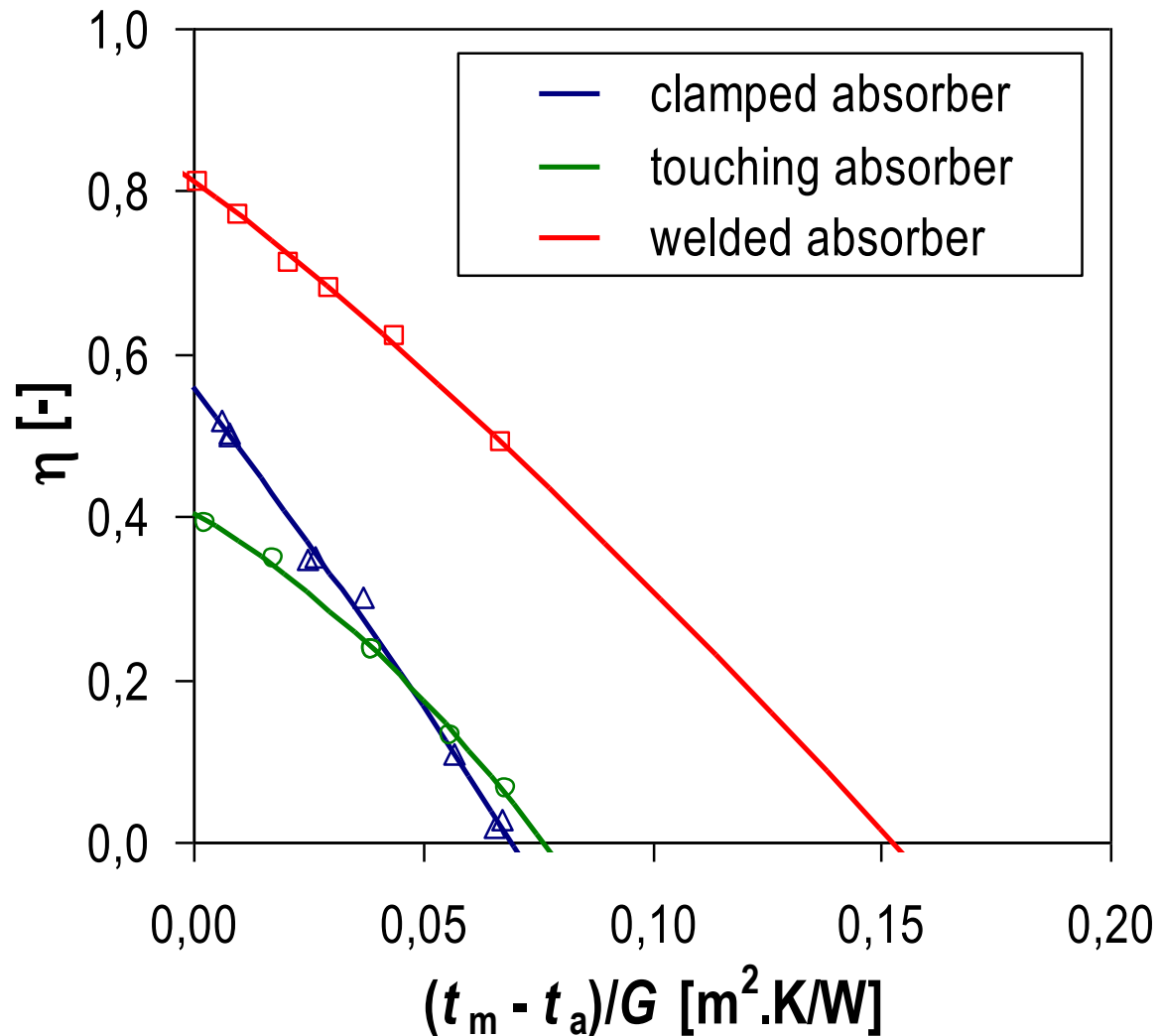


ultrasonic welded contact





Bond conductance: testing

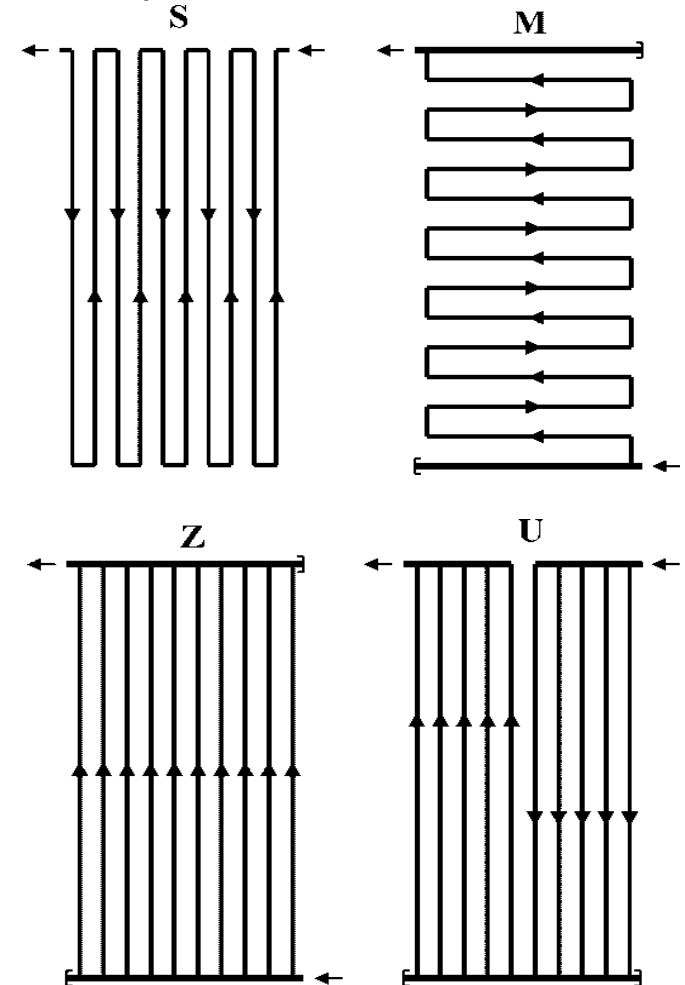
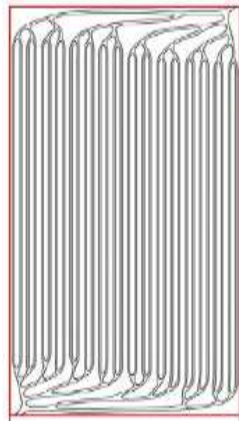




Convection heat transfer inside pipes

forced convection heat transfer in pipes is given by:

- heat transfer fluid type
- collector flow rate
- concept of collector hydraulic (parallel, serial-parallel, serpentine)
- number of risers (flow rate distribution)
- diameter of risers
- temperature





Convection heat transfer inside pipes

Nusselt number as criterion, number of models are available for

- **laminar flow** (mostly present in collector), turbulent flow
- **constant heat flux case** (uniformly irradiated absorber condition)
- constant temperature (heat transfer with phase change)
- fully developed profile, entry region with developing profile of velocity and temperature

$$h_{fi} = Nu_D \cdot \frac{\lambda_f}{D_i}$$



Nusselt number in circular pipes

- **laminar flow**, fully developed velocity and temperature profile, constant heat flux

$$\text{Nu}_D = \frac{48}{11} = 4.364 \quad (\text{Shah})$$

- **laminar flow**, entry region of length L , developing profile, constant heat flux

$$\text{Nu}_D = \begin{cases} 1.953 \cdot L^{*-1/3} & L^* \leq 0.03 \\ 4.364 + \frac{0.0722}{L^*} & L^* > 0.03 \end{cases} \quad (\text{Shah})$$

$$L^* = \text{Gz}^{-1} = \frac{L/D_i}{\text{Re}_D \cdot \text{Pr}}$$

Gz ... Graetz number



Nusselt number in circular pipes

- **turbulent flow**

$$\text{Nu}_D = A \text{Re}_D^m \text{Pr}^n \quad (\text{Dittus-Boelter, Colburn, Sieder-Tate})$$

$$\text{Nu}_D = \frac{(f/8)(\text{Re}_D - 1000)\text{Pr}}{1 + 12.7(f/8)^{1/2}(\text{Pr}^{2/3} - 1)} \quad (\text{Gnielinski})$$

where $f = (0.79 \ln \text{Re}_D - 1.64)^{-2}$ for smooth pipes

for more models see Reference handbook to KOLEKTOR



Convection heat transfer inside pipes

- **high heat transfer require**

- high velocity
- higher flow rate
- low dimension
- low viscosity
- high conductivity of liquid

