NMA – homework from week 4

1. Explicit and implicit Euler's method

Consider Cauchy problem

$$y' = -2y + 2x$$
, $y(0) = 2$.

- (a) Find the interval of maximal solution.
- (b) Choose step-size h = 0.25 and using explicit Euler method compute approximate value of y(0.5).
- (c) Choose step-size h = 0.5 and using implicit Euler method compute approximate value of y(0.5).

2. Midpoint (Collatz) method

Consider Cauchy problem

$$y' = -y + x$$
, $y(0) = -1$.

- (a) Find the interval of maximal solution.
- (b) Choose step-size h = 0.5 and using the midpoint method compute approximate value of y(0.5).