

## Double integrals, Elementary Domain of Integration (EDI)

1. Given  $f(x, y) = \frac{1}{\sqrt{9-x^2-y^2}}$ .  
 $\exists? \iint_D f(x, y) dx dy$

(a)  $D = \{x, y \in \mathbb{R}^2; x \geq 0 \wedge x^2 + y^2 < 9\}$

(b)  $D = \{x, y \in \mathbb{R}^2; x \geq 0 \wedge x^2 + y^2 \leq 8\}$

2. Given domain in  $\mathbb{R}^2$ , bounded by curves:  $y = x - 1$ ;  $y = -1$ ;  $y = \ln(x)$ .

(a) Sketch the domain and express it as EDI relative to  $y$ -axis.

(b) Express the domain as EDI relative to  $x$ -axis.

(c) Compute area of the domain.

3. Given curves:  $y^2 = x + 2$ ;  $y = x$ .

(a) Sketch a domain bounded between them and determine intersection points.

(b) Express the domain as EDI relative to  $y$ -axis.

(c) Compute area of the domain.

4. Given domain  $D = \{x, y \in \mathbb{R}^2; x \geq 0 \wedge x + y \leq 2 \wedge y \geq \sqrt{x}\}$ .  
To the given function  $f(x, y) = xy$  compute  $\iint_D f(x, y) dx dy$ .

5. Change the order of integration:

$$\int_1^e \left( \int_0^{\ln(x)} f(x, y) dy \right) dx$$

6. Reverse the order of integration (a):

$$\int_0^1 \left( \int_1^{x+1} e^x dy \right) dx$$

and compute the double integral (b).