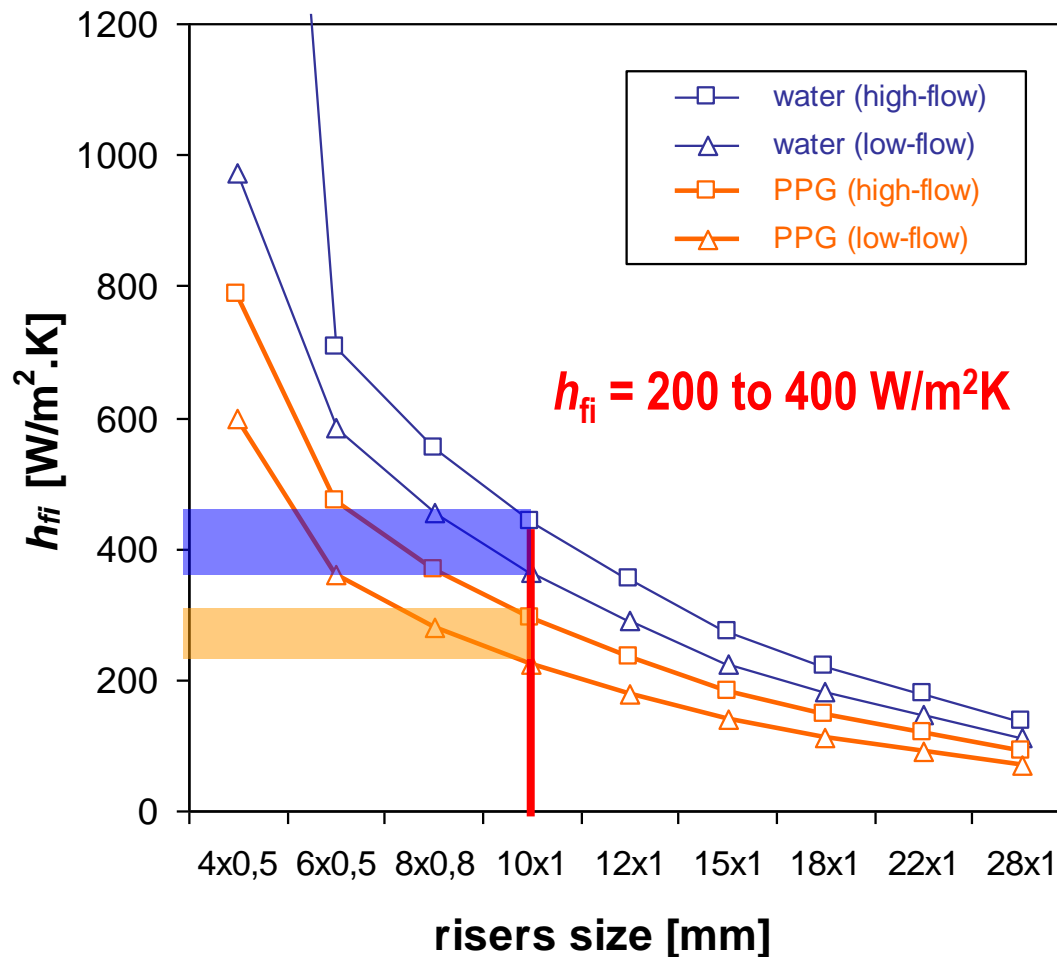


high Reynolds number

high Nusselt number



Convection heat transfer inside pipes



high flow: 0.025 kg/s.m^2

low flow: 0.005 kg/s.m^2



Influence of riser pipe diameter

$$F' = \frac{1/U}{W \left[\frac{1}{U[2a + (W - 2a)F]} + \frac{1}{C_b} + \frac{1}{h_{fi} \pi D_i} \right]}$$

$$\frac{1}{h_{fi} \pi D_i} = \frac{D_i}{Nu \lambda_f} \frac{1}{\pi D_i} = \frac{1}{Nu \lambda_f \pi}$$

term is dependent directly on Nu

laminar flow

$$Nu_D = f(\text{constant}) = 4.364$$

$$Nu_D = f(L^*)$$

thermal diffusivity

$$L^* = \frac{L}{D_i} \frac{\nu}{u \cdot D_i} \frac{\alpha}{\nu} = \frac{L \cdot \alpha}{D_i^2} \frac{\pi D_i^2}{4 \dot{V}} = \frac{\pi L \alpha}{4 \dot{V}}$$

term $\frac{1}{h_i \pi D}$ is independent of D in laminar flow



Analysis of efficiency factor F'

length $L = 2$ m, fin width $W = 100$ mm, absorber thickness $d = 0.2$ mm,
copper $\lambda = 350$ W/m.K, pipe $D_e/D_i = 10/8$ mm

bond conductance $C_b = 250$ W/K

$h_i = 400$ W/m²K

	$\frac{1}{U \cdot [D_e + (W - D_e) \cdot F]}$	$\frac{1}{C_{spoj}}$	$\frac{1}{h_i \cdot \pi \cdot D_i}$
$U = 4$ W/m ² .K	2,6	0,004	0,099

heat transfer coefficient: **minor influence** to F' if $h_i > 200$ W/m²K

bond conductance: **minor influence** to F' if $C_b > 30$ W/mK

geometry is principal property of absorber if low heat loss collector



Do we need for turbulators in pipes?

length $L = 2$ m, fin width $W = 110$ mm, absorber thickness $d = 0.2$ mm,
copper $\lambda = 350$ W/m.K, pipe $D_e/D_i = 10/8$ mm

bond conductance $C_b = 200$ W/K

$U = 4$ W/m²K

	$\frac{1}{h_i \cdot \pi \cdot D_i}$	F
		$U = 4$ W/m ² K
$h_i = 400$ W/m ² .K	0.099	0.919
$h_i = 600$ W/m ² .K	0.066	0.931

enhancement of heat transfer inside pipe by **50 %**

minor influence to F change by **1.3 %**



Fully wetted absorber vs. fin&tube

- how can the geometry of the absorber influence the thermal performance of the solar collector?
- influence on efficiency curve
- influence on the yields

- **fully wetted absorber from steel**
 - type of bond middle, pipes $D_e/D_i = 6/5$ mm, bond $a/b = 3/1$ mm
 - material steel, thickness 0.5 mm
 - bond conductivity 100 W/mK
 - number of channels 145 pcs (not 150 pcs) ... **$W = 6.01$ mm $> D_e$**

