| A | CONSTRUCTIVE GEOMETRY |  |  |  |  |  | E01A021 |
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| Surname |  |  |  |  |  |  |  |
| First name |  |  |  |  |  |  |  |
| Date |  | Examiner |  |  |  |  |  |
| Score | 1 | 2 | 3 | 4 | 5 | 6 | Total |

1. Construct the rotary solid given by technical drawing in technical isometry. Point $S$ lies at origin and axis of revolution of the solid is identical with $y$-axis of coordinate system.

2. Determine analytically the solid drawn in example 1.

SPHERE R 40


The solid is determined by the following areas.

- Inner area of left hemisphere $\sigma$ given by centre $(S=(0,0,0)$ and radius 40 mm :

$$
y \geqslant-\sqrt{40^{2}-x^{2}-z^{2}}
$$

- Inner area of truncated cone of revolution $\rho$ given by vertex $V=$ $(0,180,0)$, semiaxes $a=c=30, a\|x, c\| z$ and altitude $b=180$ :

$$
\frac{x^{2}}{30^{2}}+\frac{(y-180)^{2}}{180^{2}}+\frac{z^{2}}{30^{2}} \leqslant 0, y \in[0,60]
$$

- Inner area of right hemisphere $\omega$ given by centre $C=(0,60,0)$ and radius 20 mm :

$$
y \leqslant \sqrt{20^{2}-x^{2}-z^{2}}
$$

3. Involute motion is given by fixed centrode $p$ and moving centrode $h$. Considering the continuous part of fixed centrode only, construct three new positions of moving circle $c$. Construct points of contact between circle $c$ and its envelope $(c)$ at all positions and sketch the envelope $(c)$.

4. Construct the development of oblique cylinder $\sigma$.

5. Two surfaces of revolution $\sigma=(m, o)$ and $\sigma^{\prime}=\left(m^{\prime}, o^{\prime}\right)$ are given. Using Monge projection, construct intersection curve $q=\sigma \cap \sigma^{\prime}$. Indicate the visibility.
6. Helicoidal surface $\sigma=\left(k, o, v_{0}\right.$, right-handed $)$ is given. Using Monge projection, construct the right principal half-meridian $m$ of helicoidal surface $\sigma$.

