

- 1) James and Edith will come.
- 2) Margaret or David will come.
- 3) If Jane comes, then Andrew will come too.
- 4) Charles will come if and only if Katy comes.

- **Negate each statement:**

- 1) James will not come or Edith will not come. ( $\neg A \vee \neg B$ )
- 2) Margaret will not come and David will not come. ( $\neg A \wedge \neg B$ )
- 3) Jane will come and Andrew will not come. ( $A \wedge \neg B$ )
- 4) Charles will not come if and only if Katy comes. ( $\neg A \Leftrightarrow B$ )  
Charles will come if and only if Katy does not come. ( $A \Leftrightarrow \neg B$ )

$$x + y = 10$$

Determine, what statement is true:

- $\forall x \in \mathbf{N} \forall y \in \mathbf{R} : x + y = 10$
- $\forall y \in \mathbf{N} \exists x \in \mathbf{Z} : x + y = 10$
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- $\exists y \in \mathbf{R} \exists x \in \mathbf{R} : x + y = 10$

$$x + y = 10$$

Determine, what statement is true:

- $\forall x \in \mathbf{N} \forall y \in \mathbf{R} : x + y = 10$  ✗
- $\forall y \in \mathbf{N} \exists x \in \mathbf{Z} : x + y = 10$  ✓
- $\exists x \in \mathbf{Z} \forall y \in \mathbf{N} : x + y = 10$  ✗
- $\forall x \in \mathbf{Z} \exists y \in \mathbf{N} : x + y = 10$  ✗
- $\exists y \in \mathbf{N} \forall x \in \mathbf{Z} : x + y = 10$  ✗
- $\exists y \in \mathbf{R} \exists x \in \mathbf{R} : x + y = 10$  ✓

$$x \cdot y = 0$$

Determine, what statement is true:

- $\forall y \in \mathbf{R} \exists x \in \mathbf{N} : x \cdot y = 0$
- $\exists x \in \mathbf{N} \forall y \in \mathbf{R} : x \cdot y = 0$
- $\forall x \in \mathbf{R} \exists y \in \mathbf{Z} : x \cdot y = 0$
- $\exists y \in \mathbf{Z} \forall x \in \mathbf{R} : x \cdot y = 0$

**"If little Peter is well-behaved, he will get a cake."**

Now, let's analyze the truth values of the following statements based on the given conditional sentence:

- A) Peter was well-behaved, he got a cake.
- B) Peter was well-behaved, he did not get a cake.
- C) Peter was not well-behaved, he got a cake.
- D) Peter was not well-behaved, he did not get a cake.

**"If it rained, then it will be wet outside."**

Determine if it is true and create the reverse implication:

- $A \Rightarrow B \rightarrow$  If it rained, then it will be wet outside. ✓
- $B \Rightarrow A \rightarrow$  If it is wet outside, then it rained. ✗
- $\neg B \Rightarrow \neg A \rightarrow$  If it is not wet outside, then it did not rain.  
✓ (True, this is the contrapositive = logically equivalent)

**"If a street lamp falls, then the world will end."**

Determine if it is true and create the reverse implication:

- $A \Rightarrow B \rightarrow$  If a street lamp falls, then the world will end. ✕
- $B \Rightarrow A \rightarrow$  If the world ends, then a street lamp will fall. ✓
- $\neg B \Rightarrow \neg A \rightarrow$  If the world does not end, then the street lamp will not fall. ✕