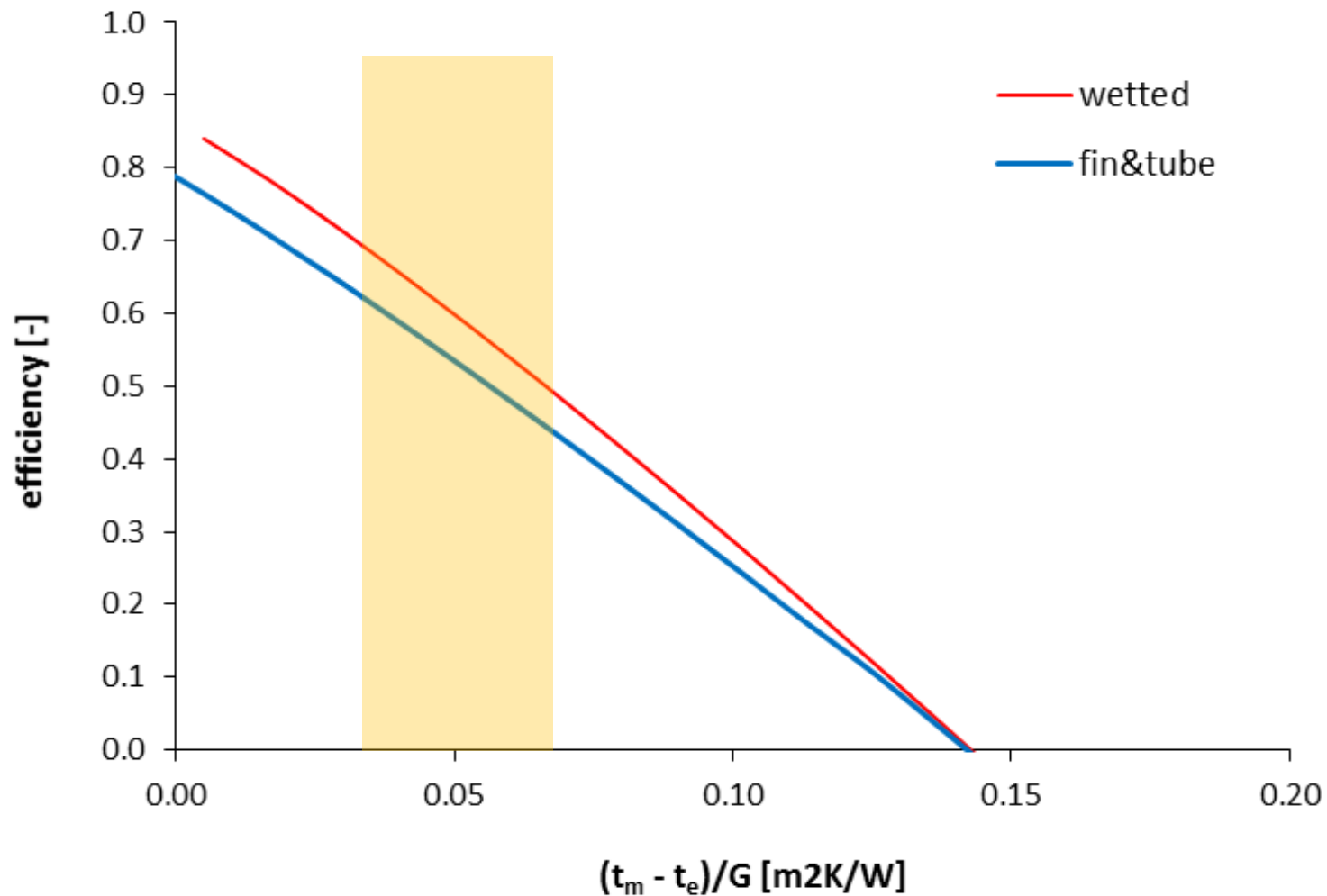


Fully wetted absorber vs. fin&tube

- run KOLEKTOR programme, open **default.kol**
- Absorber card make the changes **Material, Type of bond**
 change Geometry, dimensions
- Calculation card select Efficiency curve calculation
 Calculate, Export results
- open Evaluation.xls
- make a copy for the wetted alternative
- open res file in excel, mind the semicolons as separators
- **compare the efficiency curves based on $(t_m - t_e)/G$**



Fully wetted absorber vs. fin&tube





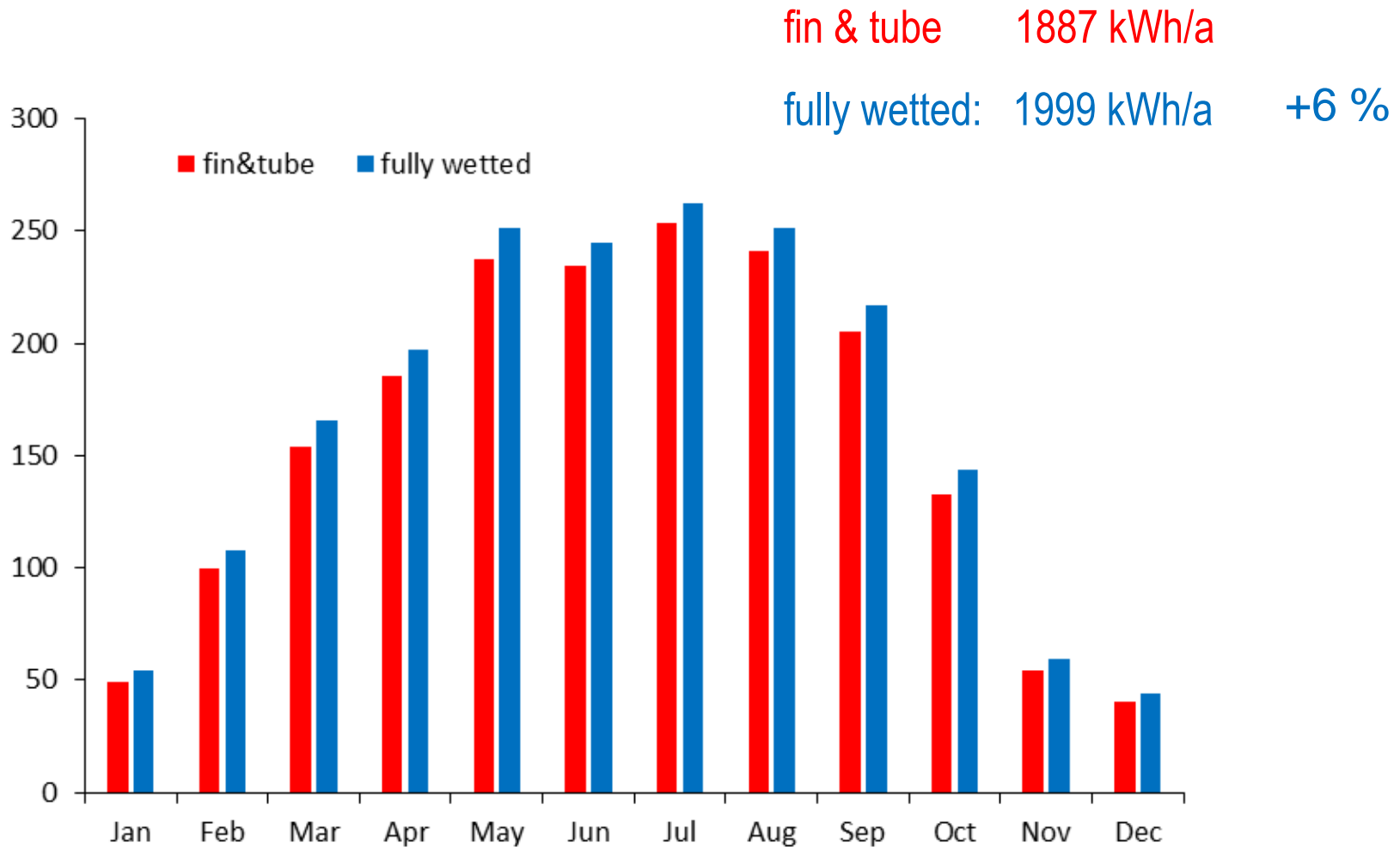
Fully wetted absorber vs. fin&tube

- how can the absorber geometry influence the annual energy yields of collector?

■ fin&tube	$\eta_0 = 0.789$	$a_1 = 4.857$	$a_2 = 0.006$
■ fully wetted	$\eta_0 = 0.877$	$a_1 = 5.371$	$a_2 = 0.007$
- open studio SDHW-SOLNET in TRNSYS
- make a change of coefficients in KOLEKTOR type
- results of collector yield find under Totals.txt
- **compare the annual sums for both alternatives**



