

Conservative fields, potential

- $\vec{f}(x, y) = (xy, x + y)$.
 - Where is \vec{f} conservative?
 - Find its potential $\varphi(x, y)$.
 - Compute the work done (line integral) along line segment between $A = [1; 3]$ and $B = [1; 2]$.
- $\vec{f}(x, y) = (x^2, y^2)$.
 - Where is \vec{f} conservative?
 - Find its potential $\varphi(x, y)$.
 - Compute the work done (line integral) along line segment between $A = [0; 0]$ and $B = [1; 2]$.
- $\vec{f}(x, y) = -(x - y)^{-2}\vec{i} + (x - y)^{-2}\vec{j}$.
 - Where is \vec{f} conservative?
 - Choose correct potential:
 - $\varphi(x, y) = \frac{1}{y-x} + 2$
 - $\varphi(x, y) = \frac{-1}{y-x} + 1$
 - $\varphi(x, y) = \frac{1}{x-y} + 1$
 - $\varphi(x, y) = \frac{1}{x-y} - \pi$
 - Compute the work done (line integral) along a curve $x^2 + y^2/2 = 2$ in a second quadrant, oriented clockwise.
- To the given potential $\varphi(x, y) = x^2y + c$, ($c \in \mathbb{R}$)
 - determine the constant c if $\varphi = 9$ in $A = [\sqrt{2}; \sqrt{2}]$.
 - find the conservative \vec{f} (corresponding to φ).
 - Compute $\oint_C \vec{f} \cdot \vec{ds}$ where $C : x^2 + y^2 = 4$ oriented counter-clockwise.
- Determine a domain where \vec{f} is conservative and find its potential (if possible).
 - $\vec{f}(x, y) = (x^3y^2 + x, y^2 + yx^4)$
 - $\vec{f}(x, y) = (\ln y - \frac{e^y}{x^2}, \frac{e^y}{x} + \frac{x}{y})$
- To the given potential $\varphi(x, y) = xe^{x+y}$
 - find the conservative \vec{f} (corresponding to φ).
 - Compute $\int_C \vec{f} \cdot \vec{ds}$ where $C : x^2 + y^2 = 1$ in a first quadrant, oriented counter-clockwise.