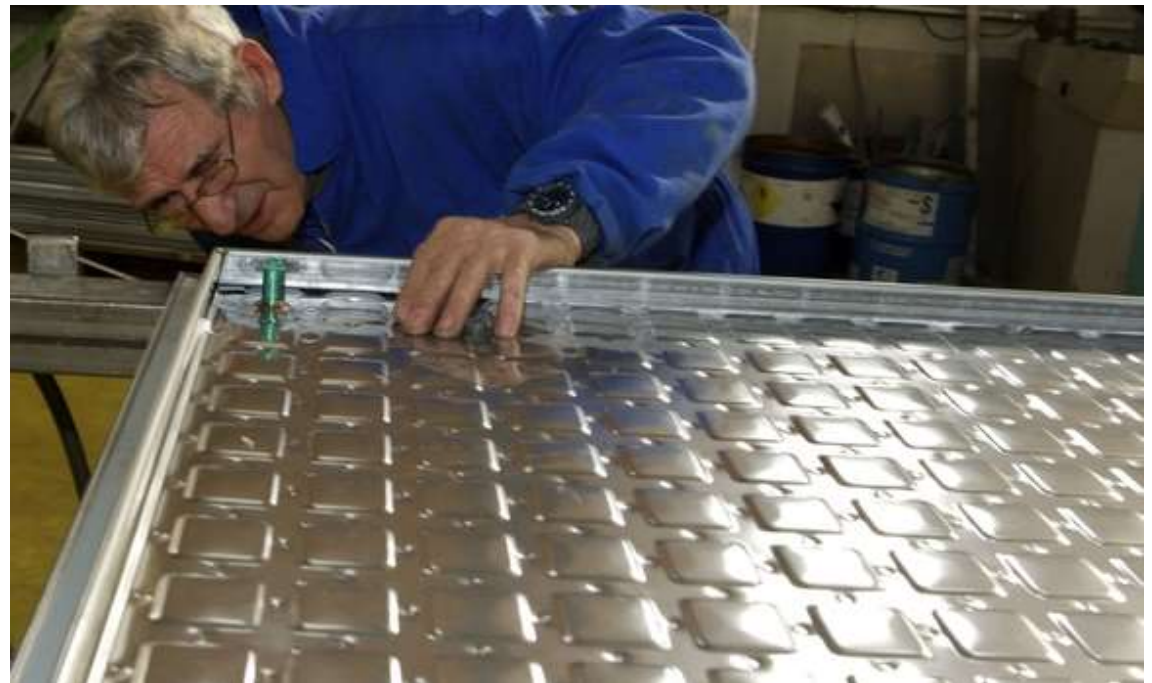
Fully wetted absorber vs. fin&tube





Fully wetted absorber vs. fin&tube

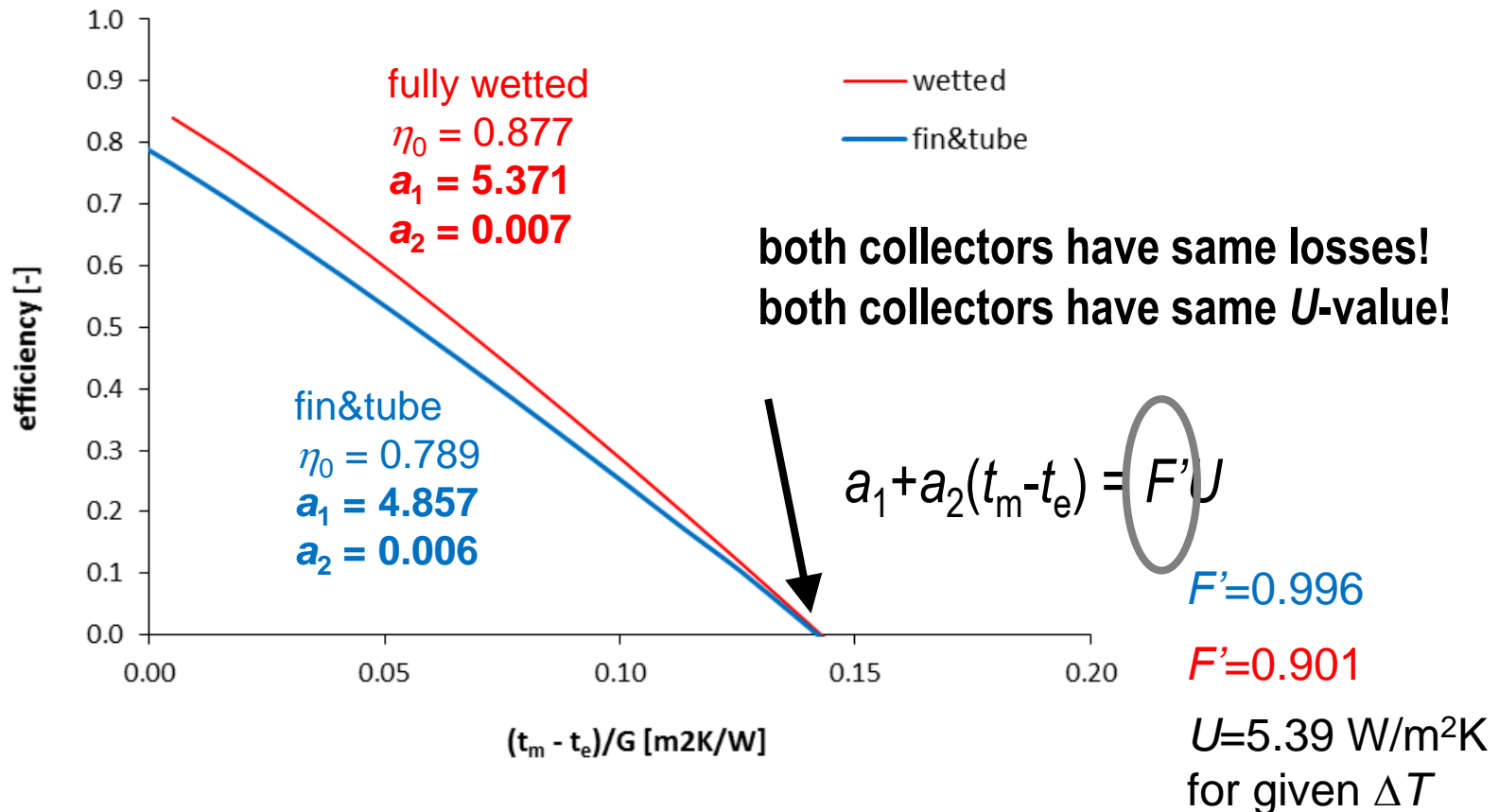
- fully wetted absorber could improve the annual energy performance by more than 5 % while **steel** could be cheaper material than copper





Fully wetted absorber vs. fin&tube

- did we make a mistake in calculation? can geometry influence losses?



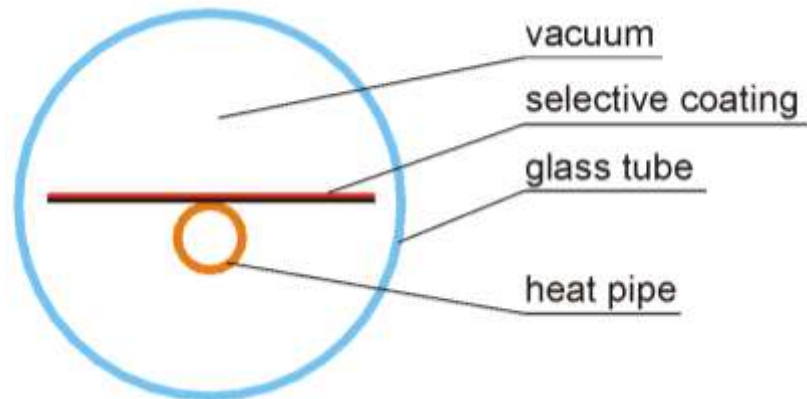
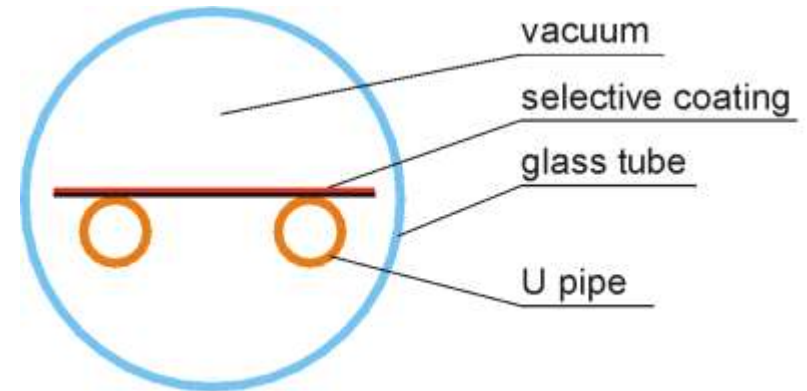
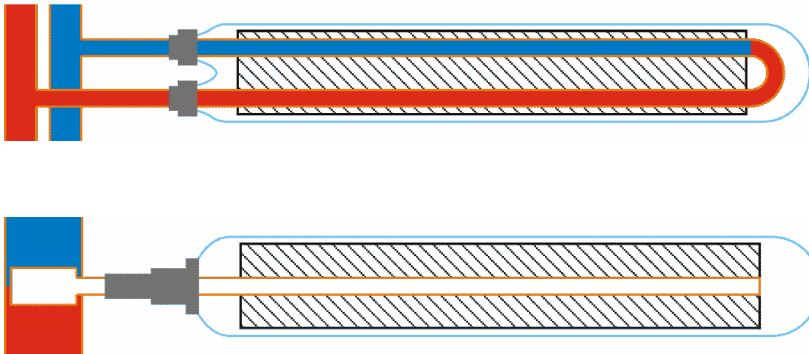
coefficients η_0 , a_1 , a_2 are one complex and cannot be separated



Vacuum tube collectors x efficiency factor

Single glass vacuum tube / flat absorber

- direct flow
- concentric direct flow
- heat pipe



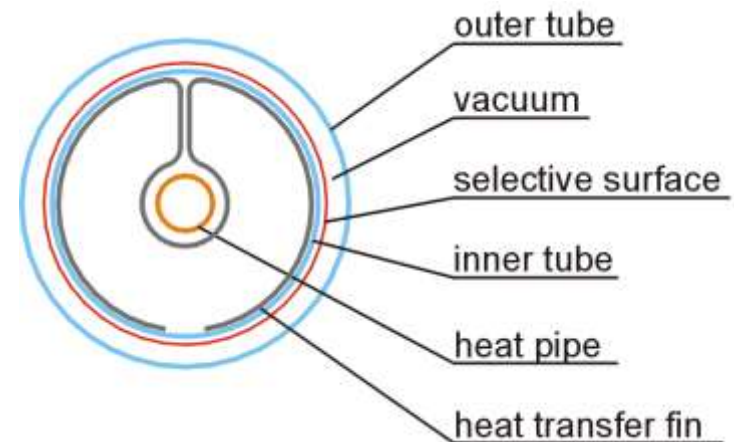
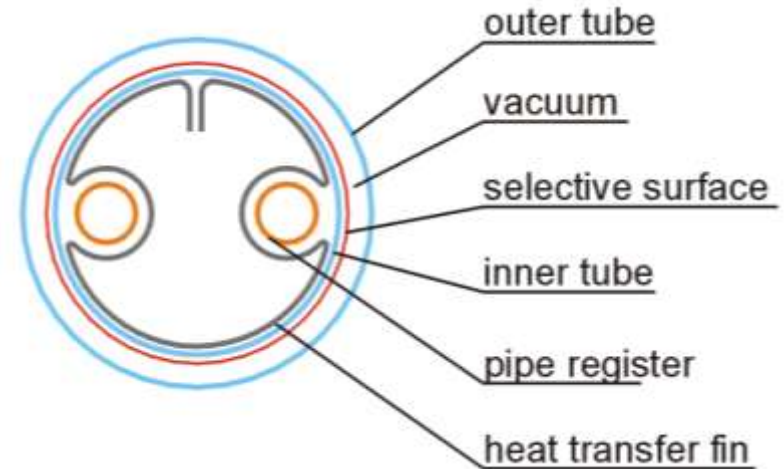
firm metal contact absorber-pipe provides high F'



Vacuum tube collectors x efficiency factor

Double-glass (Sydney) vacuum tube

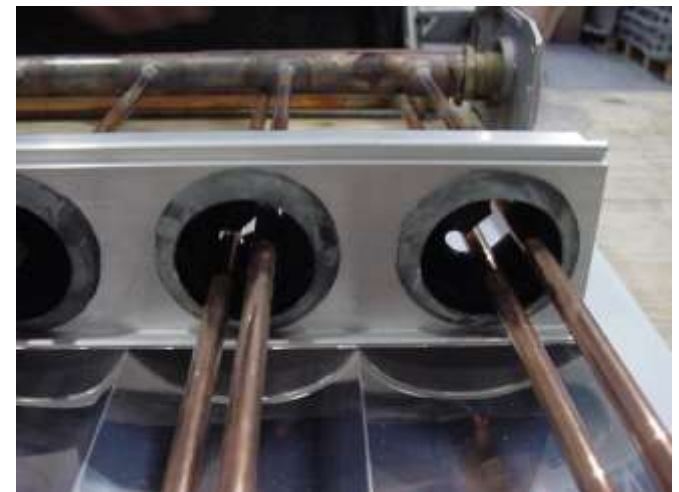
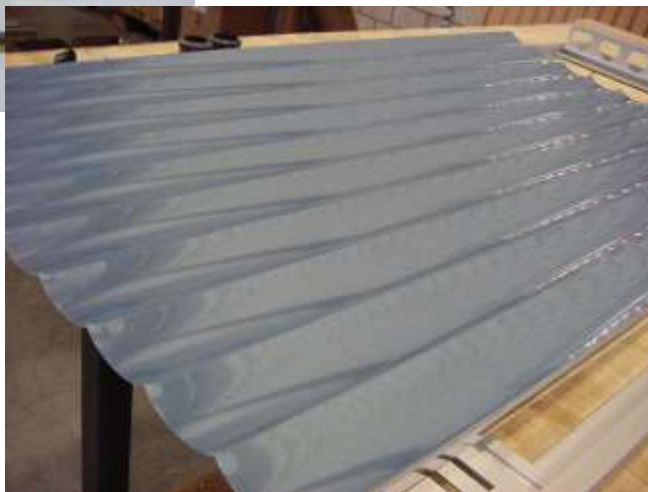
- all glass concentric tube (Dewar)
 - cylindric absorber (internal) glass tube
 - cover (external) glass tube
 - vacuum in space between
- **absorber coating** applied on exterior surface of internal glass tube
- conductive heat transfer fin in contact with interior surface



problematic contact absorber-pipe ...



Sydney vacuum tube collectors



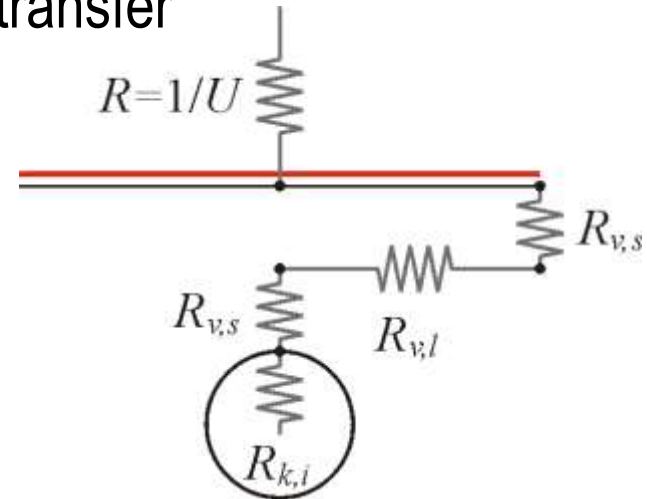


Thermal analysis of direct flow VTC

given by Sydney tube

$$\eta = F' \left[\tau\alpha - U \frac{(t_m - t_a)}{G} \right]$$

tube collector scheme of heat transfer



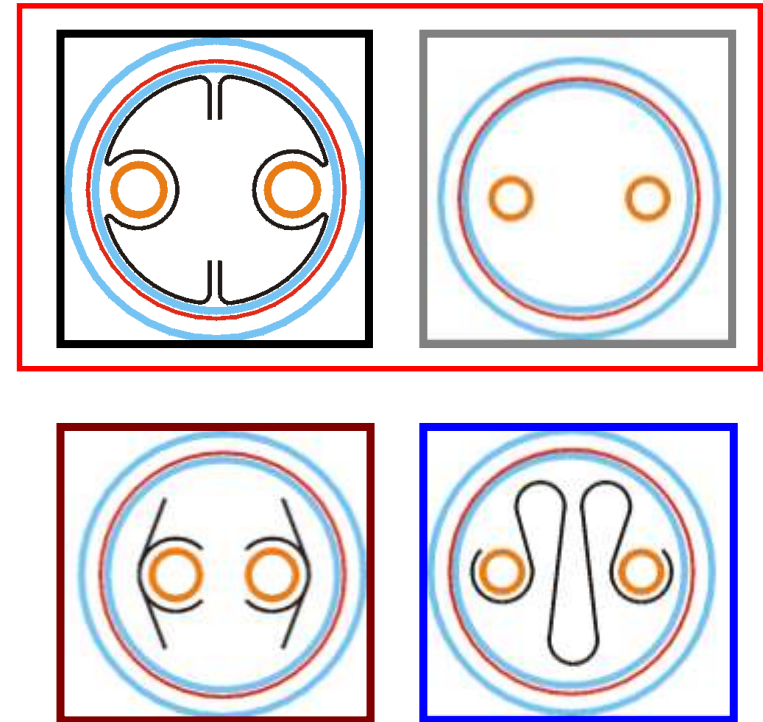
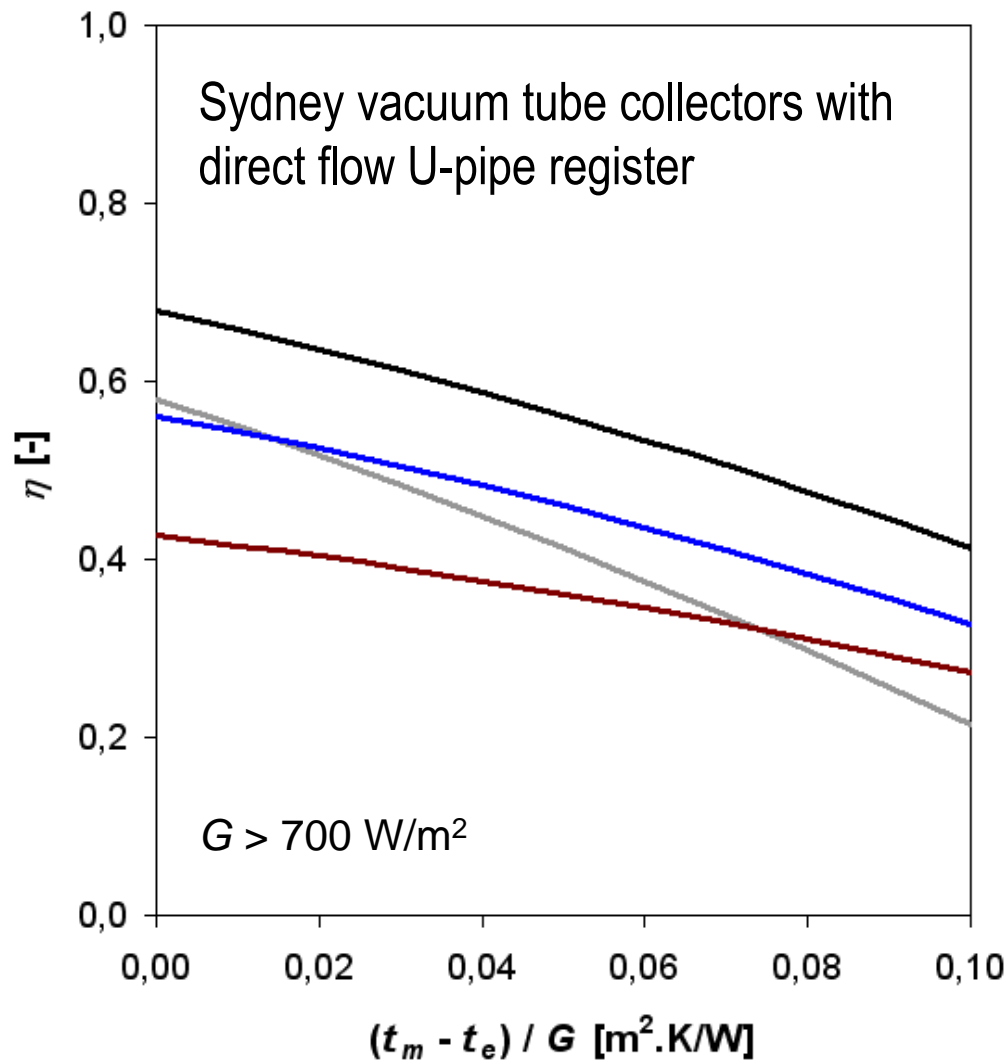
contact fin: short (W), conductive (λ), thick (d)

bond-contact: conductive; absorber tube-fin, fin-pipes

heat removal: laminar / turbulent flow in pipes



Influence of contact fin



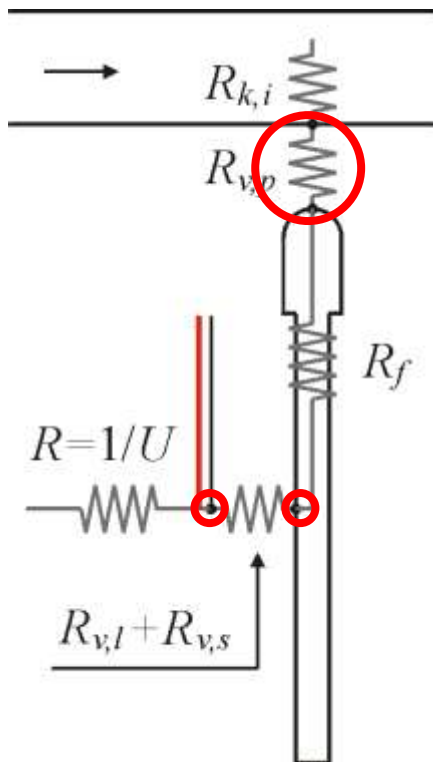
contact fin is a principle element in Sydney collector



Contact resistance in heat pipe VTC

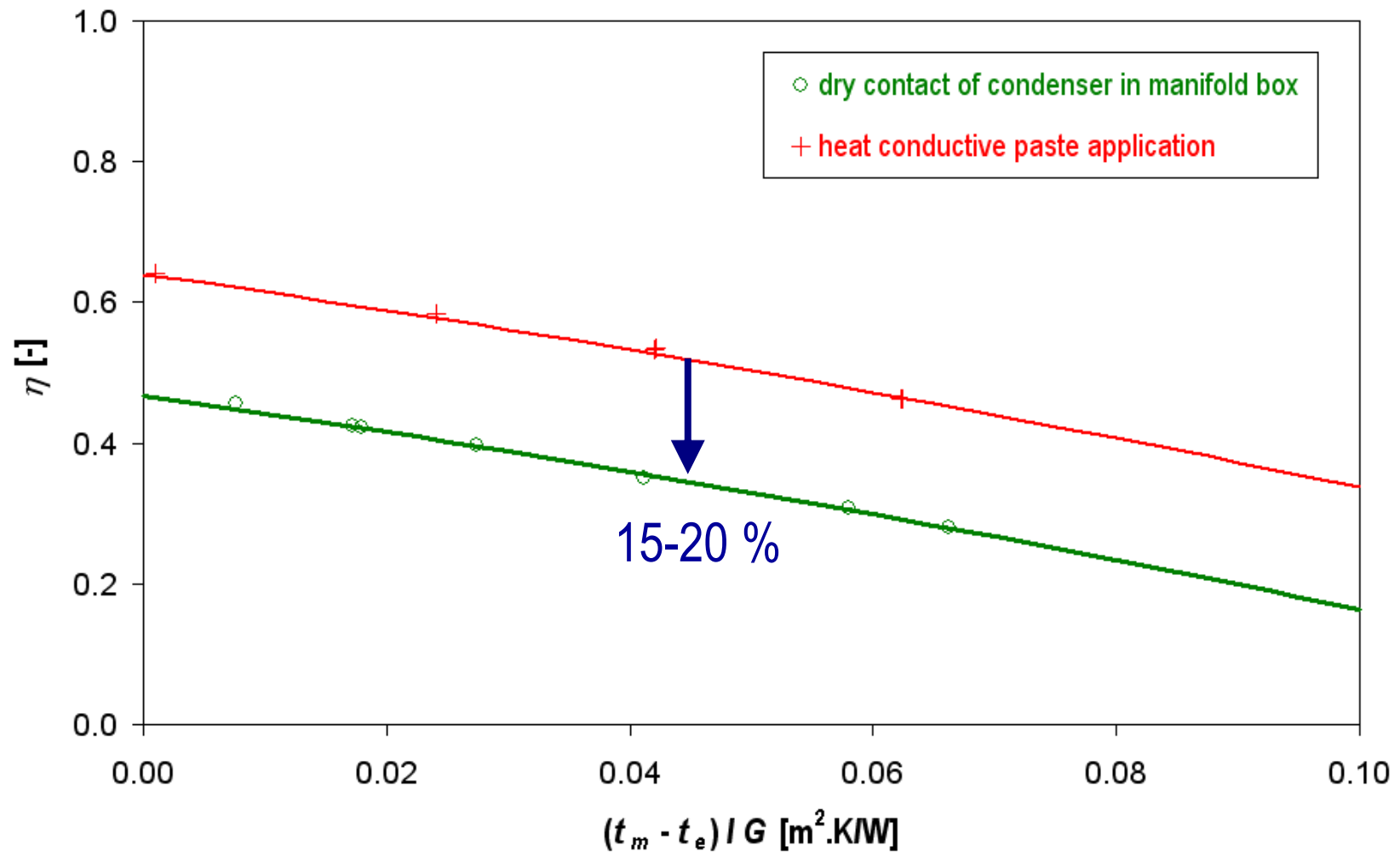
Heat pipe (phase change of working liquid, high heat transfer coefficients)

- evaporator (in contact with fin transferring the heat from inner glass tube)
- condenser (placed into manifold box)



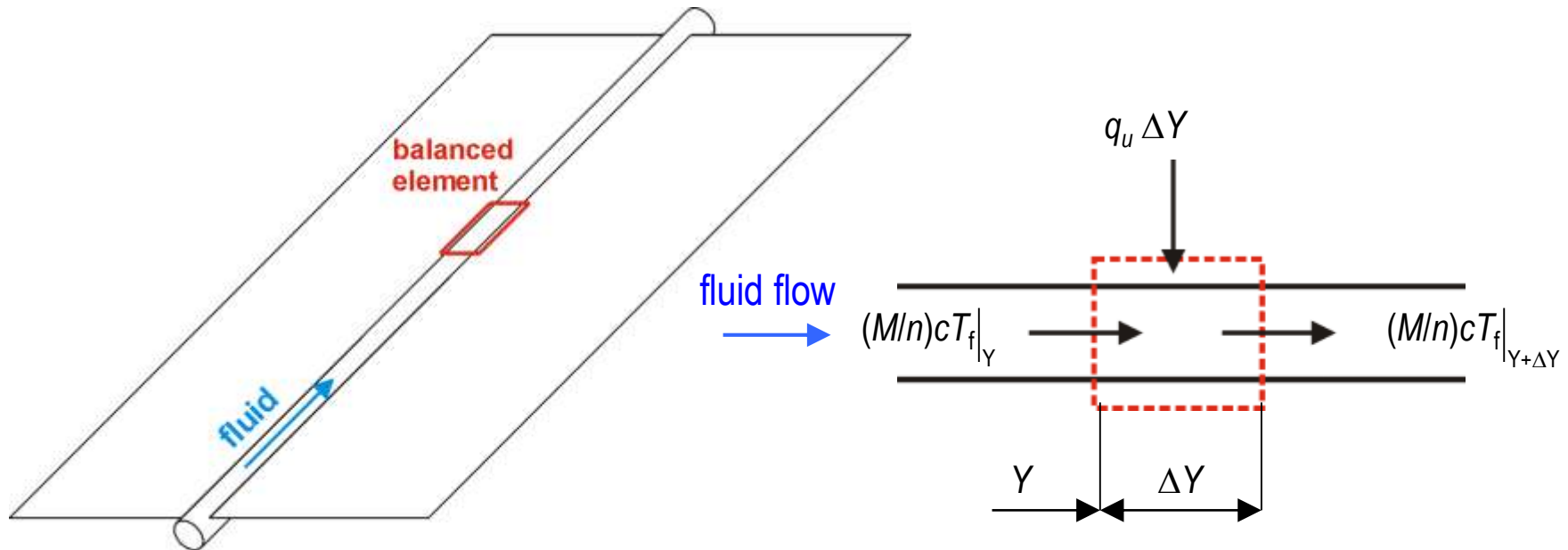


Contact resistance in heat pipe VTC





Temperature distribution in flow direction



derivation of temperature distribution between tubes (in absorber fin)

$$\left(\frac{\dot{M}}{n}\right)cT_f|_y - \left(\frac{\dot{M}}{n}\right)cT_f|_{y+\Delta y} + \Delta y q'_u = 0$$

yields in solution of differential equation of 1st order



Heat removal factor F_R

mathematical derivation of temperature profile: see *Duffie, Beckman (2006)*

definition: relates the actual collector gain to gain if absorber surface at fluid inlet temperature

$$F_R = \frac{\dot{M}c(t_{out} - t_{in})}{A_c[\tau\alpha G - U(t_{in} - t_a)]}$$

$$F_R = \frac{\dot{M}c}{A_c U} \left[1 - \exp\left(-\frac{A_c U F'}{\dot{M}c}\right) \right]$$

equivalent to **effectiveness of heat exchanger**, ratio of actual heat transfer to maximum possible heat transfer



Heat removal factor F_R

heat removal factor is dependent on:

- efficiency factor F' (geometry, quality of absorber, fin efficiency F , ...)
- collector U -value (heat losses)
- specific heat of fluid c (type of fluid)
- specific mass flow through collector M / A_c (thermal capacity of flow)



Water vs. propylene glycol

- **how can the heat transfer fluid influence the thermal performance of the solar collector?**
- influence on efficiency curve – collectors are tested with water, does anything change when filled with glycol?
- **propylene glycol / water**
 - mixture 50 % / 50 % for freezing point -32 °C
 - 8x viscous at 20 °C, high influence of temperature, only 2x at 80 °C
 - lower specific heat by cca 25 %
 - worse heat transfer

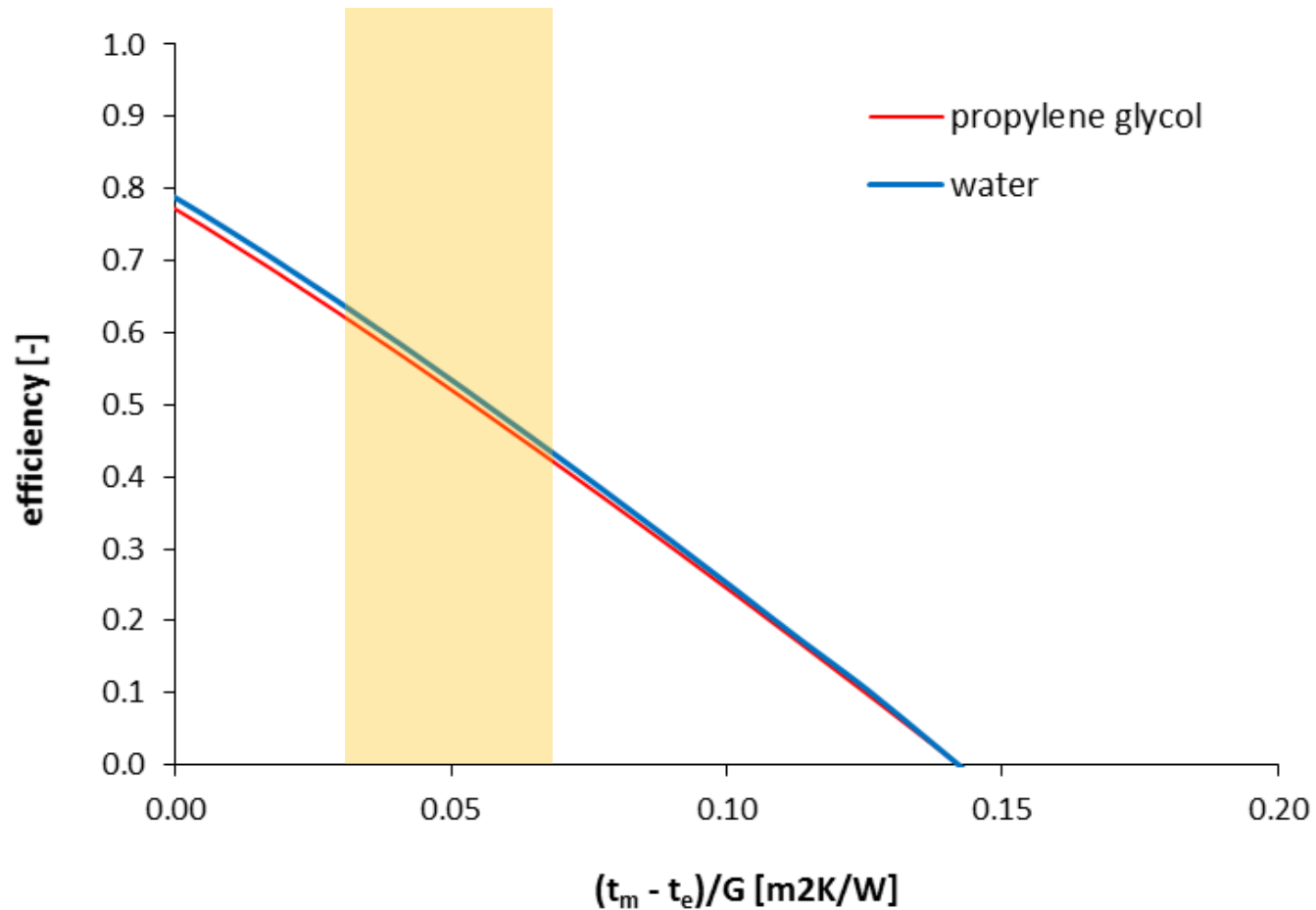


Water vs. propylene glycol

- run KOLEKTOR programme, open **default.kol**
- Absorber card make the change of fluid
- Calculation card select Efficiency curve calculation
 Calculate, Export results
- open Evaluation.xls
- make a copy for glycol alternative
- open res file in excel, mind the semicolons as separators
- **compare the efficiency curves based on $(t_m - t_e)/G$**

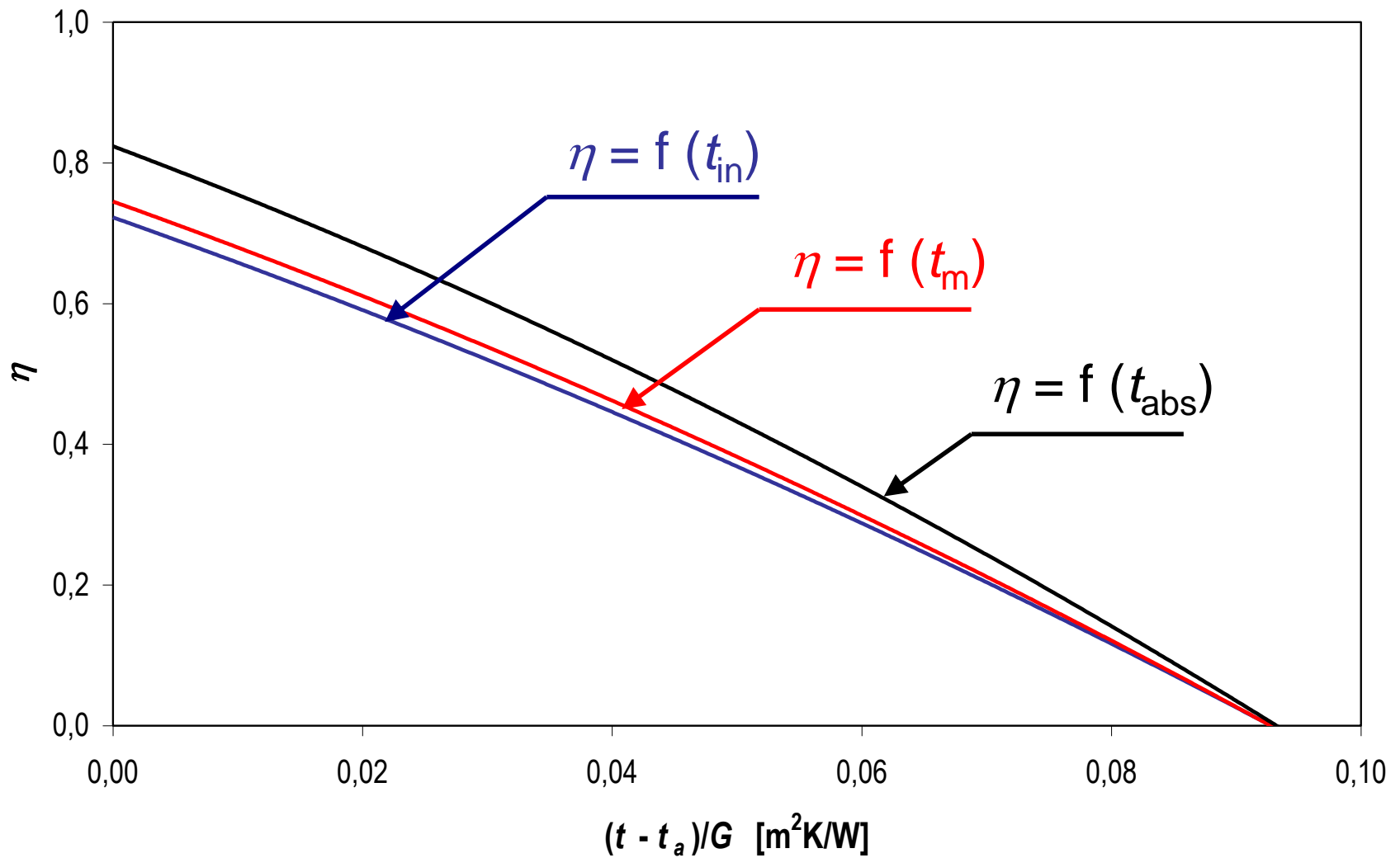


Water vs. propylene glycol





Efficiency curve





Useful heat output of solar collector

based on absorber temperature, external balance of absorber

$$\dot{Q}_u = A_c [\tau \alpha G - U(t_{abs} - t_a)]$$

based on mean fluid temperature, experimental work

$$\dot{Q}_u = F' A_c [\tau \alpha G - U(t_m - t_a)]$$

based on fluid inlet temperature, simulation tools

$$\dot{Q}_u = F_R A_c [\tau \alpha G - U(t_{in} - t_a)]$$



Solar collector temperatures

mean absorber temperature

$$t_{\text{abs}} = t_{\text{in}} + \frac{\dot{Q}_u / A_c}{F_R U} (1 - F_R)$$

mean fluid temperature

$$t_m = t_{\text{in}} + \frac{\dot{Q}_u / A_c}{F_R U} \left(1 - \frac{F_R}{F'}\right)$$

based on

fluid inlet temperature

fluid output temperature

$$t_{\text{out}} = 2t_m - t_{\text{in}}$$



Solar collector efficiency

based on absorber temperature

$$\eta = \tau\alpha - U \frac{(t_{abs} - t_a)}{G}$$

based on mean fluid temperature

$$\eta = F' \left[\tau\alpha - U \frac{(t_m - t_a)}{G} \right]$$

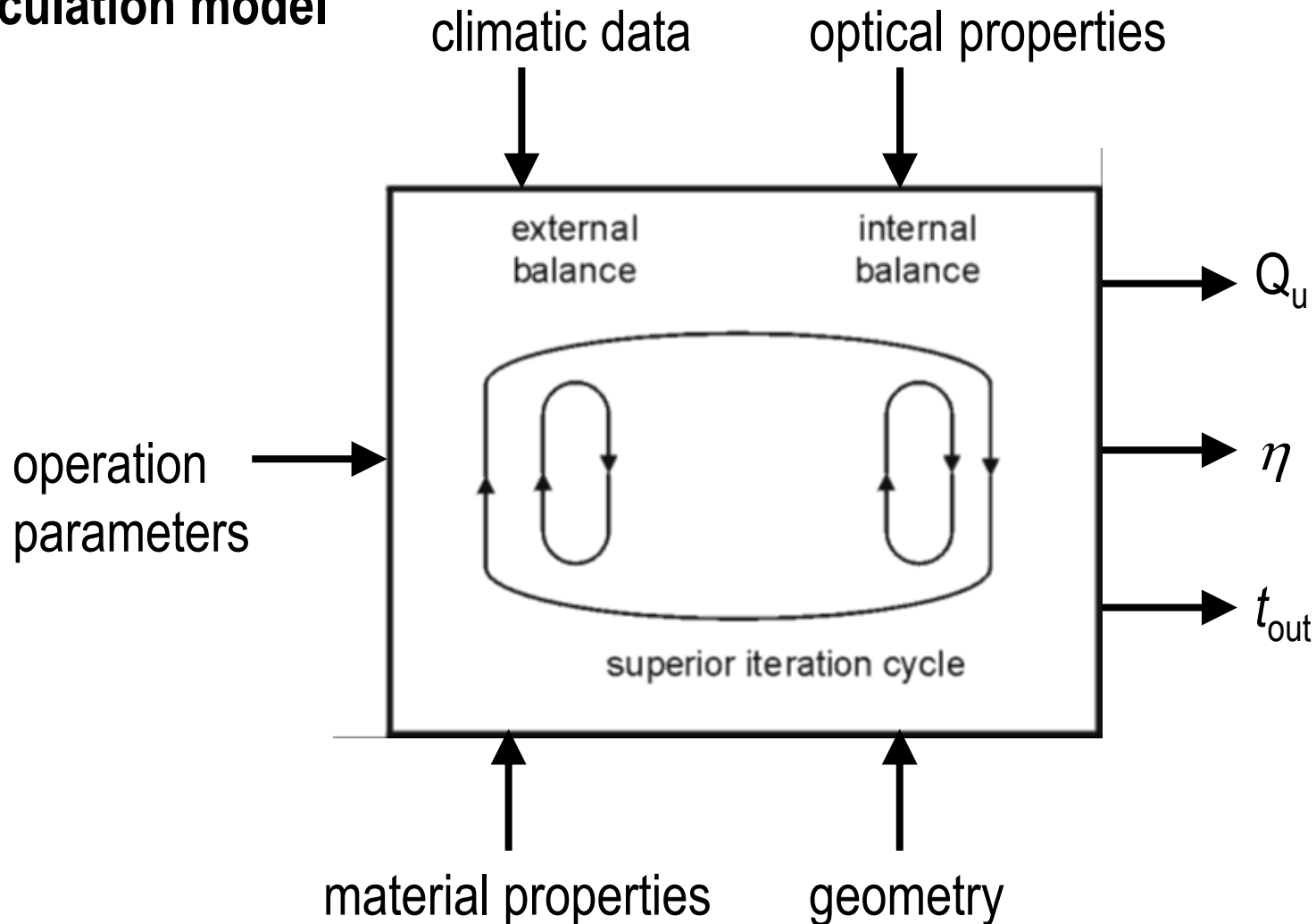
based on fluid inlet temperature

$$\eta = F_R \left[\tau\alpha - U \frac{(t_{in} - t_a)}{G} \right]$$



Solar collector performance calculation

calculation model





Conclusions of the day

- KOLEKTOR is a design tool for virtual prototyping
 - to perform calculations of designs without need for fabrication prototypes
 - to optimize construction and design of collector
- KOLEKTOR is not perfect, but relevant TRNSYS type is on the way
 - for modelling solar thermal collectors (Slava Shemelin)
 - extension for glazed PVT collectors (Nikola Pokorny)
- efforts for extremely high performing solar thermal collectors could be sometimes useless if target is annual performance and not marketing